

Combined Task and Motion Planning for Mobile Manipulation

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Abstract

We present a hierarchical planning system and its application to robotic manipulation. The novel features of the system are: 1) it finds high-quality kinematic solutions to task-level problems; 2) it takes advantage of subtask-specific irrelevance information, reusing optimal solutions to state-abstracted subproblems across the search space. We briefly describe how the system handles uncertainty during plan execution, and present results on discrete problems as well as pick-and-place tasks for a mobile robot.

1. Introduction

A useful household robot should be able to autonomously move around and manipulate objects in its environment. One such task is to tidy up a room by putting away objects in a set of target regions. In this paper, we assume that the initial state of the world is known (approximately) and consider the resulting decision-making problem. The robot must sequence the various pick-and-place operations, and decide on appropriate base positions, specific target locations for each object, and feasible grasps and corresponding paths through configuration space for its arms. We specifically consider *optimization* problems, where the goal is to find plans that minimize some measure of total cost (e.g., execution time).

Problems like these present a rich set of challenges. Even in simple environments, there are geometric constraints that are difficult to capture symbolically. For example, deciding where to move the base prior to placing a juice bottle on a table requires attention to obstacles on the floor and table, as well as the kinematics of the robot. These problems also have complex combinatorial structure, and are hard for A*-based planners (Helmert and Röger 2008). Finally, even specialized planners for low-level tasks such as arm movement take tens of milliseconds, strongly limiting the number of node expansions that can be performed by a forward search algorithm under real-time constraints.

Traditionally, such problems have been attacked top-down, separating high-level task planning (e.g., sequencing pick-and-place operations) from lower-level planning (e.g., finding feasible paths for the arm). Task planning is simplified by ignoring low-level details, but the resulting plans may be inefficient or even infeasible due to missed lower-level synergies and conflicts. For example, the task planner

might sequence b before a , unaware that a particular way of doing a leaves the robot in an ideal configuration to follow with b , or worse, that every way of doing b renders a infeasible (e.g., by blocking the only feasible grasp for a).

Our first technical contribution is an alternative method, described in Section 3, for encoding robotic manipulation problems as vertically integrated hierarchical task networks (HTNs). At the bottom of the hierarchy, primitive actions (e.g., for arm or base movements) are modeled by calling out to external solvers such as rapidly-exploring random trees (RRTs). Continuous choices (e.g., grasp angles) are made finite via sampling. Sensing and robustness to failures are handled within the primitive actions. Given this encoding, the optimal plan allowed by the hierarchy can be found by exhaustive search. This plan will (with high probability) be a high-quality, guaranteed-feasible kinematic solution.

Our second contribution is the SAHTN algorithm, described in Section 4, which uses *subtask-specific irrelevance* to speed up this search. For example, the best way to move the arm to pick up object 23 depends only on the position of the base, arm, object 23, and nearby objects, and the results of such planning can be reused every time this subproblem occurs in the search space. Empirical results, presented in Section 5, show the effectiveness of the combined system.

2. Related Work

Several recent algorithms integrate information from the task level into a sampling-based motion planning framework. The configuration space can then be viewed as consisting of regions (one per instantiation of the discrete variables), connected by lower-dimensional submanifolds. aSyMov (Gravot, Cambon, and Alami 2003) decomposes the configuration space for manipulation into transit and transfer manifolds, taking advantage of stability constraints for free objects. Hauser and Latombe (2009) use a geometrically motivated heuristic function to focus sampling on those subtasks that are likely to be feasible. HYDICE (Plaku, Kavraki, and Vardi 2009), a hybrid system verification tool, also uses a heuristic estimate of the likely feasibility of each subproblem to focus sampling. Our algorithm differs from these in its focus on optimization, and its use of relevance information (aSyMov does this to some degree by reusing roadmaps). An advantage of the above methods is that they interleave sampling between motion planning subproblems.

