Cluster-Guided Contrastive Graph Clustering Network

Xihong Yang¹, Yue Liu¹, Sihang Zhou², Siwei Wang¹, Wenxuan Tu¹, Qun Zheng³, Xinwang Liu^{1*}, Liming Fang⁴, En Zhu^{1†}

¹College of Computer, National University of Defense Technology, Changsha, China

²College of Intelligence Science and Technology, National University of Defense Technology, Changsha, China

³University of Science and Technology of China

⁴ Nanjing University of Aeronautics and Astronautics yangxihong@nudt.edu.cn

Abstract

Benefiting from the intrinsic supervision information exploitation capability, contrastive learning has achieved promising performance in the field of deep graph clustering recently. However, we observe that two drawbacks of the positive and negative sample construction mechanisms limit the performance of existing algorithms from further improvement. 1) The quality of positive samples heavily depends on the carefully designed data augmentations, while inappropriate data augmentations would easily lead to the semantic drift and indiscriminative positive samples. 2) The constructed negative samples are not reliable for ignoring important clustering information. To solve these problems, we propose a Cluster-guided Contrastive deep Graph Clustering network (CCGC) by mining the intrinsic supervision information in the high-confidence clustering results. Specifically, instead of conducting complex node or edge perturbation, we construct two views of the graph by designing special Siamese encoders whose weights are not shared between the sibling sub-networks. Then, guided by the high-confidence clustering information, we carefully select and construct the positive samples from the same high-confidence cluster in two views. Moreover, to construct semantic meaningful negative sample pairs, we regard the centers of different high-confidence clusters as negative samples, thus improving the discriminative capability and reliability of the constructed sample pairs. Lastly, we design an objective function to pull close the samples from the same cluster while pushing away those from other clusters by maximizing and minimizing the crossview cosine similarity between positive and negative samples. Extensive experimental results on six datasets demonstrate the effectiveness of CCGC compared with the existing state-of-the-art algorithms. The code and appendix of CCGC are available at https://github.com/xihongyang1999/CCGC on Github.

Introduction

Thanks to the strong representation learning capacity of the graph data, Graph Neural Networks (GNNs) have been successfully applied to various applications, such as node classification (Kipf and Welling 2017; Veličković et al. 2018; Duan et al. 2022b; Wang et al. 2020, 2021d; Liu et al. 2022f;



Figure 1: Visualization of the positive sample pairs selected by (a) GCA (Zhu et al. 2021), (b) SCAGC, (Xia et al. 2022c) and (c) the proposed method. The red dots denote the generated sample pairs. Specifically, if a point (i, j) is selected as positive, the *i*-th sample from the first view and the *j*-th sample from the second view are integrated as a positive sample pair. (d) is the ground-truth cluster indicator. The sample order is rearranged to make samples from the same cluster beside each other. From the figures, we can find that our proposed positive sample extraction mechanism is more discriminative than the existing algorithms. As a consequence, the learned network is also more informative.

Yang et al. 2022b), graph classification (Wang et al. 2018b; Liu et al. 2021), time series analysis(Liu and Liu 2021; Liu, Wu, and Liu 2022; Xie et al. 2022), knowledge graph(Liang et al. 2022a,b), and so on. Among all the directions in graph learning, deep graph clustering is a fundamental yet challenging unsupervised task, which has become a hot research spot recently (Wang et al. 2019; Tu et al. 2020; Liu et al.

^{*}Corresponding author

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2022c,d).

Contrastive learning, which could capture the supervision information implicitly without human annotations, has become a prominent technique in deep graph clustering. Although promising performance has been achieved, we observe two issues in the contrastive sample-pair construction process. 1) The quality of positive samples heavily depends on the carefully selected graph data augmentations. However, inappropriate graph data augmentations, like random attribute permutation and random edge drop-out, would easily lead to semantic drift (Lee, Lee, and Park 2021), and indiscriminative positive samples. 2) The constructed negative samples are not reliable enough since the existing algorithms neglect to exploit the important clustering information. Concretely, the existing methods randomly select negative samples, which loosely assign negative labels to samples from the same category. To improve the quality of negative samples, GDCL (Zhao et al. 2021) and SCAGC (Xia et al. 2022c) randomly select samples from the different clusters. Although verified to be effective, the current clustering-result-based methods heavily rely on the carefully designed graph data augmentation and the well pre-trained model, thus limiting the clustering performance.

To solve these issues, we propose a novel Cluster-guided Contrastive deep Graph Clustering method, i.e., CCGC. Concretely, to construct two node views with different semantics, we take advantage of the Siamese encoders and make the parameters un-shared between two sub-networks. In this way, complex structure- and attribute-level data augmentations are avoided while the semantic drift problem has also been solved.

