

Rethinking Cancer Gene Identification Through Graph Anomaly Analysis

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Abstract

Graph neural networks (GNNs) have shown promise in integrating protein–protein interaction (PPI) networks for identifying cancer genes in recent studies. However, due to the insufficient modeling of the biological information in PPI networks, more faithfully depiction of complex protein interaction patterns for cancer genes within the graph structure remains largely unexplored. This study takes a pioneering step toward bridging biological anomalies in protein interactions caused by cancer genes to statistical graph anomaly. We find a unique graph anomaly exhibited by cancer genes, namely weight heterogeneity, which manifests as significantly higher variance in edge weights of cancer gene nodes within the graph. Additionally, from the spectral perspective, we demonstrate that the weight heterogeneity could lead to the “flattening out” of spectral energy, with a concentration towards the extremes of the spectrum. Building on these insights, we propose the Hierarchical-Perspective Graph Neural Network (HIPGNN) that not only determines spectral energy distribution variations on the spectral perspective, but also perceives detailed protein interaction context on the spatial perspective. Extensive experiments are conducted on two reprocessed datasets STRINGdb and CPDB, and the experimental results demonstrate the superiority of HIPGNN.

Code and Data — <https://github.com/zy1199710/HIPGNN>

Extended version — <https://arxiv.org/abs/2412.17240>

Introduction

Identifying cancer genes is a crucial endeavor in both research and clinical practice (Beroukhi et al. 2010; Martínez-Jiménez et al. 2020; Bailey et al. 2018). Cancer genes are closely related with protein interactions (Leiserson et al.

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2015), motivating solutions that integrate the protein–protein interaction (PPI) network for efficient identification (Yang et al. 2021; Levi, Elkon, and Shamir 2021; Chitra, Park, and Raphael 2022; Yang et al. 2023; Wang et al. 2024, 2023). Such approaches exploit, for example, multi-omics data and protein interaction information to extract and derive features that distinguish cancer genes.

The aggregation capabilities of graph neural networks (GNNs) (Wu et al. 2020) have led to notable success in methods for cancer gene identification, based on graph convolutional networks (Schulte-Sasse et al. 2021), Chebyshev graph convolutional works (Peng et al. 2022) and masked graph autoencoders (Cui et al. 2023). However, these methods only use the PPI network to update the node features by referring to neighbor representations, which do not model the complete biological information within the network. Therefore there exists a gap: more faithfully depicting complex protein interaction patterns within the graph structure.

Our motivation is as follows: cancer genes induce significant biological anomalies in protein interactions, such as mutations, changes in expression levels, or alterations in protein modifications, as illustrated in Figure 1 (a). These biological anomalies can be interpreted as graph anomalies in the PPI network, as shown in Figure 1 (b). By identifying and analyzing these graph anomalies, we aim to develop a more comprehensive understanding of cancer gene behavior on PPI networks for cancer gene identification.

Based on this vision, our statistical experiments in this paper reveal a distinctive graph anomaly of cancer in the PPI network, which we term *weight heterogeneity*. As shown in Figure 1 (c), we compute the variance distribution of all edge weights (protein interaction confidence) for each node in a widely used PPI dataset, STRINGdb. It reveals that cancer genes exhibit greater weight variance compared to non-cancer genes.

Additionally, from the spectral perspective, we demonstrate that weight heterogeneity leads to the “flattening out”

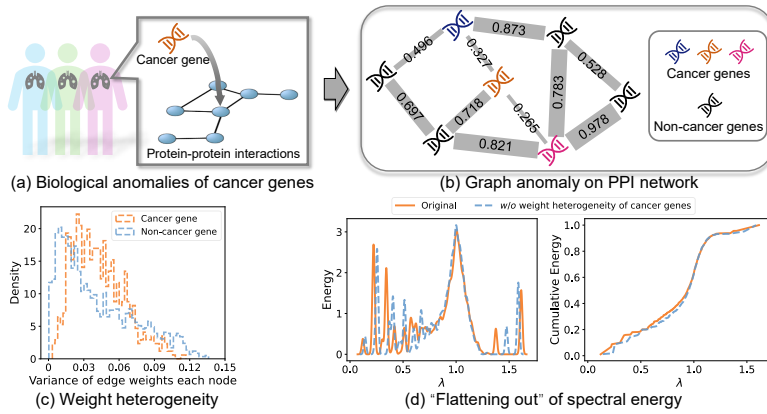


Figure 1: Overview of our motivation. (a) Cancer genes induce significant biological anomalies in protein interactions. (b) We interpret these anomalies as graph anomaly in the PPI network. (c) Then, we calculate the variance distribution of the edge weights for each gene and investigate the weight heterogeneity of cancer genes from the spatial perspective. (d) Furthermore, we compute and compare the spectral energy distribution with and without weight heterogeneity in cancer nodes and explore the “flattening out” of spectral energy from the spectral perspective. We remove the weight heterogeneity of all cancer gene nodes by setting their edge weights to 0.5.

