Neural Action Policy Safety Verification: Applicablity Filtering

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Abstract

Neural networks (NN) are an increasingly important representation of action policies π. Applicability filtering is a commonly used practice in this context, restricting the action selection in π to only applicable actions. Policy predicate abstraction (PPA) has recently been introduced to verify safety of neural π, through over-approximating the state space subgraph induced by π. Thus far however, PPA does not permit applicability filtering, which is challenging due to the additional constraints that need to be taken into account. Here we overcome that limitation, through a range of algorithmic enhancements. In our experiments, our enhancements achieve several orders of magnitude speed-up over a baseline implementation, bringing PPA with applicability filtering close to the performance of PPA without such filtering.

1 Introduction

Neural networks (NN) are an increasingly important representation of action policies in many contexts, including AI planning (Issakkimuthu, Fern, and Tadepalli 2018; Groshev et al. 2018; Garg, Bajpai, and Mausam 2019). But how to verify that such a policy π is safe? Given a start condition φ₀ and an unsafe condition φ_u, how to verify whether an unsafe state s₀ |= φ_u is reachable from a start state s₀ |= φ₀ under π? Such verification is potentially very hard as it compounds the state space explosion problem with the difficulty of analyzing even single NN decision episodes. A prominent line of work addresses neural controllers of dynamical systems, where the NN output forms input to a continuous state-evolution function (Tran et al. 2019; Huang et al. 2019; Dutta, Chen, and Sankaranarayanan 2019; Ivanov et al. 2021). A recent thread explores bounded-length verification of neural controllers (Akintunde et al. 2018, 2019; Amir, Schapira, and Katz 2021).

Here we follow up on work on policy predicate abstraction (PPA) by Vinzent et al. (2022; 2023) (henceforth: VEA), which tackles neural policies π that take discrete action choices in non-deterministic state spaces. Like classical predicate abstraction (Graf and Sáidi 1997), PPA builds an over-approximating abstraction defined through a set P of predicates, i.e., linear constraints over the state variables. However, PPA abstracts not the full state space, but the subgraph induced by π. To compute the abstract state space Θπ, one must repeatedly solve the sub-problem of deciding whether there is a transition from abstract state s_P to abstract state s'_P under π. This abstract transition problem is encoded into satisfiability modulo theories (SMT) (Barrett and Tinelli 2018), and answered querying solvers tailored to NN analysis (Katz et al. 2019). If there does not exist a path from φ₀ to φ_u in Θπ, then π is safe. Counterexample-guided abstraction refinement (CEGAR) (Clarke et al. 2003) is deployed to iteratively refine P until either π is proven safe or an unsafe counterexample is found. In an empirical evaluation, VEA show that their approach outperforms encodings into the state-of-the-art verification tool NuXmv (Cavada et al. 2014).

VEA consider neural policies that may select any action in any state, including inapplicable actions. This makes it unnecessarily difficult to learn good policies. Instead, an established practice is to filter the selection of π with respect to applicability (Toyer et al. 2020; Stahlberg, Bonet, and Geffner 2022). On the verification side, however, applicability filtering is challenging since it introduces additional disjunctive behavior into the abstract transition problem: π may select action label l depending on whether another action l’ is or is not applicable. Implemented straightforwardly, PPA with applicability filtering suffers from a huge performance loss. In our experiments on VEA’s benchmarks, it runs out of time or memory on all but the smallest instances – which, without applicability filtering, PPA tackles in a few seconds. In this paper, we devise a range of algorithmic enhancements that overcome this limitation. The enhancements exploit SMT-solver-specific encoding strategies, and simplify disjunctions in the SMT encoding of the applicability filter based on entailment of sub-constraints. Empirically, these methods achieve runtime improvements of up to three orders of magnitude, and bring PPA with applicability filtering close to the performance of PPA without such filtering.