After that, we carefully select and construct the positive samples from the same cluster in two views according to high-confidence clustering pseudo labels. In this manner, we improve the discriminative capacity of the positive samples. As shown in Fig. 1, we visualize the positive sample pairs constructed by (a) GCA (Zhu et al. 2021), (b) SCAGC (Xia et al. 2022c), (c) our methods. It is clearly observed that our constructed positive samples could better reveal the ground truth compared to other methods. Meanwhile, we regard the centers of different high-confidence clusters as the negative sample pairs, which are more reliable and semantic meaningful. Moreover, we design an objective function to pull close the samples from the same cluster and push away those from different clusters by maximizing and minimizing the cross-view cosine similarity between positive and negative samples. The key contributions of this paper are listed as follows:

- We propose a cluster-guided contrastive deep graph clustering network termed CCGC to improve the quality of positive and negative samples by mining the highconfidence clustering information.
- Instead of using carefully designed complex graph data augmentation, we conduct two views by designing special un-shared parameters Siamese encoders, thus avoiding semantic drift caused by inappropriate graph data augmentations.
- Extensive experimental results on six benchmark datasets

demonstrate the effectiveness of the proposed method against the existing state-of-the-art deep graph clustering competitors.

Related Work

Deep Graph Clustering

Clustering is a fundamental yet challenging task, which aims to learn node semantic representations and divide nodes into different clusters (Liu et al. 2022b,a; Zhang et al. 2020; Sun et al. 2021b; Wan et al. 2022; Xia et al. 2022b,d). Deep learning methods also attract attention (Zhou et al. 2020). Among those methods, deep graph clustering has been a hot research spot in recent years. According to the learning mechanism, the existing methods can be roughly grouped into three classes including generative methods, adversarial methods, and contrastive methods. Our survey paper (Liu et al. 2022d) summarizes the detailed information about the fast-growing deep graph clustering. CCGC is categorized into the last one, i.e., contrastive methods.

Inspired by the success of graph-auto-encoder (GAE) (Kipf and Welling 2016), the pioneer MGAE (Wang et al. 2017) first encodes the nodes with the graph-encoder (Kipf and Welling 2016) and then performs clustering on the latent features. After that, DAEGC (Wang et al. 2019) adopts the attention mechanisms (Vaswani et al. 2017; Veličković et al. 2018) in early works to improve the clustering performance. Furthermore, ARGA (Pan et al. 2019) and AGAE (Tao et al. 2019) improve the discriminative capability of samples by adversarial mechanisms (Wang et al. 2018a). In addition, SDCN (Bo et al. 2020) alleviates the over-smoothing problem by integrating GAE and auto-encoder into the unified framework. More recently, R-GAE (Liu et al. 2022e) enhances the existing GAE-based methods by alleviating the feature randomness and feature drift issues.

Although verified to be effective, since most of these methods adopt a distribution alignment loss function (Xie, Girshick, and Farhadi 2016) to force the learned node embeddings to have the minimum distortion against the pre-learned cluster centers, their clustering performance is highly dependent on good initial cluster centers, thus leading to manual trial-and-error pre-training (Wang et al. 2019; Pan et al. 2019; Bo et al. 2020; Tu et al. 2020). As a consequence, the performance consistency, as well as the implementing convenience, is largely decreased. Different from them, several contrastive methods (Hassani and Khasahmadi 2020; Cui et al. 2020; Pan and Kang 2021) replace the clustering guided loss function by the contrastive loss, thus getting rid of trial-and-error pre-training.

Contrastive Deep Graph Clustering

Contrastive learning has achieved great success in the fields of computer vision (Yang et al. 2022a) and graph learning (Xia et al. 2022a; Wang et al. 2021c; Yu et al. 2022; Duan et al. 2022a) in recent years. Inspired by their success, contrastive deep graph clustering methods (Liu et al. 2022c,g; Zhao et al. 2021) are increasingly proposed.

The fashions of the data augmentations and the positivenegative sample pair construction are two crucial factors to



Figure 2: Illustration of the Cluster-guided Contrastive Graph Clustering (CCGC) algorithm. In our proposed algorithm, we firstly encode the two-view node embeddings with the proposed parameter un-shared Siamese encoders. Then, we perform K-means on the fused node embeddings and obtain the clustering results. Subsequently, based on the high-confidence clustering results, we improve the quality of positive and negative samples by the discriminative positive sample construction strategy and reliable negative sample construction strategy in section . Lastly, we design an objective function to pull close the samples from the same cluster while pushing away different high-confidence cluster centers, thus enhancing the discriminative capability of the network.

determine the performance of the contrastive deep graph clustering methods. In this section, we review the existing contrastive methods from these two perspectives.