Hierarchical planning also has a long history in the

discrete planning literature, and hierarchical task network (HTN) planners such as SHOP2 (Nau et al. 2003) have been widely used in practice. The rich geometry of robotic configuration spaces seems difficult to express using standard discrete representations alone, though, and so these methods have tended to stay above the motion planning level. Moreover, little work has been done on optimization for HTNs.

Abstracting a problem using a subset of state variables has also been considered by many researchers. Most work we are familiar with in the planning literature uses abstraction to create a simpler approximation to the problem, whose solution is then expanded (Sacerdoti 1973) or used as a heuristic (Culberson and Schaeffer 1996; Holte, Grajkowski, and Tanner 2005; Felzenszwalb and McAllester 2007). For the related problem of learning or deriving an optimal policy, prior work in the reinforcement learning literature (Dietterich 2000; Diuk, Strehl, and Littman 2006) uses an exact abstraction to reduce the size of the value function or policy representation. Finally, cognitive architectures such as SOAR (Laird, Newell, and Rosenbloom 1987) use explanation-based learning to avoid deliberating about the same subproblem twice; however, these systems do not do optimal planning, and are not explicitly hierarchical.

3. Pick-and-Place Domain and Hierarchy

We consider a pick-and-place domain for a mobile robot with arm(s), where the environment consists of objects (juice bottles) on various surfaces. The robot’s task is to move all objects to their goal regions, as quickly as possible.

States for this problem consist of a robot joint configuration, along with, for each object, a description of its geometry, current position, and relation to other objects (e.g., *bottle1* on *table1*).

The primitive actions in this domain move a specific part of the robot (base, torso, arm, or gripper) to a target joint configuration. One additional action moves the arm into a grasp configuration given the approximate location of a target object and a grasp angle (this action is represented as primitive because it involves perceptual feedback from the laser scanner, and our planner assumes full observability).

For each primitive action, we require a *transition model* that takes in a state and returns the successor state and action cost (or failure). The complex geometric constraints in the environment make it difficult to use declarative representations such as PDDL directly. Instead, the transition models are procedural, and call out to external planners. For example, `ArmJointAction` is implemented by a sampling-based motion planner (Rusu et al. 2009), using a collision map rendered from the current state. Action costs are set based on the estimated time required. For example, the cost of `ArmJointAction` is the length of the returned path, multiplied by a weighting constant.

In addition to an initial state and transition model, our planning algorithm also takes a *action hierarchy* as input. This hierarchy specifies 1) a finite set of high-level actions (HLAs), including a distinguished top-level action `Act`; and 2) for each HLA and state, a set of immediate refinements into finite sequences of (possibly high-level) actions.

Such a hierarchy both structures and potentially restricts the space of solutions. In particular, rather than searching

directly over primitive action sequences, an agent can begin with a plan consisting of just `Act`, and repeatedly replace the first non-primitive action in this plan with an immediate refinement until a primitive solution is found. We assume WLOG that the hierarchy does not generate primitive non-solutions. This can always be achieved, e.g., by ending each plan with a `Goal` HLA that has zero refinements from non-goal states and an empty refinement from goal states.

Concretely, we use the following hierarchy. `Act` has recursive refinements `MoveToGoal(o)`, `Act` ranging over all objects o that are not yet in their goal positions, or just the empty refinement if this set is empty. `MoveToGoal(o)` refines in turn to `GoPick(o)`, `GoPlace(o, p)`, ranging over positions p in the goal region of o . Both of these HLAs refine to `ArmTuck`, `BaseRgn(r)` if needed (where r is a region around the target), followed by `Pick(o)` or `Place(o, p)`. `Pick` and `Place` further refine to choose a grasp/drop angle, and then generate the appropriate sequence of arm, torso, and gripper primitives to effect the appropriate pick or place operation.

