MIDAS: Microcluster-Based Detector of Anomalies in Edge Streams

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Abstract
Given a stream of graph edges from a dynamic graph, how can we assign anomaly scores to edges in an online manner, for the purpose of detecting unusual behavior, using constant time and memory? Existing approaches aim to detect individually surprising edges. In this work, we propose MIDAS, which focuses on detecting microcluster anomalies, or suddenly arriving groups of suspiciously similar edges, such as lockstep behavior, including denial of service attacks in network traffic data. MIDAS has the following properties: (a) it detects microcluster anomalies while providing theoretical guarantees about its false positive probability; (b) it is online, thus processing each edge in constant time and constant memory, and also processes the data $108 - 505$ times faster than state-of-the-art approaches; (c) it provides 46%-52% higher accuracy (in terms of AUC) than state-of-the-art approaches.

Introduction
Anomaly detection in graphs is a critical problem for finding suspicious behavior in innumerable systems, such as intrusion detection, fake ratings, and financial fraud. This has been a well-researched problem with majority of the proposed approaches (Akoglu, McGlohon, and Faloutsos 2010; Chakrabarti 2004; Hooi et al. 2017; Jiang et al. 2016; Kleinberg 1999; Shin, Eliassi-Rad, and Faloutsos 2018) focusing on static graphs. However, many real-world graphs are dynamic in nature, and methods based on static connections may miss temporal characteristics of the graphs and anomalies.

Among the methods focusing on dynamic graphs, most of them have edges aggregated into graph snapshots (Eswaran et al. 2018; Sun, Tao, and Faloutsos 2006; Sun et al. 2007; Koutra, Vogelstein, and Faloutsos 2013; Sricharan and Das 2014; Gupta et al. 2012). However, to minimize the effect of malicious activities and start recovery as soon as possible, we need to detect anomalies in real-time or near real-time i.e. to identify whether an incoming edge is anomalous or not, as soon as we receive it. In addition, since the number of vertices can increase as we process the stream of edges, we need an algorithm which uses constant memory in graph size.

Moreover, fraudulent or anomalous events in many applications occur in microclusters or suddenly arriving groups of suspiciously similar edges e.g. denial of service attacks in network traffic data and lockstep behavior. However, existing methods which process edge streams in an online manner, including (Eswaran and Faloutsos 2018; Ranshous et al. 2016), aim to detect individually surprising edges, not microclusters, and can thus miss large amounts of suspicious activity.

In this work, we propose MIDAS, which detects microcluster anomalies, or suddenly arriving groups of suspiciously similar edges, in edge streams, using constant time and memory. In addition, by using a principled hypothesis testing framework, MIDAS provides theoretical bounds on the false positive probability, which these methods do not provide.

Our main contributions are as follows:
1. Streaming Microcluster Detection: We propose a novel streaming approach for detecting microcluster anomalies, requiring constant time and memory.
2. Theoretical Guarantees: In Theorem 1, we show guarantees on the false positive probability of MIDAS.
3. Effectiveness: Our experimental results show that MIDAS outperforms baseline approaches by 46%-52% accuracy (in terms of AUC), and processes the data $108 - 505$ times faster than baseline approaches.

Reproducibility: Our code and datasets are publicly available at https://github.com/bhatiasiddharth/MIDAS.

Related Work
In this section, we review previous approaches to detect anomalous signs on static and dynamic graphs. See (Akoglu, Tong, and Koutra 2015) for an extensive survey on graph-based anomaly detection.

Anomaly detection in static graphs can be classified by which anomalous entities (nodes, edges, subgraph, etc.) are spotted.

- Anomalous node detection: (Akoglu, McGlohon, and Faloutsos 2010) extracts egonet-based features and finds empirical patterns with respect to the features. Then, it identifies nodes whose egonets deviate from the patterns,
Let \( E = \{ e_1, e_2, \cdots \} \) be a stream of edges from a time-evolving graph \( G \). Each arriving edge is a tuple \( e_i = (u_i, v_i, t_i) \) consisting of a source node \( u_i \in V \), a destination node \( v_i \in V \), and a time of occurrence \( t_i \), which is the time at which the edge was added to the graph. For example, in a network traffic stream, an edge \( e_i \) could represent a connection made from a source IP address \( u_i \) to a destination IP address \( v_i \) at time \( t_i \). We do not assume that the set of vertices \( V \) is known a priori: for example, new IP addresses or user IDs may be created over the course of the stream.