Data augmentation. The technique of data augmentation plays an important role in contrastive deep graph clustering. Specifically, the existing methods construct different views of the graph by applying distinct augmentations to the graph. For example, the graph diffusion matrix would be regarded as one of the augmented graphs in MVGRL (Hassani and Khasahmadi 2020), GDCL (Zhao et al. 2021), and DCRN (Liu et al. 2022c). Differently, SCAGC (Xia et al. 2022c) randomly adds or drops edges to perturb the structure of graphs. From the feature perspective, DCRN and SCAGC conduct augmentations on node attributes by attribute corruption. Although verified to be effective, the promising performance of these methods highly depends on the carefully selected data augmentations. Some works (Lee, Lee, and Park 2021; Sun et al. 2021a) point out that the inappropriate data augmentations would easily lead to semantic drift and the similar conclusion could be found in section . To overcome the issue, we propose a novel augmentation fashion to construct different graph views by setting the parameters of Siamese encoders to be un-shared, thus avoiding the semantic drift caused by inappropriate augmentations.

Positive and negative sample pair construction. Another crucial component in contrastive methods is the fashion of the positive and negative sample pair construction. Specifically, contrastive methods pull together positive samples while pushing away negative ones, thus the quality of pos-

itive and negative samples determines the performance of contrastive methods. Concretely, MVGRL (Hassani and Khasahmadi 2020) regards different augmented views of the same node and generates the negative samples by randomly shuffling the feature. Besides, DCRN (Liu et al. 2022c) pulls together the same node in different views while pushing away different nodes under the feature decorrelation constrain. Moreover, SCAGC (Xia et al. 2022c) and GDCL (Zhao et al. 2021) improve the quality of negative samples by randomly selecting samples from the different clusters. Although verified to be effective, they still rely on a well pre-trained model to select high-quality positive and negative samples. To solve this problem, we propose a highconfidence clustering information guided fashion of positive and negative sample construction, thus enhancing the discriminative capability and reliability of the sample pairs.

Method

In this section, we propose a novel Cluster-guided Contrastive deep Graph Clustering algorithm (CCGC). The overall framework of CCGC is shown in Fig. 2.

Notations and Problem Definition

In an undirected graph $\mathcal{G} = \{\mathbf{X}, \mathbf{A}\}$, let $\mathcal{V} = \{v_1, v_2, \ldots, v_N\}$ be a set of N nodes with K classes and \mathcal{E} be a set of edges. $\mathbf{X} \in \mathbb{R}^{N \times D}$ and $\mathbf{A} \in \mathbb{R}^{N \times N}$ denote the attribute matrix and the original adjacency matrix, respectively. The degree matrix is formulated as $\mathbf{D} = diag(d_1, d_2, \ldots, d_N) \in \mathbb{R}^{N \times N}$ and $d_i = \sum_{(v_i, v_j) \in \mathcal{E}} a_{ij}$.

The graph Laplacian matrix is defined as $\mathbf{L} = \mathbf{D} - \mathbf{A}$. With the renormalization trick $\widehat{\mathbf{A}} = \mathbf{A} + \mathbf{I}$, the symmetric normalized graph Laplacian matrix is denoted as $\widetilde{\mathbf{L}} = \mathbf{I} - \widehat{\mathbf{D}}^{-\frac{1}{2}} \widehat{\mathbf{A}} \widehat{\mathbf{D}}^{-\frac{1}{2}}$.

Parameter Un-shared Siamese Encoders

In this section, following SCGC (Liu et al. 2022e), we embed the nodes into the latent space and construct two different sample views by designing a parameter un-shared Siamese encoders.

Before encoding, we adopt a widely-used Laplacian filter (Cui et al. 2020) to conduct neighbour information aggregation as follows:

$$\widetilde{\mathbf{X}} = (\mathbf{I} - \widetilde{\mathbf{L}})^t \mathbf{X},\tag{1}$$

where $\widetilde{\mathbf{L}}$ is the symmetric normalized graph Laplacian matrix. *t* denotes the layer number of the Laplacian filter. $\widetilde{\mathbf{X}}$ is the smoothed attribute matrix. Then we encode $\widetilde{\mathbf{X}}$ with MLP encoders as follows:

$$\mathbf{E}^{v_1} = \operatorname{Encoder}_1(\widetilde{\mathbf{X}}), \ \mathbf{E}^{v_2} = \operatorname{Encoder}_2(\widetilde{\mathbf{X}}),$$
 (2)

where \mathbf{E}^{v_1} and \mathbf{E}^{v_2} denotes the first and second view of the node embeddings, respectively. For the encoders, we design them to have the same architecture but un-shared learnable parameters. Subsequently, we normalize \mathbf{E}^{v_1} and \mathbf{E}^{v_2} with ℓ^2 -norm:

$$\mathbf{E}^{v_1} = \frac{\mathbf{E}^{v_1}}{||\mathbf{E}^{v_1}||_2}, \ \mathbf{E}^{v_2} = \frac{\mathbf{E}^{v_2}}{||\mathbf{E}^{v_2}||_2}.$$
 (3)

By this setting, we construct two node views with different semantic, thus avoiding semantic drift caused by inappropriate data augmentations on the graphs. Experimental evidence could be found in section .