As with the primitive transition models, we allow the set of refinements of an HLA to be generated by arbitrary code. This allows, e.g., `GoPick` to compute a candidate base region for the grasp, and `Place` to use inverse kinematics to generate valid arm joint configurations for the drop. One complication that arises in hybrid domains is that the set of refinements of a high level action may be (uncountably) infinite. For example, the `BaseRgn(r)` action has one refinement `BaseAction(p)` for each point p in region r . We make the search space finite by having each such HLA generate a random sample of pre-specified size from its infinite set of refinements. The same random bits are used across invocations of an HLA, which produces a “graphy” reachable state space that provides more opportunities for caching. For instance, each time we consider `Place`ing a particular object we will generate the same candidate target positions.

Note that hierarchical constraints may rule out all optimal solutions; for instance, our hierarchy does not allow putting an object down in an intermediate location. A plan is called *hierarchically optimal* if has minimal cost among all plans generated by the hierarchy. Moreover, let N be the minimum number of samples used when discretizing the refinements of an HLA (or calling a sampling-based primitive planner). A planning algorithm is *hierarchically resolution-optimal* if, as $N \rightarrow \infty$, the cost of the returned plan converges almost surely to the hierarchically optimal cost. Finally, define the *reachable state space* under a hierarchy as the set of all states visited by any primitive refinement of `Act`. In this paper, we assume that the reachable state space is always finite, and restrict our attention to hierarchically (resolution-) optimal planning algorithms.

4. SAHTN Algorithm

This section presents the State-Abstracted Hierarchical Task Network (SAHTN) algorithm. It takes in a domain description, action hierarchy, and a `RELEVANT-VARS` function specifying which state variables matter for doing an action from some state. The output is a hierarchically optimal solution.

As a stepping stone towards describing SAHTN, we first present a simple exhaustive, hierarchically optimal HTN al-

Algorithm 1 : Optimal HTN algorithm for acyclic problems

/* s is a state, a is an action, p is a plan (action sequence), and
* c is its corresponding cost. The MERGE function merges maps,
* retaining the minimum-cost entry for each reachable state. */

```
function SOLVE( $s$ )  
  return the plan associated with the min-cost state  
    in RESULTS-A( $s, \text{Act}$ ), or failure if empty  
  
function RESULTS-A( $s, a$ )  
  if  $a$  is high-level then  
    return MERGE({RESULTS-P( $s, ref$ ) |  
       $ref \in \text{REFINEMENTS}(a, s)$ })  
  else if  $\neg \text{APPLICABLE}(s, a)$  then return { }  
  else return {SUCCESSOR( $s, a$ ) : [COST( $s, a$ ), [ $a$ ]]}  
  
function RESULTS-P( $s, p$ )  
   $output \leftarrow \{s : [0, [ ]]\}$   
  for each  $a'$  in  $p$  do  
     $output \leftarrow \text{MERGE}(\{\text{BOOKKEEP-A}(s', a', c', p') \mid$   
       $s' : [c', p'] \in output\})$   
  
  return  $output$   
  
function BOOKKEEP-A( $s, a, c, p$ )  
   $output \leftarrow \{ \}$   
  for each  $s' : [c', p'] \in \text{RESULTS-A}(s, a)$  do  
     $output[s'] \leftarrow [c + c', p + p']$   
  
  return  $output$ 
```

Algorithm 2 : Changes to Algorithm 1 for SAHTN algorithm

```
function BOOKKEEP-A( $s, a, c, p$ )  
   $relevant \leftarrow \text{RELEVANT-VARS}(s, a)$   
  if  $cache$  has no entry for [ $s_{relevant}, a$ ] then  
     $cache[s_{relevant}, a] \leftarrow \text{RESULTS-A}(s, a)$   
   $output \leftarrow \{ \}$   
  for each  $s' : [c', p'] \in cache[s_{relevant}, a]$  do  
     $output[s_{relevant} + s'_{relevant}] \leftarrow [c + c', p + p']$   
  
  return  $output$ 
```