We also refine VEA’s notion of safety, in that we consider the more accurate reach-avoid setting where the task of the learned policy is to reach a goal state while avoiding unsafe states. Policy executions in reach-avoid stop at goal states. In VEA’s prior work, a policy can, at least in principle, be unsafe even though unsafe states are encountered only after reaching the goal.
2 Preliminaries

We consider discrete non-deterministic transition systems described by a tuple \((V, L, O)\) where \(V\) is a finite set of bounded-integer state variables, \(L\) is a finite set of action labels and \(O\) is a finite set of operators. We denote by \(\text{Exp}\) the set of linear expressions over \(V\), i.e., of the form \(\sum v \in V d_v v + c\) with coefficients \(d_v \in \mathbb{Z}\) for each \(v \in V\) and \(c \in \mathbb{Z}\). Accordingly, \(C\) denotes the set of linear constraints, of the form \(\sum v \in V d_v v \geq c\), and Boolean combinations thereof.\(^1\) An operator \(o \in O\) is a tuple \((l, g, u)\) with label \(l \in L\), guard \(g \in C\) (a conjunction of linear constraints), and (linear) update \(u : V \rightarrow \text{Exp}\).

The state space of \((V, L, O)\) is a labeled transition system \(\Theta = (S, L, T)\). The set of states \(S\) is the finite set of all complete variable assignments over \(V\). The set of transitions \(T \subseteq S \times L \times S\) contains \((s, l, s')\) iff there exists an operator \(o = (l, g, u)\) such that \(g\) is satisfied over \(s\), formally \(g(s)\) evaluates to true, also abbreviated \(s \models o\), and \(s'(v)\) maps to the update \(u(v)\) evaluated over \(s\) for each \(v \in V\), formally \(s' = \{v \mapsto u(v)(s) \mid v \in V\}\), also abbreviated \(s' = s[o]\). The separation between action labels and operators allows both, state-dependent effects (different operators with the same label \(l\) applicable in different states) and action outcome non-determinism (different operators with the same label \(l\) applicable in the same state).

An action policy \(\pi\) is a function \(S \rightarrow L\). We consider \(\pi\) represented by a neural network (NN). Specifically, we focus on feed-forward NN with rectified linear unit (ReLU) activations \(\text{ReLU}(x) = \max(x, 0)\). These NN consist of an input layer, arbitrarily many hidden layers, and an output layer with one neuron per label \(l \in L\). A safety property is a pair \((\phi_0, \phi_u)\), where \(\phi_0 \in C\) and \(\phi_u \in C\) identify the set of start and unsafe states respectively. A policy \(\pi\) is unsafe with respect to \((\phi_0, \phi_u)\) iff there exists a state path \((s_0, \ldots, s_n)\) such that \(s_0 \models \phi_0\), \(s_n \models \phi_u\), and \((s_i, \pi(s_i), s_{i+1})\) \(\in T\) for \(i \in \{0, \ldots, n-1\}\). Otherwise \(\pi\) is safe.

Policy predicate abstraction (PPA) (Vinzent, Steinmetz, and Hoffmann 2022) is an extension of classical predicate abstraction (Graf and Saiti 1997). Unlike its classical counterpart, PPA abstracts not the full state space, but the subgraph induced by \(\pi\). Assume a set of predicates \(P \subseteq C\). An abstract state \(s_P\) is a complete truth value assignment over \(P\). \([s_P] = \{s \in S \mid \forall p \in P : p(s) = s_P(p)\}\) denotes the set of concrete states represented by \(s_P\). The policy predicate abstraction of \(\Theta\) over \(P\) and \(\pi\) is the labeled transition system \(\Theta^\pi_P = (S_P, L, T^\pi_P)\) where \(S_P\) is the set of abstract states over \(P\) and \((s_P, l, s_P')\) \(\in T^\pi_P\) iff there exists \((s, l, s')\) \(\in T\) such that \(s \in [s_P]\), \(s' \in [s_P']\) and \(\pi(s) = l\).