We model \( G \) as a directed graph. Undirected graphs can simply be handled by treating an incoming undirected edge \( e_i \) as two simultaneous directed edges, one in either direction.

We also allow \( G \) to be a multigraph: edges can be created multiple times between the same pair of nodes. Edges are allowed to arrive simultaneously: i.e. \( t_{i+1} \geq t_i \), since in many applications \( t_i \) are given in the form of discrete time ticks.

The desired properties of our algorithm are as follows:

- **Microcluster Detection:** It should detect suddenly appearing bursts of activity which share many repeated nodes or edges, which we refer to as microclusters.

- **Guarantees on False Positive Probability:** Given any user-specified probability level \( \epsilon \) (e.g. 1%), the algorithm should be adjustable so as to provide false positive probability of at most \( \epsilon \) (e.g. by adjusting a threshold that depends on \( \epsilon \)). Moreover, while guarantees on the false positive probability rely on assumptions about the data distribution, we aim to make our assumptions as weak as possible.

- **Constant Memory and Update Time:** For scalability in the streaming setting, the algorithm should run in constant memory and constant update time per newly arriving edge. Thus, its memory usage and update time should not grow with the length of the stream, or the number of nodes in the graph.

### Problem

#### Anomaly detection in graph streams

Anomaly detection in graph streams use as input a series of graph snapshots over time. We categorize them similarly according to the type of anomaly detected:

- **Anomalous node detection:** (Sun, Tao, and Faloutsos 2013) detects nodes whose egonets suddenly and significantly change.

- **Anomalous subgraph detection:** (Shin et al. 2017) identifies dense subtensors based on edge occurrence, preferential attachment, and mutual neighbors.

- **Anomalous edge detection:** (Ranshous et al. 2016) encodes an input graph based on similar connectivity among nodes, then spots edges whose removal reduces the total encoding cost significantly. (Tong and Lin 2011) factorizes the adjacency matrix and flag edges with high reconstruction error as outliers.

#### Anomaly detection in edge streams

Anomaly detection in edge streams use as input a stream of edges over time. Categorizing them according to the type of anomaly detected:

- **Anomalous node detection:** Given an edge stream, (Yu et al. 2013) detects nodes whose egonets suddenly and significantly change.

- **Anomalous subgraph detection:** Given an edge stream, (Shin et al. 2017) identifies dense subtensors created within a short time.

- **Anomalous edge detection:** (Chakrabarti 2004) encodes an input graph based on similar connectivity among nodes, then spots edges whose removal reduces the total encoding cost significantly. (Eswaran and Faloutsos 2018) identifies edge anomalies in a network traffic stream, an edge \( e_i \) could represent a connection made from a source IP address \( u_i \) to a destination IP address \( v_i \) at time \( t_i \). We do not assume that the set of vertices \( V \) is known a priori: for example, new IP addresses or user IDs may be created over the course of the stream.

We model \( G \) as a directed graph. Undirected graphs can simply be handled by treating an incoming undirected edge \( e_i \) as two simultaneous directed edges, one in either direction.

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### Table 1: Comparison of relevant edge stream anomaly detection approaches
3. Incorporating Relations:

2. Detection and Guarantees:

1. Streaming Hypothesis Testing Approach: We describe our MIDAS algorithm, which uses streaming data structures within a hypothesis testing-based framework, allowing us to obtain guarantees on false positive probability.

Proposed Algorithm

Overview

Next, we describe our MIDAS and MIDAS-R approaches. The following provides an overview:

1. Streaming Hypothesis Testing Approach: We describe our MIDAS algorithm, which uses streaming data structures within a hypothesis testing-based framework, allowing us to obtain guarantees on false positive probability.

2. Detection and Guarantees: We describe our decision procedure for determining whether a point is anomalous, and our guarantees on false positive probability.

3. Incorporating Relations: We extend our approach to the MIDAS-R algorithm, which incorporates relationships between edges temporally and spatially.