of the spectral energy, theoretically and experimentally. Figure 1 (d) illustrates the spectral energy distribution with and without weight heterogeneity in cancer nodes using the graph Fourier transform of node attributes. The spectral energy of the original graph (with weight heterogeneity) tends to concentrate more towards the extremes of the spectrum. We describe this phenomenon as the “flattening out” of spectral energy and provide rigorous proof through theoretical analysis. To further illustrate this phenomenon, we also validate it on two synthetic graphs. Based on the above observations, we recognize that both spatial and spectral perspectives offer information about graph anomaly of cancer. This motivates us to design a cancer gene identification model that integrates both perspectives.

Therefore, we propose an innovative Hierarchical-Perspective Graph Neural Network, termed HIPGNN, to identify cancer genes on the PPI network. HIPGNN can not only discern spectral energy distribution variations to tackle the “flattening out” on the spectral perspective, but also perceive detailed protein interaction context for handling weight heterogeneity on the spatial perspective. Specifically, after obtaining the Laplace matrix eigenvalues, we encode the position and proximity of the eigenvalues to integrate the spectral energy distribution information. Following this, we design the proximity-aware spectral graph representation using spectral eigenvalue encoding to update node representations. Finally, we decode the spatial context for node representation by perceiving protein interaction information.

Building on previous works (Schulte-Sasse et al. 2021; Cui et al. 2023), we reprocessed two datasets, STRINGdb and CPDB, which contain real-world PPIs and cancer gene data, to extract more comprehensive protein interaction information. Extensive experiments on these datasets demonstrate the superior performance of the proposed HIPGNN compared to state-of-the-art methods.

Preliminaries

Theoretical Analysis

we first provide several necessary definitions and notation.

Weighted graph We define a weighted graph as $\mathcal{G}_w = \{\mathcal{V}, \mathcal{E}, \mathcal{W}, \mathcal{X}, \mathcal{Y}\}$, where $v_i \in \mathcal{V}$ represents the node and $N = |\mathcal{V}|$. The node features and labels are denoted as $x_i \in \mathcal{X}$ and $y_i \in \mathcal{Y}$, respectively. The edge $e_{ij} \in \mathcal{E}$ connects nodes v_i and v_j , and $w_{ij} \in \mathcal{W}$ is the edge weight of e_{ij} . Let A be the corresponding adjacency matrix, where $A_{ij} = w_{ij}$ if there exists a weighted edge. It is worth mentioning that all graphs studied in this paper are undirected graphs, i.e., $A_{ij} = A_{ji}$.

Unweighted graph An unweighted graph $\mathcal{G}_{uw} = \{\mathcal{V}, \mathcal{E}, \mathcal{X}, \mathcal{Y}\}$ is defined similarly to a weighted graph, except that in its adjacency matrix A , $A_{ij} = 1$ if there exists an edge.

Given the weight heterogeneity exhibited by cancer genes on the PPI network, we model this phenomenon using a random weighted graph (Khorunzhy, Shcherbina, and Vengerovsky 2004; Ding and Jiang 2010). Specifically, for an unweighted graph \mathcal{G} , we define a set of variables $\{w_{ij}; 1 \leq i < j \leq N\}$ that are independently and identically Gaussian distributed, while assigning the same weight to the symmetric edge weights, making \mathcal{G} a weighted graph. For all i, j , $w_{ij} = w_{ji}$, $\mathbb{E}(w_{ij}) = \mu$, and $\text{Var}(w_{ij}) = \sigma^2$. Based on this, we use σ^2 to measure the degree of weight heterogeneity. Holding μ constant, we argue that the larger the σ^2 , the higher the weight heterogeneity on the graph.

On the weighted graph \mathcal{G} , let D be the diagonal degree matrix. The Laplacian matrix L is defined $L = D - A$ (regular) or $L = I - D^{-1/2}AD^{-1/2}$ (normalized), where I is the identity matrix. L is a symmetric matrix with eigenvalues $0 = \lambda_1 \leq \lambda_2 \leq \dots \leq \lambda_N$ and a corresponding orthonormal basis of eigenvectors $U = (u_1, u_2, \dots, u_N)$. Assume that $x = (x_1, x_2, \dots, x_N)$ is a random signal whose graph