Analogously to safety, \(\Theta^\pi_P\) is said to be unsafe in \(\Theta^\pi_P\) iff there exists an abstract path \((s_P^0, l^0, \ldots, l^{n-1}, s_P^n)\) such that \(s_0 \models \phi_0\) for some \(s_0 \in [s_P^0]\), \(s_n \models \phi_u\) for some \(s_n \in [s_P^n]\), and \((s_P^i, l^i, s_P^{i+1})\) \(\in T^\pi_P\) for \(i \in \{0, \ldots, n-1\}\). Otherwise \(\pi\) is safe in \(\Theta^\pi_P\), in which case it is safe in \(\Theta\) as well. An (unsafe) abstract path in \(\Theta^\pi_P\) may be spurious, i.e., there does not exist a corresponding path in \(\Theta\) under \(\pi\). Counterexample-guided abstraction refinement (CEGAR) (Clarke et al. 2003) iteratively removes such spurious abstract paths by refining \(P\), until either the abstraction is proven safe, or a non-spurious abstract path is found proving \(\pi\) unsafe. VEA provide a CEGAR framework specialized to PPA (Vinzent, Sharma, and Hoffmann 2023).

To compute \(\Theta^\pi_P\), one must solve the abstract transition problem for every possible abstract transition: \((s_P, l, s_P') \in T^\pi_P\) iff for some \(l\)-labeled operator \(o \in O\) there exists a concrete state \(s \in [s_P]\) such that \(s \models o\), \(s[o] \models [s_P']\) and \(\pi(s) = l\). In the classical setting where no policy is considered and thus condition \(\pi(s) = l\) is not needed, such abstract transition problems are routinely encoded into satisfiability modulo theories (SMT) (e.g. (Barrett and Tinelli 2018)). For PPA however, the policy condition \(\pi(s) = l\) introduces a key new source of complexity as the SMT sub-formula representing the neural network \(\pi\) contains one non-linear constraint for every ReLU activation. VEA show how this can be dealt with through approximate SMT checks – embedded into an exact decision procedure. In particular, they use continuous relaxations of the bounded-integer state variables, which can be dispatched to Marabou (Katz et al. 2019), an SMT solver tailored to NN analysis.

3 Applicability Filtering

VEA consider neural action policies that are obtained by applying argmax to the output of the NN. Let \(\pi_1(s)\) be the NN output for label \(l \in L\) given input state \(s \in S\), then \(\pi(s) = \text{argmax}_\pi \pi_1(s)\). Such \(\pi\) may select any label in any \(l \in L\) state, even if it is not applicable, i.e., there does not exist \(s' \in S\) such that \((s, l, s') \in T\) or equivalently, there does not exist an \(l\)-labeled operator \(o\) with \(s \models o\).

From a learning perspective, allowing \(\pi\) to select inapplicable actions is unnecessarily difficult, as \(\pi\) must learn which actions are applicable in which state. A simple commonplace technique to avoid this is to filter the selection of \(\pi\) with respect to applicability (e.g. (T øyer et al. 2020)). Formally, the policy under applicability filtering is defined

\[
\pi_{\text{af}}(s) = \begin{cases} 
\text{argmax}_\pi \pi_1(s) & \text{if } \exists o \in O : s \models o \\
\tau & \text{otherwise}
\end{cases}
\]

where \(O_\tau = \{l \mid \exists o \in O : s \models o\}\) is the set of \(l\)-labeled operators and \(\tau\) is a \(l\) is a noop-label \(l \in L\) with \(O_\tau = \emptyset\), which we define to be selected iff \(s\) is terminal and \(\text{argmax}_\tau\) is undefined (cf. Section 5).

From a verification perspective, applicability filtering also is desirable because, without such filtering, a policy may be safe simply because of stalling, selecting an inapplicable action which ends policy execution. However, applicability filtering adds an additional source of complexity to the abstract transition problem, specifically to the policy condition \(\pi(s) = l\). In what follows, we focus on the SMT encoding of this sub-problem. The encoding of the neural network itself remains unaffected. We provide a full specification in an online TR (Vinzent and Hoffmann 2024).
Let $\pi_l$ denote the SMT variable representing the NN output of label $l$. Without filtering, the policy selection condition is a simple conjunction $\bigwedge_{l' \in \mathcal{L}(l)} \pi_l \supset \pi_{l'}$. Under applicability filtering however, each conjunct here becomes a disjunction $\bigwedge_{l' \in \mathcal{L}(l)} (\pi_l \supset \pi_{l'} \lor \neg \bigwedge_{o \in \mathcal{G}_l} g_o)$ where $g_o$ denotes the guard of operator $o$. In words: either the output value of $l$ is greater than that of $l'$, or $l'$ is not applicable. Since each $g_o$ is a conjunction of linear constraints, the selection condition expands to