Cluster-guided Contrastive Learning

In this section, we propose the Cluster-guided Contrastive Learning (CCL) to improve the discriminative capability and reliability of samples by mining the high-confidence clustering information. To be specific, we firstly fuse the two views of the node embeddings as follows:

$$\mathbf{E} = \frac{1}{2} (\mathbf{E}^{v_1} + \mathbf{E}^{v_2}). \tag{4}$$

Then we perform K-means on **E** and obtain the clustering results. In order to generate more reliable clustering information (Liu et al. 2022g), we define the confidence score **CONF** $_i$ of *i*-th sample as formulated:

$$\mathbf{CONF}_i = e^{-||\mathbf{E}_i - \mathbf{C}_p||^2},\tag{5}$$

where \mathbf{E}_i denotes the *i*-th node embedding. Besides, $\mathbf{C}_p(p = 1, 2, ..., K)$ denotes the center of the cluster, which contains the *i*-th sample. Subsequently, based on **CONF**, we denote the high-confidence sample indexes *h* as follows:

$$h = \{h_1, h_2, \dots, h_i, \dots\},\tag{6}$$

where the element h_i indicates that h_i -th sample belongs to top τ high-confidence sample set.

Based on these high-confidence samples and their clustering pseudo labels, we propose two sample construction strategies including Discriminative Positive sample construction Strategy (DPS) and Reliable Negative sample construction Strategy (RNS).

Discriminative Positive Sample Construction Strategy. In this part, we design DPS to enhance the discriminative capability of positive samples. The proposed DPS contains three steps. Firstly, we select the high-confidence samples of two views with high-confidence indexes h as follows:

$$\mathbf{H}^{v_1} = \mathbf{E}^{v_1}_{[h,:]}, \ \mathbf{H}^{v_2} = \mathbf{E}^{v_2}_{[h,:]}.$$
(7)

Then, according to the corresponding pseudo labels, we group \mathbf{H}^{v_1} and \mathbf{H}^{v_2} into K disjoint clusters, i.e., $\mathbf{B}_p^{v_1}(p = 1, 2, ..., K)$, and $\mathbf{B}_q^{v_2}(q = 1, 2, ..., K)$. Subsequently, the positive samples will be selected and constructed from the same high-confidence clusters in Eq. (9). In this setting, the high-confidence clustering pseudo labels could be utilized as the supervisory information to improve the discriminative capability of the positive samples.

Reliable Negative Sample Construction Strategy. For the negative sample construction, the existing works (Zhu et al. 2021; Liu et al. 2022c) directly regard all other non-positive samples as negative samples, easily bringing false-negative samples. To alleviate this issue, we propose RNS, which contains two steps. Concretely, we first calculate the centers of high-confidence samples in two views:

$$CEN_{p}^{v_{1}} = avg(\mathbf{B}_{p}^{v_{1}}), p = 1, 2, ..., K,$$

$$CEN_{q}^{v_{2}} = avg(\mathbf{B}_{q}^{v_{2}}), q = 1, 2, ..., K,$$
(8)

where avg is the average function. Then we regard the different high-confidence centers as the negative samples in Eq. (10). In this manner, RNS would enhance the reliability of negative samples, thus reducing the possibility of false-negative samples.

In summary, the proposed CCL would guide our network to mine the supervisory information in the high-confidence clustering pseudo labels, thus improving the discriminative capability and reliability of samples.

Objective Function

The proposed method jointly optimizes two objectives including the positive sample loss \mathcal{L}_{pos} and the negative sample loss \mathcal{L}_{neg} .