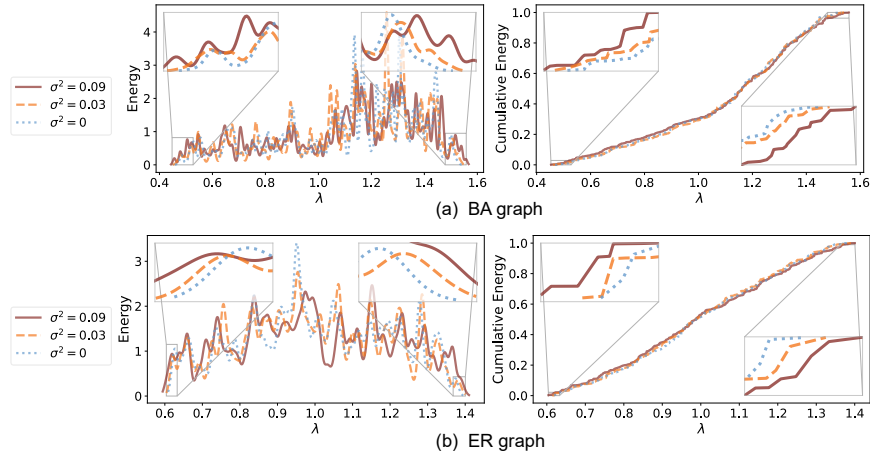


Figure 2: The distributions of spectral energy and cumulative energy on two synthetic graphs: Barabasi–Albert (BA) graph and Erdős–Rényi (ER) graph. We measure the effect of weight heterogeneity with different weight variances σ^2 . Red solid line means $\sigma^2 = 0.09$, orange dashed line means $\sigma^2 = 0.03$, and blue dotted line means $\sigma^2 = 0$.

Fourier transform is $\hat{x} = U^T x = (\hat{x}_1, \hat{x}_2, \dots, \hat{x}_N)$. The spectral energy distribution at λ_k is denoted as $f_k(x, L) = \hat{x}_k^2 / \sum_{i=1}^N \hat{x}_i^2$. We summarize the following finding from the theory: **The weight heterogeneity observed among cancer genes results in “flattening out” of spectral energy, which means that spectral energy is elevated at extremes and lowered in the middle.**

To verify the finding theoretically, we first provide some definitions of the spectral energy distribution:

Definition 1. Expectation of spectral energy. For $\lambda \in \lambda_1, \lambda_2, \dots, \lambda_N$, we define the expectation of the spectral energy on λ as:

$$\mathbb{E}_\lambda(f(x, L)) = \frac{\sum_{k=1}^N \lambda_k \hat{x}_k^2}{\sum_{k=1}^N \hat{x}_k^2}.$$

And Definition 1 can also be converted into the form of Rayleigh quotient (Dong, Zhang, and Wang 2023; Gao et al. 2023):

$$\mathbb{E}_\lambda(f(x, L)) = \frac{\sum_{k=1}^N \lambda_k \hat{x}_k^2}{\sum_{k=1}^N \hat{x}_k^2} = \frac{x^T L x}{x^T x} \quad (1)$$

$$= \frac{1}{2} \frac{\sum_{i,j=1}^N (x_i - x_j)^2 w_{ij}}{\sum_{i=1}^N x_i^2}. \quad (2)$$

Equation (2) bridges the energy distribution in the spectral domain with the smoothness of the signal on the graph structure in the spatial domain. It can be seen that if the signal is less smooth, the spectral energy moves to higher points. Further, we define the variance of the spectral energy distribution.

Definition 2. Variance of spectral energy. For $\lambda \in \lambda_1, \lambda_2, \dots, \lambda_N$, The variance of spectral energy on λ is defined as:

$$\text{Var}_\lambda(f(x, L)) = \frac{\sum_{k=1}^N \lambda_k^2 \hat{x}_k^2}{\sum_{k=1}^N \hat{x}_k^2} - \left(\frac{\sum_{k=1}^N \lambda_k \hat{x}_k^2}{\sum_{k=1}^N \hat{x}_k^2} \right)^2.$$

A larger variance indicates that the spectral energy disperses more to both sides of the spectrum. Up to this point,

we will now state how the weight heterogeneity on the graph structure affects the variance of spectral energy.

Proposition 3. Give $L = D - A$ and $\{w_{ij} \sim \mathcal{N}(\mu, \sigma^2), w_{ij} = w_{ji}; 1 \leq i < j \leq N\}$, the expectation of variance of spectral energy with respect to w , $\mathbb{E}_w(\text{Var}_\lambda(f(x, L)))$, monotonically increases with the variance of edge weights σ^2 .

The details of the proof process we put in the technical appendix. Proposition 3 illustrates that a larger variance in the edge weights (weight heterogeneity) on the graph leads to a broader dispersion (“flattening out”) of the spectral energy. Intuitively, disrupting edge weights affects functional connectivity metrics such as effective resistance (Ghosh, Boyd, and Saberi 2008), which in turn affects the upper and lower bounds of spectral energy distribution (Barooh and Hespanha 2006).