gorithm (see Figure 1). The top-level SOLVE function takes an initial state, and returns a hierarchically optimal solution (or *failure*). RESULTS-A and RESULTS-P take an initial state and action or plan, and return a map from each state reachable by (some refinement of) the given action or plan to a tuple containing an optimal primitive refinement that reaches this state and its cost (cf. the exact valuations of Marthi, Russell, and Wolfe (2008)). In particular, RESULTS-A returns the single outcome state for a primitive action, or the best cost and plan to each reachable state (over all refinements) for a high-level action. RESULTS-P computes the result for an action sequence by progressing through each action in turn. Finally, BOOKKEEP-A simply calls RESULTS-A, with some extra bookkeeping to sum optimal costs and concatenate optimal plans along action sequences.

SAHTN (see Algorithm 2) makes this into a dynamic programming algorithm by adding state-abstracted caching to the BOOKKEEP-A function. We assume a global *cache* of the results of each call to RESULTS-A(s, a), keyed by a and the values of state variables in s that are *relevant* to a from s . Then, in a later call to RESULTS-A(s', a) where s' has the same relevant variable values as s , we simply look up the cached result and combine it with the irrelevant variables of s' to produce the output mapping. For this output to be correct, it is crucial that RELEVANT-VARS(s, a) truly captures

all aspects of state s that are relevant to doing action a :

Definition 1. A state variable v is *relevant* to action a from state s , iff (1) the set of primitive refinements of a from s depends on v , or (2) any primitive refinement of a from s conditions on, sets, or has cost dependent on the value of v .

For example, the only variables relevant to BaseAction(p) are the the current base position, and the positions of objects that are potential obstacles.¹

Before stating the correctness of SAHTN, there is one more issue that must be made concrete. As described, the algorithm will loop forever in *cyclic* hierarchies; we first define this condition, and later discuss how it can be relaxed.

Definition 2. Call pair (s', a') a *subproblem* of (s, a) iff there exists a refinement r of a from s and integer i s.t. $s' = \text{SUCCESSOR}(s, r_{1:i-1})$ and $a' = r_i$. A hierarchy is *cyclic* from initial state s iff there exists any subproblem of (s, Act) that has itself as a subproblem.

Equivalently, a hierarchy is cyclic if SAHTN ever recursively calls RESULTS-A(s, a) when RESULTS-A(s, a) is already on the call stack. Note that an acyclic hierarchy may include recursive HLAs. For instance, while the Act HLA for our pick-and-place domain is recursive, the hierarchy is *not* cyclic because in every recursive application of Act, one more object will have been placed in its goal position.

Theorem 1. Given an acyclic hierarchy, correct RELEVANT-VARS function, and finite reachable state space, SAHTN will always return a hierarchically optimal solution.²

The acyclic requirement can rule out some natural hierarchies. For instance, consider a Nav(x, y) HLA in a grid-world domain, which refines to the empty sequence iff at (x, y) , and otherwise to a primitive move action followed by a recursive Nav(x, y). In this case, the refinement Left, Right, Nav(x, y) leads to a cycle in the above sense. Fortunately, a simple change to SAHTN can extend Theorem 1 to such cases. The basic idea is to add a case to RESULTS-A: if (s, a) potentially leads to a cycle, instead of recursively decomposing run Dijkstra's algorithm locally over the space of potential cycles, switching back to recursive computation for (s', a') pairs that can not cycle back to (s, a) .²

5. Results

We now present comparisons of SAHTN with three other search algorithms. Uniform-cost search (UCS) searches forward from the initial state, without using a hierarchy. Hierarchical UCS (H-UCS) searches in a space where each node consists of the state arising from the primitive prefix of a plan, together with the remaining actions in the plan. N-SAHTN is the SAHTN algorithm with no state abstraction.

We first present results on a version of the *taxi domain*, a benchmark commonly used in the reinforcement learning literature (Dietterich 2000). Taxi problems consist of a taxi

¹With appropriate changes to the algorithm, more general notions of relevance can be considered as well. For instance, in a multi-robot problem one could share results between MoveToGoal($robot1, o$) and MoveToGoal($robot2, o$) for interchangeable robots with identical starting configurations.