$$\bigwedge_{l' \in \mathcal{L}(l)} \left( \pi_l \supset \pi_{l'} \lor \bigwedge_{o \in \mathcal{G}_l} \bigwedge_{i \in \{1, \ldots, m\}} g^i_o \right)$$

where sub-guard $g^i_o$ denotes the $i$-th linear constraint of guard conjunction $g_o$ and $m$ is the guard size. To simplify notation, we assume that $m$ is constant over all guards – any guard can be extended to some maximal $m$ by adding trivially-true constraints.

4 Enhancements

Applicability filtering extends the SMT encoding of the abstract transition problem by a layer of conflated disjunctions. To tackle this new source of complexity, we devise a layer of convoluted disjunctions over $\mathcal{L}(l)\setminus\pi_l$. Let $\phi$ be a disjunction $\bigvee_{i \neq j} \phi^i$ contained in conjunction $\psi$. If, for some $i$ and $j$, $\psi \not\vdash \phi^i$, then $\phi$ can be simplified removing $\phi^j$, i.e., $\bigvee_{i \neq j} \phi^i$. If, for some $i$, $\psi \not\vdash \phi_i$, for every $j$, then $\psi$ entails disjunct $i$ and so the entire disjunction $\phi$. Hence, $\psi$ can be simplified removing $\phi_i$. If $\psi \not\vdash \phi_i$, for some $j$, then the entire disjunct $i$ is infeasible and $\phi$ can be simplified removing $\phi_i$, i.e., $\bigvee_{i \neq j} \phi_i$. If all disjuncts $i$ are infeasible, then the entire disjunction $\phi$ is infeasible and so is $\psi$. We apply entailment information to optimize the encoding of disjunctions on two levels.

Firstly, on a per operator level (ENTAIL-OP). For each operator $o$, VEA’s algorithm to compute $\Theta^P_o$ runs an applicability test $\exists s \in [s_P]: s \models o$. If this test fails then the guard conjunction $g_o$ is entailed to be infeasible in abstract state $s_P$. Say $o$ is $l'$-labeled. We can use this entailment information to simplify the policy condition for any label $l \neq l'$.

Secondly, on a generic linear level (ENTAIL-GEN) with entailed $\phi$ in the form of a linear constraint $\sum_{v \in \mathcal{V}} d_v \cdot v \geq c$.

Let $lo_v(\psi)$ and $up_v(\psi)$ denote a lower and upper bound for $v$ entailed by $\psi$ respectively. Then $\psi$ entails $\phi$ if

$$\sum_{v \in \mathcal{V}^+} d_v \cdot lo_v(\psi) + \sum_{v \in \mathcal{V}^-} d_v \cdot up_v(\psi) \geq c$$

where $\mathcal{V}^+ = \{v \in \mathcal{V} \mid d_v > 0\}$ denotes the variable set with positive coefficients, and $\mathcal{V}^- = \{v \in \mathcal{V} \mid d_v < 0\}$ the variable set with negative coefficients. Analogously, $\psi$ entails $\neg\phi$, we also say $\phi$ is infeasible, if

$$\sum_{v \in \mathcal{V}^+} d_v \cdot up_v(\psi) + \sum_{v \in \mathcal{V}^-} d_v \cdot lo_v(\psi) < c$$

in the form of the abstract transition problem syntactically entails variable bounds in that many predicates in $p$ are bound constraints $v \geq c$ and, thereby, the conditions $s \in [s_P]$ and $s[l] \in [s_P]$ involve bound tightenings. In addition, Marabou deploys techniques to derive tight bounds on the NN outputs (e.g., (Singh et al. 2019)).
The generic entailment check on general linear constraints extends a native check in Marabou for infeasible bound constraints in disjunctions – in our experiments the native check is enabled in our baseline.