Validation on Synthetic Graphs

To illustrate our theoretical findings more intuitively, we investigate the “flattening out” of spectral energy on Barabasi–Albert (BA) (Albert and Barabási 2002) and Erdős–Rényi (ER) (Erdős et al. 2012) graphs, each with 500 nodes. The BA graph models real-world network properties, while the ER graph has a uniform degree distribution.

To add weight heterogeneity to original graphs, we assign Gaussian independently distributed weights $w_{ij} \sim \mathcal{N}(\mu, \sigma^2)$ to all edges, with $w_{ij} = w_{ji}$. The σ^2 is set to 0.09, 0.03, and 0 (unweighted graph). Given that even with the largest variance, there is only a probability of less than 0.001% for a weight to fall outside the range of $[0, 2]$, we confine the weight values to this interval to ensure realistic weight values. The graph signal is uniformly distributed between 0 and 1.

As shown in Figure 2, we compute and plot the spectral energy distribution (KDE) and the spectral cumulative energy $\eta_k(x, L) = \sum_{i=1}^k \hat{x}_i^2 / \sum_{i=1}^N \hat{x}_i^2$ on the two synthetic graphs. For clarity, we omit the small energy at $\lambda_1 = 0$ and provide a magnified view of the spectrum’s extremes.

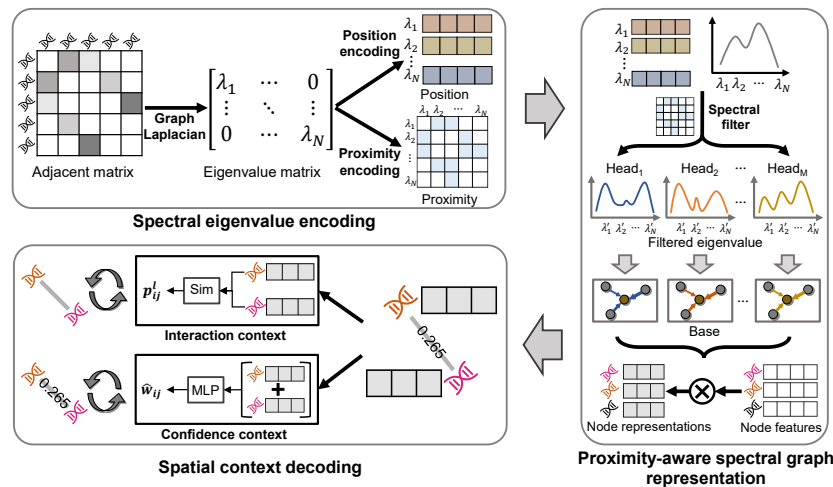


Figure 3: The overview of the HIPGNN framework. It comprises three modules: the spectral eigenvalue encoding to encode the position and proximity of eigenvalues; the proximity-aware spectral graph representation to fuse eigenvalue position and proximity encoding with spectral filters and get the node representation; the spatial context decoding for perceiving protein interaction information.

A clear “flattening out” of spectral energy is observed on both graphs. We summarize the following observations: (1) For the spectral energy distribution, a larger σ^2 causes the spectral energy to deviate from the middle and to have lower wave peaks, with a regular arrangement according to σ^2 size at both ends of the spectrum. (2) For the spectral cumulative energy distribution, an increase in σ^2 leads to elevated energy in the low-frequency range and reduced energy in the high-frequency range. These trends are particularly pronounced at both ends of the spectrum. Overall, these observations empirically substantiate the Proposition 3 and provide intuitive insights into the effects of varying σ^2 on spectral energy distribution.

Problem Formulation

So far, we have formulated the PPI network-based cancer gene identification problem. Existing methods (Schulte-Sasse et al. 2021; Peng et al. 2022; Cui et al. 2023) treat protein interactions above a certain confidence threshold as unweighted edges, constructing an unweighted graph. In contrast, we use confidence as edge weights to construct a weighted graph, capturing variations in confidence levels and their correlation with cancer genes in the PPI network.

PPI network based cancer gene identification This task is regarded as a semi-supervised node classification task. Given a weighted graph \mathcal{G}_w based on a PPI network and some nodes with known labels, our goal is to infer the labels of the remaining nodes, determining whether they are cancer genes.

Method

Based on the analysis in Preliminaries, cancer genes exhibit a unique graph anomaly, i.e. weight heterogeneity, in the PPI network and show a “flattening out” phenomenon in the spectral energy distribution. To address the anomaly from

both spectral and spatial perspectives simultaneously, we introduce a hierarchical-perspective graph neural network, termed HIPGNN, for cancer gene identification as shown in Figure 3.