In detail, \mathcal{L}_{pos} is the Mean Squared Error (MSE) loss between the normalized cross-view positive sample embeddings, as formulated:

$$\mathcal{L}_{pos} = \frac{1}{K} \sum_{p=1}^{K} \sum_{i=1}^{n_p} \left\| \mathbf{B}_{p[i,:]}^{v_1} - \mathbf{B}_{p[i,:]}^{v_2} \right\|_2^2$$

$$= \frac{1}{K} \sum_{p=1}^{K} \sum_{i=1}^{n_p} \left(2 - 2 \left\langle \mathbf{B}_{p[i,:]}^{v_1}, \mathbf{B}_{p[i,:]}^{v_2} \right\rangle \right),$$
(9)

where $\mathbf{B}_{p[i,:]}^{v_1}$ and $\mathbf{B}_{p[i,:]}^{v_2}$ denotes the *i*-th normalized node embedding in the *p*-th cluster of the first and second view,

Dataset	Metrix	DAEGC	ARGA	SDCN	AGE	MVGRL	AutoSSL	AFGRL	GDCL	CCGC
CORA	ACC	70.43±0.36	71.04±0.25	35.60±2.83	73.50±1.83	70.47±3.70	63.81±0.57	26.25±1.24	70.83±0.47	73.88±1.20
	NMI	52.89±0.69	51.06±0.52	14.28±1.91	57.58±1.42	55.57±1.54	47.62±0.45	12.36±1.54	56.30±0.36	56.45±1.04
	ARI	49.63±0.43	47.71±0.33	07.78±3.24	50.10±2.14	48.70±3.94	38.92±0.77	14.32±1.87	48.05±0.72	52.51±1.89
	F1	68.27±0.57	69.27±0.39	24.37±1.04	69.28±1.59	67.15±1.86	56.42±0.21	30.20±1.15	52.88±0.97	70.98±2.79
CITESEER	ACC	64.54±1.39	61.07±0.49	65.96±0.31	69.73±0.24	62.83±1.59	66.76±0.67	31.45±0.54	66.39±0.65	69.84±0.94
	NMI	36.41±0.86	34.40±0.71	38.71±0.32	44.93±0.53	40.69±0.93	40.67±0.84	15.17±0.47	39.52±0.38	44.33±0.79
	ARI	37.78±1.24	34.32±0.70	40.17±0.43	45.31±0.41	34.18±1.73	38.73±0.55	14.32±0.78	41.07±0.96	45.68±1.80
	F1	62.20±1.32	58.23±0.31	63.62±0.24	64.45±0.27	59.54±2.17	58.22±0.68	30.20±0.71	61.12±0.70	62.71±2.06
AMAP	ACC	75.96±0.23	69.28±2.30	53.44±0.81	75.98±0.68	41.07±3.12	54.55±0.97	75.51±0.77	43.75±0.78	77.25±0.41
	NMI	65.25±0.45	58.36±2.76	44.85±0.83	65.38±0.61	30.28±3.94	48.56±0.71	64.05±0.15	37.32±0.28	67.44±0.48
	ARI	58.12±0.24	44.18±4.41	31.21±1.23	55.89±1.34	18.77±2.34	26.87±0.34	54.45±0.48	21.57±0.51	57.99±0.66
	F1	69.87±0.54	64.30±1.95	50.66±1.49	71.74±0.93	32.88 ± 5.50	54.47±0.83	69.99±0.34	38.37±0.29	72.18±0.57
BAT	ACC	52.67±0.00	67.86±0.80	53.05±4.63	56.68±0.76	37.56±0.32	42.43±0.47	50.92±0.44	45.42±0.54	75.04±1.78
	NMI	21.43±0.35	49.09±0.54	25.74±5.71	36.04±1.54	29.33±0.70	17.84±0.98	27.55±0.62	31.70±0.42	50.23±2.43
	ARI	18.18±0.29	42.02±1.21	21.04±4.97	26.59±1.83	13.45±0.03	13.11±0.81	21.89±0.74	19.33±0.57	46.95±3.09
	F1	52.23±0.03	67.02±1.15	46.45±5.90	55.07±0.80	29.64±0.49	34.84±0.15	46.53±0.57	39.94±0.57	74.90±1.80
EAT	ACC	36.89±0.15	52.13±0.00	39.07±1.51	47.26±0.32	32.88±0.71	31.33±0.52	37.42±1.24	33.46±0.18	57.19±0.66
	NMI	05.57±0.06	22.48±1.21	08.83±2.54	23.74±0.90	11.72±1.08	07.63±0.85	11.44±1.41	13.22±0.33	33.85±0.87
	ARI	05.03±0.08	17.29±0.50	06.31±1.95	16.57±0.46	04.68±1.30	02.13±0.67	06.57±1.73	04.31±0.29	27.71±0.41
	F1	34.72±0.16	52.75±0.07	33.42±3.10	45.54±0.40	25.35±0.75	21.82±0.98	30.53±1.47	25.02±0.21	57.09±0.94
UAT	ACC	52.29±0.49	49.31±0.15	52.25±1.91	52.37±0.42	44.16±1.38	42.52±0.64	41.50±025	48.70±0.06	56.34±1.11
	NMI	21.33±0.44	25.44±0.31	21.61±1.26	23.64±0.66	21.53±0.94	17.86±0.22	17.33±0.54	25.10±0.01	28.15±1.92
	ARI	20.50±0.51	16.57±0.31	21.63±1.49	20.39±0.70	17.12±1.46	13.13±0.71	13.62±0.57	21.76±0.01	25.52±2.09
	F1	50.33±0.64	50.26±0.16	45.59±3.54	50.15±0.73	39.44±2.19	34.94±0.87	36.52±0.89	45.69±0.08	55.24±1.69

Table 1: The average clustering performance of ten runs on six benchmark datasets. The performance is evaluated by four metrics with mean value and standard deviation. The bold and underlined values indicate the best and the runner-up results, respectively.