5 Reach-Avoid Verification

VEA verify safety of \( \pi \) against an unsafety condition \( \phi_u \) given a start condition \( \phi_0 \). However, the task of a practical policy is not only to avoid unsafe states, but also to reach a goal \( G \) – here, a conjunction \( \bigwedge_i G_i \) of linear constraints \( G_i \in C \). Policy execution stops once \( G \) is reached. This corresponds to a reach-avoid property: avoid \( \phi_u \) while not \( G \). Formally, a policy \( \pi \) is unsafe with respect to \( (\phi_0, \phi_u, G) \) if there exists a path \( (s^0, \ldots, s^n) \) such that \( s^0 = \phi_0, s^n = \phi_u, (s^i, \pi(s^i), s^{i+1}) \in T \) for \( i \in \{0, \ldots, n-1\} \) and \( s^i \not\models G \) for \( i \in \{0, \ldots, n\} \). Otherwise \( \pi \) is safe.

VEA do not consider reach-avoid, thus potentially reporting unsafe paths that contain goal states. Such counterexamples are not relevant in practice. Hence, we refine VEA’s approach to support reach-avoid. Specifically, reach-avoid can be encoded in VEA’s framework by annotating the unsafety condition \( \phi_u \) and the guard \( g \) of each operator \( o \in O \) with the non-goal condition \( \neg G \) – making goal states terminal.

On the algorithmic level, reach-avoid adds another source of complexity to the abstract transition problem, specifically the non-goal disjunction \( \bigvee_i \neg G_i \). Our enhancements introduced for applicability filtering can be applied to simplify this disjunction as well. This pertains in particular to \( \text{ENTAIL-GEN} \), and \( \text{ENTAIL-OP} \) with the adapted test \( \exists s \in [s_p] : s \models G \). If this test fails, then \( G \) is infeasible in \( s_p \).

6 Experiments

We implemented our approach on top of VEA’s C++ code base. The enhancements are largely implemented directly into Marabou, in particular \( \text{OPT-SLACK-VAR} \) and \( \text{ENTAIL-GEN} \), which is a contribution to improve Marabou’s performance on disjunctions in general. All experiments were run on machines with Intel Xenon E5-2650 processors at 2.2 GHz, with time and memory limits of 12 h and 4 GB. Our tool (and all experiments) are publicly available (2024).

Benchmarks. We use VEA’s benchmarks. These are nondeterministic variants of the planning domains BlocksWorld, SlidingTiles and Transport encoded in JANI (Budde et al. 2017). For each domain instance, there are three NN policies trained by VEA using Q-learning (Mnih et al. 2015), each with two hidden layers of size 16, 32 and 64 respectively, and with ReLU activation nodes. There are policies that do, and ones that do not, take move costs into account.

The policies by VEA are trained without applicability filtering. In our evaluation, we verify these same policies with and without applicability filtering, to allow direct comparison of verification performance. As goal condition \( G \) for reach-avoid, we set the goal used by VEA during training. Training episodes stop at \( G \), which exactly matches reach-avoid semantics.

Configurations. We compare a range of algorithmic configurations combining different enhancements for abstract transition computation with applicability filter and reach-avoid as part of VEA’s verification algorithm.

- \( \text{NoOpt} \) disables and \( \text{AllOpt} \) enables all enhancements.
- \( \text{OnlyPerOp} \), \( \text{OnlySlack} \), \( \text{OnlyOp} \) respectively.
- \( \text{OnlyPerOp} \), \( \text{NoSlack} \), \( \text{NoOp} \), \( \text{NoGen} \) enables all enhancements except \( \text{PER-DISJ} \), \( \text{OPT-SLACK-GEN} \) respectively.
- Vea verifies the policy without applicability filtering and without reach-avoid as done by VEA.

With vs. without enhancements. Table 1 shows our results. \( \text{AllOpt} \) clearly dominates \( \text{NoOpt} \). The latter only terminates on the smallest problem instances, with a runtime offset of up to three orders of magnitude.

Ablation study. \( \text{OnlyPerOp} \) covers 10 additional instances compared to \( \text{NoOpt} \). In addition, \( \text{OnlyPerOp} \) always decreases runtime by at least one order of magnitude on instances covered by \( \text{NoOpt} \). This indicates that the choice of encoding (\( \text{PER-DISJ} \) or not) is a crucial factor for efficiency. That said, also the other configurations with a single enhancement, especially \( \text{OnlyGen} \), increase coverage compared to \( \text{NoOpt} \). \( \text{OnlyGen} \) and \( \text{OnlyOp} \) often decrease runtime by at least one order of magnitude. \( \text{OnlySlack} \) is less successful, usually performing on par with \( \text{NoOpt} \). \( \text{AllOpt} \) outperforms every single-enhancement configuration and always covers additional instances. This shows that also the combination of enhancements is crucial.