Spectral Eigenvalue Encoding

Most polynomial filter-based spectral GNNs (Defferrard, Bresson, and Vandergheynst 2016; He, Wei, and Wen 2022; He et al. 2021; Wang and Zhang 2022) use a fixed polynomial basis for all eigenvalues to approximate arbitrary filters. Nevertheless, these scalar eigenvalue computation methods fall short of expressive capability and cannot capture the “flattening out” of the spectral energy well. To tackle this issue, we intend to design a more powerful eigenvalue encoding rule to directly reflect the distribution of eigenvalues, such as the spectral gap (Hoffman, Kahle, and Paquette 2021).

Eigenvalue position encoding Given a normalized Laplace matrix $L = U\Lambda U^T$ of a weighted graph \mathcal{G}_w , we encode each eigenvalue of the matrix $\lambda \in \lambda_1 \leq \lambda_2 \leq \dots \leq \lambda_N$ from a scalar to a meaningful vector: $\mathbb{R}^1 \rightarrow \mathbb{R}^d$, by using a position encoding function as follows:

$$\begin{aligned} \rho_{2i}(\lambda) &= \sin(100\lambda/10000^{2i/d}), \\ \rho_{2i+1}(\lambda) &= \cos(100\lambda/10000^{2i/d}), \end{aligned} \quad (3)$$

where i is an integer and its value domain ranges from 0 to $d/2 - 1$. This function forms a multiscale representation of the eigenvalues and has the advantage of filtering arbitrary multivariate continuous functions(Bo et al. 2022).

Eigenvalue proximity encoding Furthermore, to intuitively perceive the spectral energy distribution, we propose to encode the proximity between eigenvalues. A proximity matrix is computed by eigenvalue position encodings: $\mathbb{R}^{N \times d} \rightarrow \mathbb{R}^{N \times N}$. Each element of this matrix obtained is as

follows:

$$R_{ij} = \rho(\lambda_i)^T \rho(\lambda_j), \quad (4)$$

where there exist the following two theoretical properties of R_{ij} that can be proved.

Proposition 4. *The proximity between λ_i to λ_j , R_{ij} , is determined by $\lambda_i - \lambda_j$.*

Proposition 5. *The R_{ij} is undirected.*

The two propositions (proof in the technical appendix) illustrate that proximity matrix R_{ij} can effectively capture and represent the spectral energy distribution variations, which further enables the GNN to process the spectral energy ‘‘flattening out’’.

Proximity-aware Spectral Graph representation

After generating the valuable eigenvalue encoding, we utilize it in the spectral graph representation. Then we propose a Transformer-based (Vaswani et al. 2017) proximity-aware spectral graph representation to fuse eigenvalue position and proximity encoding with spectral filters and get the node representation.

Proximity-aware spectral filter Unlike using a regular transformer to design spectral filters (Bo et al. 2022), we introduce the eigenvalue proximity information to the attention computation process for designing trainable spectral filters. Given the initial representation which concatenates eigenvalues with their encodings: $Z = [\lambda_1 \| p(\lambda_1), \dots, \lambda_n \| p(\lambda_n)]^T \in \mathbb{R}^{N \times (d+1)}$, an innovative attention computation function is proposed as follows:

$$Q = ZW_m^Q, \quad K = ZW_m^K, \quad V = ZW_m^V, \\ Z'_m = \text{Attention}(Q, K, V) = \text{Softmax}\left(\frac{QK^T + R}{\sqrt{d_q}}\right)V, \quad (5)$$

where d_q is the dimension of each head, and m represent the m -th head. We include the proximity matrix R as part of attention for learning the global distribution of eigenvalues. Afterward, the representation Z'_m of each head is used as a spectral filter to compute new eigenvalues as $\lambda'_m = \phi(Z'_m W_\lambda)$, where $\lambda'_m \in \mathbb{R}^{N \times 1}$ is the m -th eigenvalue vector after the spectral filtering.

Learnable bases After obtaining M vectors of filtered eigenvalues, we use a feed-forward network (FFN) in the standard Transformer layer to create the learnable bases for graph convolution. The reconstruction and concatenating processes can be formulated as follows:

$$S_m = U \text{diag}(\lambda'_m) U^T, \quad \hat{S} = \text{FFN}([I_N \| S_1 \| \dots \| S_M]), \quad (6)$$

where $I_N \in \mathbb{R}^{N \times N}$ denotes the unit matrix.

Graph convolution Eventually, we regard each dimension of the node features as a graph signal and multiply it with the combined Laplace matrix base \hat{S} :

$$\hat{X}_{:,i}^{l-1} = \hat{S}_{:,i} X_{:,i}^{l-1}, \quad X^l = \sigma(\hat{X}^{l-1} W_x^{l-1}) + X^{l-1}, \quad (7)$$

where $\sigma()$ is activation and X^l is the node representation in the l -th layer.