Dataset	Туре	Sample	Dimension	Edge	Class
CORA	Graph	2708	1433	5429	7
CITESEER	Graph	3327	3703	4732	6
AMAP	Graph	7650	745	119081	8
BAT	Graph	131	81	1038	4
EAT	Graph	399	203	5994	4
UAT	Graph	1190	239	13599	4

respectively. Besides, n_p is the number of high-confidence samples in the *p*-th cluster. In this manner, the positive samples are pulled together. Besides, we define \mathcal{L}_{neg} as the cosine similarity between different centers of the highconfidence embeddings:

$$\mathcal{L}_{neg} = \frac{1}{K^2 - K} \sum_{p=1}^{K} \sum_{q=1}^{K} \frac{\left\langle \mathbf{CEN}_{p}^{v_1}, \mathbf{CEN}_{q}^{v_2} \right\rangle}{\|\mathbf{CEN}_{p}^{v_1}\|_2 \cdot \|\mathbf{CEN}_{q}^{v_2}\|_2}, p \neq q,$$
(10)

where $\mathbb{CEN}_p^{v_1}$ is the *p*-th high-confidence center in the first view and $\mathbb{CEN}_q^{v_2}$ is the *q*-th high-confidence center in the second view. By setting this, we push the negative samples away. In summary, the total loss of the proposed CCGC is calculated as:

$$\mathcal{L} = \mathcal{L}_{pos} + \alpha \mathcal{L}_{neg}, \tag{11}$$

where α is a trade-off between \mathcal{L}_{pos} and \mathcal{L}_{neg} . The detailed learning process of CCGC is shown in Algorithm 1.

Experiments

Benchmark Datasets

The experiments are conducted on six widely-used benchmark datasets, including CORA (Cui et al. 2020), CITE- SEER (Cui et al. 2020), BAT (Liu et al. 2022e; Mrabah et al. 2021), EAT (Liu et al. 2022e), UAT (Liu et al. 2022e), AMAP (Liu et al. 2022c). The summarized information is shown in Table 2.

Experiment Setup

The experimental environment contains one desktop computer with the Intel Core i7-7820x CPU, one NVIDIA GeForce RTX 2080Ti GPU, 64GB RAM, and the PyTorch deep learning platform. The max training epoch number is set to 400. We minimize the total loss in Eq. (11) with widely-used Adam optimizer (Kingma and Ba 2014) and then perform K-means over the learned embeddings. To obtain reliable clustering, we adopt a two-stage training strategy. The discriminative capacity of the model can be improved in the first stage. In the second stage, the contrastive learning mechanism can be enhanced by the high-confidence clustering pseudo labels. Ten runs are conducted for all methods. For the baselines, we adopt their source with original settings and reproduce the results. The hyper-parameter settings are summarized in Table 1 of the Appendix. The clustering performance is evaluated by four metrics including ACC, NMI, ARI, and F1 (Zhou et al. 2019; Wang et al. 2021b,a; Li et al. 2022).

Performance Comparison

In this subsection, we compare the clustering performance of our proposed algorithm with baselines on six datasets with four metrics. Among these methods, three classical deep graph clustering methods (Wang et al. 2019; Pan et al. 2019; Bo et al. 2020) utilize the graph auto-encoder to learn the node representation for clustering. Besides, five contrastive deep graph clustering methods (Cui et al. 2020; Hassani



Figure 3: 2D visualization on two datasets. The first row and second row correspond to CORA and AMAP, respectively.

Algorithm 1: CCGC

Input: The input graph $\mathcal{G} = \{\mathbf{X}, \mathbf{A}\}$; The iteration number *I*;

Output: The clustering result **R**.