MIDAS: Streaming Hypothesis Testing Approach

![Figure 1: Time series of a single source-destination pair (u, v), with a large burst of activity at time tick 10.](image)

Consider the example in Figure 1 of a single source-destination pair (u, v), which shows a large burst of activity at time 10. This burst is the simplest example of a micro-cluster, as it consists of a large group of edges which are very similar to one another (in fact identical), both spatially (i.e. in terms of the nodes they connect) and temporally.

Streaming Data Structures

In an offline setting, there are many time-series methods which could detect such bursts of activity. However, in an online setting, recall that we want memory usage to be bounded, so we cannot keep track of even a single such time series. Moreover, there are many such source-destination pairs, and the set of sources and destinations is not fixed a priori.

To circumvent these problems, we maintain two types of Count-Min-Sketch (CMS) (Cormode and Muthukrishnan 2005) data structures. Assume we are at a particular fixed time tick t in the stream; we treat time as a discrete variable for simplicity. Let \( s_{uv} \) be the total number of edges from u to v up to the current time. Then, we use a single CMS data structure to approximately maintain all such counts \( s_{uv} \) (for all edges \( uv \)) in constant memory: at any time, we can query the data structure to obtain an approximate count \( \hat{s}_{uv} \).

Secondly, let \( a_{uv} \) be the number of edges from u to v in the current time tick (but not including past time ticks). We keep track of \( a_{uv} \) using a similar CMS data structure, the only difference being that we reset this CMS data structure every time we transition to the next time tick. Hence, this CMS data structure provides approximate counts \( \hat{a}_{uv} \) for the number of edges from u to v in the current time tick \( t \).

Hypothesis Testing Framework

Given approximate counts \( s_{uv} \) and \( a_{uv} \), how can we detect microclusters? Moreover, how can we do this in a principled framework that allows for theoretical guarantees?

Fix a particular source and destination pair of nodes, \((u, v)\), as in Figure 1. One approach would be to assume that the time series in Figure 1 follows a particular generative model: for example, a Gaussian distribution. We could then find the mean and standard deviation of this Gaussian distribution. Then, at time \( t \), we could compute the Gaussian likelihood of the number of edge occurrences in the current time tick, and declare an anomaly if this likelihood is below a specified threshold.

However, this requires a restrictive Gaussian assumption, which can lead to excessive false positives or negatives if the data follows a very different distribution. Instead, we use a weaker assumption: that the mean level (i.e. the average rate at which edges appear) in the current time tick (e.g. \( t = 10 \)) is the same as the mean level before the current time tick (\( t < 10 \)). Note that this avoids assuming any particular distribution for each time tick, and also avoids a strict assumption of stationarity over time.

Hence, we can divide the past edges into two classes: the current time tick (\( t = 10 \)) and all past time ticks (\( t < 10 \)). Recalling our previous notation, the number of events at \( t = 10 \) is \( a_{uv} \), while the number of edges in past time ticks (\( t < 10 \)) is \( s_{uv} - a_{uv} \).

Under the chi-squared goodness-of-fit test, the chi-squared statistic is defined as the sum over categories of \( \frac{(\text{observed} - \text{expected})^2}{\text{expected}} \). In this case, our categories are \( t = 10 \) and \( t < 10 \). Under our mean level assumption, since we have \( s_{uv} \) total edges (for this source-destination pair), the expected number at \( t = 10 \) is \( \frac{2s_{uv}}{t} \), and the expected number for \( t < 10 \) is the remaining, i.e. \( \frac{t-1}{t}s_{uv} \). Thus the chi-squared statistic is:

\[
X^2 = \frac{(\text{observed} - \text{expected})^2}{\text{expected}} = \frac{(a_{uv} - \frac{s_{uv}}{t})^2}{\frac{2s_{uv}}{t}} + \frac{(s_{uv} - a_{uv})^2}{\frac{t-1}{t}s_{uv}}
\]

\[
= (a_{uv} - \frac{s_{uv}}{t})^2 + (s_{uv} - a_{uv})^2
\]

\[
= (a_{uv} - \frac{s_{uv}}{t})^2 + \frac{t-1}{t}s_{uv}
\]

\[
= (a_{uv} - \frac{s_{uv}}{t})^2 \frac{t^2}{s_{uv}(t-1)}
\]