Spatial Context Decoding

Recalling our findings, in addition to the ‘‘flattening out’’ of the spectral energy, we also observe weight heterogeneity within the weighted graph. This indicates that the information about the protein interaction context over the spatial domain is also helpful in distinguishing such anomalies. Motivated by this hypothesis, we decode the protein interaction context to correlate different nodes on graph data. Therefore, after obtaining the node representations, we design the spatial context decoding module to perceive the protein interaction and confidence information in the spatial domain.

Interaction context perception Given node representations X^l , we compute the interaction probability between x_i^l and x_j^l by cosine similarity and then leverage cross entropy to approximate the interactions on the graph:

$$p_{ij}^l = \cos(x_i^l, x_j^l), \\ \mathcal{L}_l = \sum_{(i,j) \in \hat{\mathcal{E}}} (y_{ij}^l \log(p_{ij}^l) + (1 - y_{ij}^l) \log(1 - p_{ij}^l)), \quad (8)$$

where the set $\hat{\mathcal{E}}$ contains the edges \mathcal{E} on the graph and the negatively sampling edges from the original dataset. if (i, j) is negatively sampling edge, $y_{ij}^l = 0$.

Confidence context perception More importantly, the model needs to perceive protein interaction confidence to tackle weight heterogeneity. Given the node representations X^w , the MLP model and MSE are utilized to predict confidence scores between x_i^w and x_j^w as well as to compute losses, respectively:

$$\hat{w}_{ij} = \text{MLP}((x_i^w + x_j^w)/2), \\ \mathcal{L}_w = \sum_{(i,j) \in \hat{\mathcal{E}}_{\text{train}}} \text{MSE}(\hat{w}_{ij}, w_{ij}). \quad (9)$$

In $(i, j) \in \hat{\mathcal{E}}$, if (i, j) is negatively sampling edge, $w_{ij} = 0$.

It is worth mentioning that we set up node representing channels independent of cancer gene identification for the above two perception modules. We use multiple standard transformer models to obtain separate node representations for each channel: X^n , X^l , and X^w .

Cancer gene identification Here, we proceed with the loss function for cancer gene identification. We feed X^n to the MLP with sigmoid function to get the cancer gene node probability p^n . The weighted cross-entropy loss is used to alleviate the challenge from label imbalance as follows:

$$\mathcal{L}_n = \sum_{i \in \mathcal{V}_{\text{train}}} (\gamma y_i \log p_i^n + (1 - y_i) \log(1 - p_i^n)), \quad (10)$$

where $\mathcal{V}_{\text{train}}$ is the training set of nodes \mathcal{V} , and γ is the ratio of cancer gene nodes ($y_i = 1$) to non-cancer gene nodes ($y_i = 0$) in the training set. At last, we sum all the losses with weights to get the total loss: $\mathcal{L} = \alpha \mathcal{L}_n + \beta \mathcal{L}_l + \gamma \mathcal{L}_w$.

Complexity Analysis

Considering the large size of the graph, we intend to use only a few important eigenvalues as inputs to the model in

Graph	Method	STRINGdb						CPDB					
		20%			80%			20%			80%		
		AUC	F1	AP	AUC	F1	AP	AUC	F1	AP	AUC	F1	AP
Unweighted	GCN	81.68	72.09	64.16	87.99	77.43	75.61	81.84	73.54	67.55	82.48	73.67	69.16
	GAT	81.67	71.62	58.88	85.25	73.35	68.52	80.16	70.66	61.02	84.50	76.26	68.70
	GraphSAGE	84.37	73.75	65.48	87.09	78.98	72.13	78.02	69.32	62.99	85.96	78.36	76.31
	Chebnet	83.35	73.20	66.47	86.44	78.33	73.39	75.70	66.77	59.29	82.00	71.72	68.32
	EMOGI	79.06	64.27	59.74	86.88	70.18	73.22	80.84	67.10	66.94	80.84	68.25	64.00
	MTGCN	84.30	73.97	66.82	86.90	76.05	73.89	77.25	69.62	60.95	83.71	68.84	70.22
	SMG	89.81	78.62	75.69	90.80	79.74	77.43	84.75	72.34	70.83	86.57	77.77	77.83
HIPGNN	89.08	78.17	75.56	90.81	81.71	79.66	87.99	79.13	78.07	87.80	79.87	77.40	
Weighted	GCN	81.65	72.46	63.91	87.17	76.25	74.22	81.79	73.91	67.04	82.97	73.70	68.93
	GAT	77.99	69.93	54.49	85.85	74.50	72.67	74.48	42.19	57.71	85.51	75.69	68.55
	Chebnet	83.64	73.91	66.58	87.17	78.03	74.72	76.00	66.32	59.81	83.35	74.34	69.82
	HIPGNN	88.39	79.60	76.13	91.18	83.33	81.21	87.88	79.38	78.13	89.66	80.91	79.71

Table 1: Performance on the two datasets under different percentages of the training data. (%)

order to greatly reduce the computational complexity. By analyzing the spectral energy distribution, we believe that the eigenvalues at both extremes are more effective in encoding the “flattening out” of the spectral energy.