- 1: Obtain the smoothed attributes $\widetilde{\mathbf{X}}$ with Eq (1).
- 2: for i = 1 to I do
- 3: Encode $\mathbf{\tilde{X}}$ into two views with Eq. (2).
- 4: Normalize the embeddings \mathbf{E}^{v_1} , \mathbf{E}^{v_2} with Eq. (3).
- 5: Perform K-means on **E** to obtain the clustering result.
- 6: Fuse \mathbf{E}^{v_1} and \mathbf{E}^{v_2} to obtain \mathbf{E} with Eq. (4).
- 7: Obtain high-confidence samples \mathbf{H}^{v_1} and \mathbf{H}^{v_2} with Eq. (7).
- 8: Construct positive and negative samples by DPS and RNS.
- 9: Calculate the contrastive loss with Eq. (9) and Eq. (10).
- 10: Update the whole network by minimizing \mathcal{L} in Eq. (11).
- 11: end for
- 12: Perform K-means on **E** to obtain the final clustering result **R**. 13: return **R**

and Khasahmadi 2020; Jin et al. 2021; Lee, Lee, and Park 2021; Zhao et al. 2021) improve the discriminative capability of samples by the contrastive strategies. From the results in Table.1, we find that CCGC obtains better performance compared with the classical deep graph clustering methods. The reason is that contrastive learning could assist the model capture the supervision information implicitly. Besides, the contrastive methods achieve sub-optimal performance compared to ours. This is because we improve the discriminative capability and reliability of samples with the important clustering information. In summary, our method outperforms most of them on six datasets with four metrics. Taking the results on EAT dataset for example, CCGC exceeds the runner-up by 5.06%, 10.11%, 10.42%, 4.34% with respect to ACC, NMI, ARI, and F1. Besides, due to the limitation of the space, we conduct additional comparison experiments with nine baselines. Those results are shown in Table 2 of the Appendix. The results could also demonstrate the superiority of CCGC.

Ablation Studies

In this section, we first verify the effectiveness of two proposed sample construction strategies with experiments. Besides, we demonstrate the effect of parameter un-shared encoders and analyze the sensitivity of hyper-parameters in CCGC.

Effectiveness of DPS and RNS To verify the effect of the proposed Discriminative Positive sample construction Strategy (DPS) and Reliable Negative sample construction Strategy (RNS), we conduct extensive experiments as shown in Table 3. For simplicity, we denote "(w/o) DPS" and "(w/o) RNS" as replacing DPS and RNS in our model with the regular positive and negative sample construction fashion (Liu et al. 2022c), i.e., regarding the same samples in two view as positive samples while considering other samples as negative ones. From the observations, we conclude that the performance will decrease without any one of DPS and RNS, revealing that both strategies make essential contributions to boosting the performance. In addition, the quality of positive and negative sample pairs is improved compared with the regular sample construction fashion. Overall, the experimental results have verified the effectiveness of DPS and RNS.

Effectiveness of Parameter Un-shared Encoders To avoid the complex augmentations on graphs, we design the un-shared Simases encoders to conduct two-node views. In this part, we compare our view construction method with other classical graph data augmentations including edge dropping (Xia et al. 2022c), edge adding (Xia et al. 2022c), graph diffusion (Hassani and Khasahmadi 2020), and feature masking (Zhao et al. 2021). Concretely, in Table 3, we first make the encoders in CCGC to share parameter and then adopt the data augmentation as randomly dropping 20% edges ("Drop Edges"), or randomly adding 20% edges ("Add Edges"), or graph diffusion ("Diffusion") with 0.20 teleportation rate, or randomly masking 20% features ("Mask Features"). From the results, we observe that the commonly used graph augmentations might lead to semantic drift (Lee, Lee, and Park 2021), thus undermining the performance. In summary, expensive experiments have demonstrated the effectiveness of the proposed parameter un-shared encoders.

Hyper-Parameter Analysis

Sensitivity Analysis of hyper-parameter threshold τ We investigate the influence of the hyper-parameter threshold τ on six datasets as shown in Fig.5. From the results, we observe that the model obtains promising performance when $\tau \in [50\%, 70\%]$. The reasons are as follows: 1) When