\( \text{NoPerOp} \) performs competitive on 8-puzzle and smaller BlocksWorld instances, but fails on larger ones similar to \( \text{NoOpt} \). On Transport it performs consistently slower than \( \text{AllOpt} \). Again, this demonstrates the relevance of \( \text{PER-DISJ} \). \( \text{NoOpt} \) tends to be more efficient than \( \text{NoGen} \). This indicates that \( \text{ENTAIL-GEN} \) is more crucial than \( \text{ENTAIL-OP} \). \( \text{NoSlack} \) usually performs on par with \( \text{AllOpt} \). In line with the results for \( \text{OnlySlack} \), this shows that \( \text{OPT-SLACK-GEN} \) is the least crucial enhancement.

While \( \text{AllOpt} \) does never dominate any “all-but-one-enhancement” configuration over all instances, it always dominates in terms of accumulated runtime. This demonstrates that on average enabling all enhancements is more successful.

Comparison to Vea. Clearly, the additional complexity of applicability filtering and reach-avoid in SMT can increase verification time. On BlocksWorld, \( \text{AllOpt} \) is worse than Vea, covering four instances less. On 8-puzzle, on the other hand, \( \text{AllOpt} \) covers three more instances than Vea and is competitive on the remaining ones. This is presumably due to the actual verification results – on NN 32 (cost-ign), the policy is safe without applicability filtering, but is unsafe with applicability filtering. This exemplifies that, without applicability filtering, a policy may be safe due to stalling. This questionable form of safety is no longer possible under applicability filtering. Presumably, the same issue occurs in the 8-puzzle instances not covered by Vea. On BlocksWorld
Table 1: Runtime results in seconds for the evaluated configurations of enhancements for applicability filtering with reach-avoid over different benchmarks and NN policies. (distinguishing cost-aware policies and cost-ignoring policies where applicable).

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<thead>
<tr>
<th>Benchmark NN Safe</th>
<th>NoOpt</th>
<th>OnlyPerOpt</th>
<th>OnlySlack</th>
<th>OnlyOp</th>
<th>OnlyGen</th>
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<th>AllOpts</th>
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<td>27</td>
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Table 1: Runtime results in seconds for the evaluated configurations of enhancements for applicability filtering with reach-avoid over different benchmarks and NN policies. (distinguishing cost-aware policies and cost-ignoring policies where applicable).

- indicates runs that exceed the resource limit of 12h time and 4 GB memory. Vea shows results for verification without applicability-filtering and without reach-avoid.

and Transport, there are no such verification result differences. In particular, on the former many policies are safe with and without applicability filtering.

Unlike applicability filtering, reach-avoid does not affect the safety results for the verified policies. That is, any policy safe under reach-avoid is also safe for Vea. In other words, VEA’s policies are safe “behind” the goal. Furthermore, we remark that verifying reach-avoid adds no significant runtime overhead compared to applicability filtering without reach-avoid, i.e., the increase in complexity compared to Vea is dominated by applicability filtering. We provide additional results (applicability filtering without reach-avoid and reach-avoid without applicability filtering) in the TR.

7 Conclusion

The verification of neural action policies is important. Here we contribute enhancements for PPA with applicability filtering, getting rid of much of the additional complexity suffered by a baseline implementation. We also show how to verify safety for the more practical reach-avoid setting.

Important future directions for PPA include liveness properties, in particular the guarantee that a policy will eventually reach the goal; partial safety verification, continuing CEGAR on instances already proved to be unsafe, in order to identify safe regions of the state space; and the extension to probabilistic and/or continuous-state transition systems. Our enhancements are orthogonal to all these extensions.

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References


Amir, G.; Schapira, M.; and Katz, G. 2021. Towards Scalable Verification of Deep Reinforcement Learning. In For-