Therefore, we introduce a hyperparameter q to adjust for only considering the first q small and the last q large eigenvalues. Ultimately, the complexity of HIPGNN is $\mathcal{O}(2q^2d_1 + 2q^2M + Nd_1L + Nd_1^2 + N^2d_2 + 2E^2d_2 + Nd_2^2 + 2Ed_2^2)$, where N and E are the nodes and edges of the weighted graph, M and L denote the number of filters and layers, and d_1 and d_2 represent the hidden dimensions of graph layer and node representation.

Experiments

Experimental Setup

Datasets Based on previous works (Schulte-Sasse et al. 2021; Cui et al. 2023), we extract richer protein interaction information on two widely used PPI datasets with confidence (Szklarczyk et al. 2021; Kamburov et al. 2009), and integrate cancer gene data to construct two datasets. We name these two datasets directly after the PPI databases: STRINGdb and CPDB. Unlike previous works that used fixed threshold confidence to construct unweighted graphs, HIPGNN directly leverages protein confidence as edge weights to construct weighted graph.

Metrics We choose AUC, F1 (macro), and AP for model performance evaluation. AUC measures the area under the ROC curve, providing a global assessment across all classification thresholds. F1 (macro) is the unweighted average of F1 scores for both categories, suitable for imbalanced datasets. AP is the area under the precision-recall curve, and is considered the most important metric for cancer gene identification (Schulte-Sasse et al. 2021).

Baselines The baseline methods can be categorized into two groups: firstly, general GNN-based models including GCN (Kipf and Welling 2016), GAT (Veličković et al. 2018), GraphSAGE (Hamilton, Ying, and Leskovec 2017), and Chebnet (Defferrard, Bresson, and Vandergheynst 2016); and secondly, state-of-the-art cancer gene identification methods including EMOGI (Schulte-Sasse et al. 2021), MTGCN (Peng et al. 2022) and SMG (Cui et al. 2023). We

also implement GCN, GAT, and Chebnet on weighted graph and HIPGNN on unweighted graph.

Performance Comparison

Table 1 presents the results of HIPGNN and other baseline methods with training ratios of 20% and 80%. From the table, we draw the following conclusions.

Importance of spectral graph representation Only Chebnet and HIPGNN outperform on weighted graphs compared to unweighted ones, highlighting that edge weights can negatively impact models like GCN, which function as low-pass filters. This demonstrates the effectiveness of appropriate spectral filters in addressing weight heterogeneity.

Importance of spatial context HIPGNN shows a significant performance boost at a 20% training ratio, particularly on the CPDB dataset, outperforming SMG by 7.30% in AP. This indicates that spatial context in protein interactions aids in identifying unknown cancer genes, especially when labels are sparse.

Superiority of HIPGNN HIPGNN consistently outperforms other models across most metrics, effectively handling weight heterogeneity to distinguish cancer genes. Notably, HIPGNN improves AP by 0.44% on STRINGdb and 7.30% on CPDB at a 20% training ratio, and by 3.78% on STRINGdb and 1.88% on CPDB at an 80% training ratio, compared to SMG.

Due to space constraints, subsequent experiments focus on the STRINGdb dataset, with CPDB results provided in the technical appendix.

Ablation Analysis

Proximity-aware spectral graph representation We examine the impact of the spectral graph representation module with spectral eigenvalue encoding in HIPGNN. We compare EMOGI, MTGCN, SMG, and HIPGNN (without spatial context decoding) using five-fold cross-validation at an 80% training ratio. The left subfigure of Figure 4 shows box plots of the results, where HIPGNN with only spectral graph representation still outperforms, highlighting the effectiveness of spectral eigenvalue encoding.

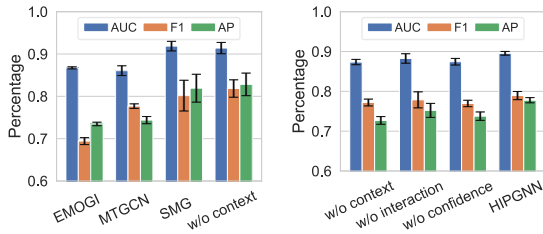


Figure 4: Ablation analysis of spectral graph representation (left) and spatial context decoding (right) on the STRINGdb dataset.