²Proof and other supplemental materials are available at www.ros.org/wiki/Papers/ICAPS2010_Wolfe

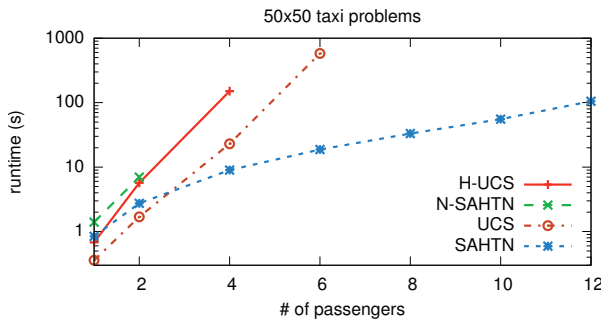


Figure 1: Runtimes for algorithms on 50x50 taxi problems, as a function of the number of passengers. Larger problems were not solvable by any algorithm but SAHTN within 512MB of memory.

in a grid world, and passengers with randomly chosen source and destination squares. The taxi must pick up and drop off the passengers, one at a time. On such problems (see Figure 1), SAHTN (with the Dijkstra modification mentioned above) clearly scales much better than other algorithms as the number of passengers increases, due to decoupling of navigation decisions from high-level sequencing of passengers. All algorithms are primitive-optimal in this domain.

We next evaluated our algorithms on the full pick-and-place domain, using a prototype PR2 robot constructed by Willow Garage, Inc (Wyrobek et al. 2008). The robot has a wheeled base and two 7-dof arms (including 1-dof gripper). Figure 2 shows results on single-arm pick-and-place tasks with two tables and randomly placed objects and goal regions, for increasing numbers of objects. There is no obvious way to apply uniform-cost search to these problems, so we compare the three other algorithms (all of which take advantage of our hierarchical problem formulation), using the same sampling settings. We again see significant improvement in runtime from state abstraction in SAHTN, increasing as the number of objects grows. SAHTN’s performance is initially dominated by the polynomially many primitive action applications it must make, although eventually the exponential cost of the top-level traveling salesman problem will take over.

We also implemented, for each primitive action, a function to execute it on the PR2. The execution primitives were responsible for implementing perceptual feedback and returning a success flag, which was used to implement a simple executive that retried failed actions. A video of the PR2 executing a 4-object plan is available online.²

6. Conclusion

We view this work as a proof-of-concept that task-level planning can be successfully extended all the way to the kinematic level, to generate robust and high-quality plans. To help reduce computation times for larger tasks, future work will examine extensions of SAHTN that can use available heuristic information, and perhaps approximate models for the HLAs and primitives (Marthi, Russell, and Wolfe 2008), to guide search and reduce calls to external solvers. Another important improvement will be incremental, adaptive search algorithms that better manage the tradeoff between computational cost and plan quality.

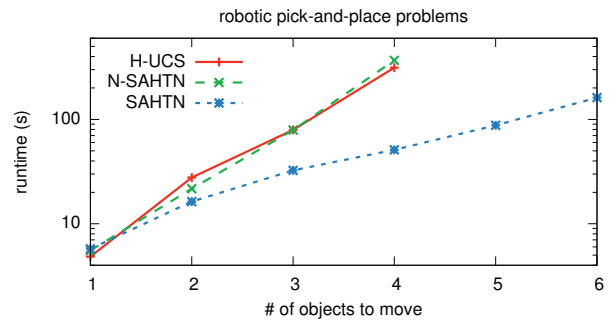


Figure 2: Runtimes (averaged over three runs) for three algorithms on pick-and-place tasks, as a function of the number of objects to be moved. Larger problems were not solvable by any algorithm except SAHTN within 10 min. Two runs where unlucky sampling led to no solutions being found were discarded and rerun.

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