Imbalanced Multiple Noisy Labeling for Supervised Learning

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Abstract
When labeling objects via Internet-based outsourcing systems, the labelers may have bias, because they lack expertise, dedication and personal preference. These reasons cause Imbalanced Multiple Noisy Labeling. To deal with the imbalance labeling issue, we propose an agnostic algorithm PLAT (Positive Label frequency Threshold) which does not need any information about quality of labelers and underlying class distribution. Simulations on eight real-world datasets with different underlying class distributions demonstrate that PLAT not only effectively deals with the imbalanced multiple noisy labeling problem that off-the-shelf agnostic methods cannot cope with, but also performs nearly the same as majority voting under the circumstances that labelers have no bias.

Introduction
Online outsourcing systems, such as Amazon’s Mechanical Turk, allow multiple human labelers to label the same objects efficiently. However, the quality of labels cannot be guaranteed. Facing noisy labels, it is usual to obtain multiple labels for some or all data points. A preliminary study (Sheng, Provost and Ipeirotis 2008) discussed a straightforward strategy of using multiple noisy labels majority voting (MV). Their work implicitly assumed that mislabeling is uniformly distributed across the entire data points, and concluded that as long as the labeling quality is greater than 50\%, the eventual integrated labeling quality and the performance of the model learned are improved if more repeated labels are obtained.

However, the reality is that mislabeling is usually not uniformly distributed. Due to lack of expert knowledge, most labelers tend to make shallow determination by common sense or simply repeat what others say. Taking binary classification for example, it is not unusual that labeling on minority examples is error-prone. In this study, we treat minority as the positive class. When labeling is imbalanced, the number of negative labels obtained is far more than that of positive labels. If $MV$ is applied, it will make negative examples outnumber positive ones, resulting in an imbalanced class distribution in the final training set, even if the true distribution is balanced. Extremely, the training set might contain no positive examples.

Besides $MV$, other approaches have been proposed. Snow et al. (2008) proposed a simple Naive Bayes ($NB$) approach to construct a weighted ensemble for consensus labeling. Raykar et al. (2010) modeled label expertise via the EM algorithm to predict underlying labels. Yan et al. (2011) proposed a semi-supervised approach to model multiple noisy annotators. All these methods require prior information such as prior knowledge about each labeler or difficulty of each example. In real-world applications, this is truly a chicken-and-egg problem when the tasks start up on the Internet.

We propose an agnostic algorithm PLAT to use skewed noisy labels to induce an integrated label for each example. It solves the problem that minority examples (assuming positive cases) in the training set occur rarely, because of imbalanced noisy labeling.

Problem statement
We assume that a data set contains a proportion $d$ of true positive examples and $1-d$ of true negative examples. $d = 0.5$ indicates the underlying class distribution is completely balanced. A variable $V$ is introduced to control the percentage of mislabeling on the positive data points. It reflects the level of imbalanced labeling, the larger $V$ the higher level of imbalance. If all labelers have the same overall labeling quality $p$ which can be treated as the integration of the labeling quality on positive examples ($p_+$), and $p_-$ on negative examples, we calculate $p_+ = (d+Vp-V)/d$ and $p_- = (p+V-Vp-d)/(1-d)$. When $MV$ is applied, the integrated quality $q$ of multiple noisy labels can be calculated by using Bernoulli model as (with a total odd number of labels $2N+1$):

\[ q = \sum_{i=N+1}^{2N+1} \binom{2N+1}{i} p^i (1-p)^{2N+1-i}. \]

Similarly, we have $q_+$ and $q_-$ on positive examples and negative examples respectively by applying the formula to...
$p_P$ and $p_N$. Then we calculate the ratio of the number of “labeled” positive examples ($N_P$) and that of “labeled” negative examples ($N_N$) as follows:

$$\alpha = \frac{N_P}{N_N} = \frac{(d_q + (1-d)(1-q_s))/((1-d)q_s + d(1-q_p))}{\alpha}$$

For example, supposing the underlying class distribution is completely balanced ($d = 0.5$) and $V = 0.8$, if $0.5 < p < 0.7$, $\alpha$ decreases as the number of labels increases when $MV$ is applied. With the reduction of $\alpha$, the number of positive examples in the final training set declines, which will eventually reduce the learning model accuracy. Theoretical analysis shows if (1) the quality of labeling is quite low ($0.5 \leq p \leq 0.7$) and (2) the imbalance labeling level is significant ($0.7 \leq V \leq 1.0$), $MV$ does not work at all with imbalanced multiple noisy labeling. If the underlying class distribution is imbalanced, the result will be even worse.

**PLAT Algorithm and Experiments**

Our approach, based on the distribution of positive labels in the multiple noisy label set of each example, is to dynamically determine the threshold that can make the ratio of the numbers of positive and negative examples in the integrated training set close to the underlying class distribution of the dataset. We first calculate the frequency of positive labels (denoted by $f_+$) of each multiple label set. Then we group the examples with the same and almost the same $f_+$ values. Due to the imbalance, the labeling qualities on two classes are different. Given an example with the true positive label, the number of positive labels obeys the binomial distribution $B(N, p_P)$. Similarly, for a true negative example, the number of positive labels obeys $B(N, 1-p_N)$. With these two distributions and the numbers of examples in different $f_+$, we propose an approach PLAT (Positive Label frequency Threshold) to estimate a threshold $T$. If we plot the number of examples with the same $f_+$ as Figure 1 illustrates, we will find (1) two peaks when $p_P$ and $1-p_N$ are significantly different, which stand for the centers of positive and negative examples respectively; (2) only one peak when $p_P$ and $1-p_N$ are nearly the same. Correspondingly, we can choose (1) the valley between two peaks, or (2) the only peak as the estimated $T$ value. PLAT uses the threshold $T$ to determine the integrated labels of training examples.

We compared our approach with $MV$ and its two variants $MV Beta$ and Pairwise Beta proposed by (Sheng 2011) on eight real-world datasets with different $d$ values collected from the UCI database repository. We conducted the simulation using J48 in WEKA (Witten and Frank 2005). We show accuracy results on four of these eight datasets under different settings in Figure 2. Our approach is superior to the three off-the-shelf methods.

![Figure 2. Accuracy of different utilization methods](image)

**Conclusion**

We have comprehensively investigated the performance of PLAT under different circumstances: balanced or imbalanced labeling, potentially balanced or imbalanced class distributions, and/or labelers with different labeling qualities. Experimental results have shown that it always performs effectively. In the future, we will further study how to handle the imbalance labeling of multi-class classification and how to apply PLAT to active learning of imbalanced repeated labeling.

**References**