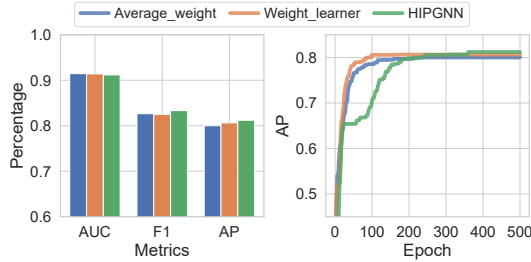


Figure 5: Comparison of the three model metrics as well as the variation of the best AP metric in the test set under three different loss weight schemes.

Spatial context decoding For decoding protein interaction contexts, we consider both interaction and confidence contexts for node representations. We evaluate the contribution of these contexts to HIPGNN using four variants: (1) Without context: removes both interaction and confidence contexts; (2) Without interaction: removes interaction context; (3) Without confidence: removes confidence context; (4) HIPGNN: the original model. The right subfigure of Figure 4, using a 20% training ratio and five-fold cross-validation, shows that both contexts improve HIPGNN’s performance, with confidence context being particularly impactful.

Parameter Analysis

Loss weights For the final loss computation, we used α , β , and γ to weight the protein interaction context, interaction confidence context, and cancer gene label loss, respectively. We empirically set $\alpha = 0.01$ on STRINGdb and $\alpha = 0.02$ on CPDB, with $\beta = 2/3(1-\alpha)$ and $\gamma = 1/3(1-\alpha)$. To validate this, we compared two other schemes: Average weight (uniformly setting all weights to $1/3$) and Weight learner, which uses a Bayesian learnable loss function (Li et al. 2020; Peng et al. 2021): $\mathcal{L} = \frac{1}{\alpha_l^2} \mathcal{L}_n + \frac{1}{\beta_l^2} \mathcal{L}_i + \frac{1}{\gamma_l^2} \mathcal{L}_w + 2\log(\alpha_l \beta_l \gamma_l)$, where α_l , β_l , and γ_l are learnable parameters. Figure 5 shows the three model performance metrics and the best AP metric variation over 500 epochs under the three schemes. Empirical weights achieved the best results. Additionally, setting α smaller aids in the convergence of cancer gene labeling loss. We observed that Average weight and Weight learner fall into local optima early, while our scheme continues optimizing, with metrics possibly improving beyond 500 epochs.

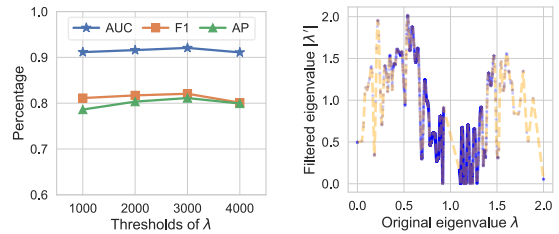


Figure 6: The eigenvalue thresholds analysis (left) and the spectral filter visualization (right).

Thresholds of eigenvalue We introduced the parameter q to control the selection of the first q -small and last q -large eigenvalues input into the model, thereby regulating its complexity. We evaluated HIPGNN’s performance with q values ranging from 1,000 to 4,000. As shown in the left subfigure of Figure 6, setting q to 3,000 yielded the best performance. Increasing q beyond this point resulted in decreased performance, aligning with our initial observation that the spectral energy tends to “flatten out” more at the spectrum’s ends.

Visualization of Spectral Filter

We applied a spectral filter to obtain the filtered eigenvalues in the proximity-aware spectral graph representation. In the right subfigure of Figure 6, we visualize the relationship between the filtered and original eigenvalues. The blue stars depict the distribution of eigenvalues, connected by a yellow dashed line. The figure shows that the spectral filter prioritizes eigenvalues near the spectrum’s ends over those in the middle. This suggests that spectral eigenvalue coding effectively addresses the key phenomenon in PPI networks caused by cancer genes: the “flattening out” of spectral energy.

Conclusion

This work takes a pioneering step toward bridging significant biological anomalies in protein interactions caused by cancer genes to the statistical graph anomaly. We identify a unique graph anomaly in cancer genes, termed weight heterogeneity, which leads to the “flattening out” of spectral energy. In response, we propose a novel model, HIPGNN, for the identification of cancer genes.

Broader impact. This work has the potential to benefit both the bioinformatics and network science fields. It not only lays a new theoretical foundation for cancer gene identification but also offers a fresh perspective and direction for research in graph anomaly detection.

Limitations. The phenomenon of weight heterogeneity was observed only in cancer genes on two PPI networks. Further validation on other PPI networks is necessary to refine this observation. Additionally, exploring other real-world scenarios where weight heterogeneity occurs could provide more validation datasets for graph anomaly detection.

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