Dataset	Metric	(w/o) Positive	(w/o) Negitive	Drop Edges	Add Edges	Diffusion	Mask Feature	Ours
CORA	ACC	60.03±6.28	70.29±0.86	57.95±4.32	57.89±3.16	59.57±2.95	67.40±1.76	73.88±1.20
	NMI	47.33±3.97	53.67±1.15	39.32±4.90	39.11±3.82	39.84±2.72	48.84±2.02	55.56±1.04
	ARI	37.66±5.86	47.09±1.29	29.10±4.52	29.74±2.84	30.73±2.95	41.32±2.33	52.51±1.89
	F1	53.85±9.38	68.48±1.17	53.45±5.57	55.33± 6.39	55.01±7.22	63.16±3.54	70.98±2.79
CITESEER	ACC	58.26±6.19	67.92±1.32	66.55±1.27	66.31±1.40	68.32±0.62	69.14±0.66	69.84±0.94
	NMI	38.62±3.34	42.05±1.34	38.91±2.04	39.43±1.72	41.83±0.94	42.49±0.89	44.33±0.79
	ARI	35.78±4.28	42.66±1.65	38.85±1.63	39.00±1.32	41.23±0.99	43.12±1.16	44.68±1.80
	F1	45.90±7.76	62.82±0.92	58.38±1.51	59.56±1.40	59.89±0.83	60.78±1.43	62.71±2.06
АМАР	ACC	29.81±1.71	73.74±0.82	75.84±1.12	75.75±1.77	70.89±3.28	76.48±1.88	77.25±0.41
	NMI	15.18±1.93	62.65±1.48	62.98±1.15	63.11±1.89	58.14±2.05	66.44±0.85	67.44±0.48
	ARI	05.85±0.95	52.74±1.51	55.81±1.63	55.79±2.85	49.68±3.16	56.81±2.09	57.99±0.66
	F1	26.61±3.49	68.45±1.08	69.82±3.24	69.83±3.13	60.43±6.16	71.13±1.40	72.18±0.57
BAT	ACC	65.19±2.00	73.59±2.32	50.00±3.87	67.02±2.71	52.60±2.72	72.06±2.92	75.04±1.78
	NMI	44.08±1.35	47.07±2.38	24.59±2.01	45.13±4.73	29.78±5.06	48.67±2.47	50.23±2.43
	ARI	38.46±2.60	44.37±3.47	18.91±3.80	39.18±5.16	21.12±5.70	44.07±3.80	46.95±3.09
	F1	62.24±2.57	73.36±2.35	48.44±4.90	65.54±2.66	48.72±2.54	71.57±3.46	74.90±1.80
EAT	ACC	48.42±2.91	52.31±1.66	45.76±1.00	49.32±1.53	45.71±1.67	52.61±1.70	57.19±0.66
	NMI	25.88±2.73	26.12±2.07	14.57±3.14	23.45 ± 2.00	19.98±1.84	27.18±1.55	33.85±0.87
	ARI	19.29±2.02	20.94±1.40	10.43±1.63	16.85±1.76	14.71±3.32	20.50±1.46	27.71±0.41
	F1	46.39±4.98	52.63±1.90	43.78±1.36	48.99±2.18	40.46±3.81	52.51±2.02	57.09±0.94
UAT	ACC	41.39±2.96	49.04±1.33	57.02±1.44	55.61±1.00	51.45±2.04	52.33±1.95	56.34±1.11
	NMI	12.08±1.86	22.89±1.71	26.07±1.43	29.06±1.49	24.18±2.19	24.12±1.99	28.15±1.92
	ARI	7.70±0.63	20.70±1.22	26.03±1.88	23.69±1.58	22.55 ± 2.80	18.54±3.07	25.52±2.09
	F1	36.14±3.32	44.22±2.24	54.67±1.67	54.74± 1.16	46.06±2.97	51.17±2.16	55.24±1.69

Table 3: Ablation studies of CCGC on six datasets.



Figure 4: Sensitivity analysis of the hyper-parameter α on six datasets.

 $\tau < 50\%$, the discriminative capacity of the network is limited due to few number of positive samples. 2) When $\tau > 70\%$, the over-confidence pseudo labels would easily lead the network to confirmation bias (Arazo et al. 2020).

Sensitivity Analysis of hyper-parameter α Besides, to the trade-off hyper-parameter α , the experimental results are shown in Fig.4. From these results, we observe that the performance will not fluctuate greatly when α is varying. This demonstrates that our CCGC is insensitive to α . Moreover, CCGC is also insensitive to the layer number t of Laplacian filters. Experimental evidences can be found in Fig. 1 in Appendix.

Visualization Analysis

In this part, we visualize the distribution of the learned embeddings of six baselines and CCGC to show the superiority of CCGC on CORA and AMAP datasets via *t*-SNE algo-



Figure 5: Sensitivity analysis of the hyper-parameter τ on six datasets.

rithm (Van der Maaten and Hinton 2008). As shown in Fig. 3, we can conclude that CCGC better reveals the intrinsic clustering structure compared with other baselines.

Conclusion

In this work, we propose a Cluster-guided Contrastive deep Graph Clustering network termed CCGC to improve the quality of positive and negative samples. To be specific, we firstly construct two views with the un-shared parameters Siamese encoders to avoid semantic drift caused by the inappropriate graph data augmentations. Besides, the proposed positive and negative samples construction strategies improve the discriminative capability and reliability of samples by mining the supervision information in the highconfidence clustering pseudo labels. Extensive experiments on six datasets demonstrate the effectiveness of our proposed method.

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