---

We use ‘spatially’ in a graph sense, i.e. connecting nearby nodes, not to refer to any other continuous spatial dimension.
Note that both \( a_{uv} \) and \( s_{uv} \) can be estimated by our CMS data structures, obtaining approximations \( \hat{a}_{uv} \) and \( \hat{s}_{uv} \) respectively. This leads to our following anomaly score, using which we can evaluate a newly arriving edge with source-destination pair \((u,v)\):

**Definition 1 (Anomaly Score).** Given a newly arriving edge \((u,v,t)\), our anomaly score is computed as:

\[
score((u,v,t)) = (a_{uv} - \frac{s_{uv}}{t})^2 s_{uv}(t-1) \tag{1}
\]

Algorithm 1 summarizes our MIDAS algorithm.

**Algorithm 1: MIDAS: Streaming Anomaly Scoring**

**Input:** Stream of graph edges over time

**Output:** Anomaly scores per edge

1. **Initialize CMS data structures:**
2. Initialize CMS for total count \( s_{uv} \) and current count \( a_{uv} \)
3. while new edge \( e = (u,v,t) \) is received: do
   4. **Update Counts:**
      5. Update CMS data structures for the new edge \( uv \)
   6. **Query Counts:**
      7. Retrieve updated counts \( \hat{s}_{uv} \) and \( \hat{a}_{uv} \)
   8. **Anomaly Score:**
      9. output score\((u,v,t)\) = \((a_{uv} - \frac{\hat{s}_{uv}}{t})^2 s_{uv}(t-1)\)

**Detection and Guarantees**

While Algorithm 1 computes an anomaly score for each edge, it does not provide a binary decision for whether an edge is anomalous or not. We want a decision procedure that provides binary decisions and a guarantee on the false positive probability: i.e. given a user-defined threshold \( \epsilon \), the probability of a false positive should be at most \( \epsilon \). Intuitively, the key idea is to combine the approximation guarantees of CMS data structures with properties of a chi-squared random variable.

The key property of CMS data structures we use is that given any \( \epsilon \) and \( \nu \), for appropriately chosen CMS data structures, with probability at least \( 1 - \frac{\epsilon}{2} \), the estimates \( a_{uv} \) satisfy:

\[
a_{uv} \le a_{uv} + \nu \cdot N_t \tag{2}
\]

where \( N_t \) is the total number of edges at time \( t \). Since CMS data structures can only overestimate the true counts, we additionally have:

\[
s_{uv} \le \hat{s}_{uv} \tag{3}
\]

Define an adjusted version of our earlier score:

\[
\hat{a}_{uv} = a_{uv} - \nu N_t \tag{4}
\]

To obtain its probabilistic guarantee, our decision procedure computes \( \hat{a}_{uv} \), and uses it to compute an adjusted version of our earlier statistic:

\[
\hat{X}^2 = (\hat{a}_{uv} - \frac{\hat{s}_{uv}}{t})^2 s_{uv}(t-1) \tag{5}
\]

Then our main guarantee is as follows:

**Theorem 1** (False Positive Probability Bound). Let \( \chi_{1 - \epsilon/2}^2(1) \) be the \( 1 - \epsilon/2 \) quantile of a chi-squared random variable with 1 degree of freedom. Then:

\[
P(\hat{X}^2 > \chi_{1 - \epsilon/2}^2(1)) < \epsilon \tag{6}
\]

In other words, using \( \hat{X}^2 \) as our test statistic and threshold \( \chi_{1 - \epsilon/2}^2(1) \) results in a false positive probability of at most \( \epsilon \).

**Proof.** Recall that

\[
X^2 = (a_{uv} - \frac{s_{uv}}{t})^2 s_{uv}(t-1) \tag{7}
\]

was defined so that it has a chi-squared distribution. Thus:

\[
P(X^2 \le \chi_{1 - \epsilon/2}^2(1)) \ge 1 - \epsilon/2 \tag{8}
\]

At the same time, by the CMS guarantees we have:

\[
P(a_{uv} \le a_{uv} + \nu \cdot N_t) \le 1 - \epsilon/2 \tag{9}
\]

By union bound, with probability at least \( 1 - \epsilon \), both these events (8) and (9) hold, in which case:

\[
\hat{X}^2 = (\hat{a}_{uv} - \frac{\hat{s}_{uv}}{t})^2 s_{uv}(t-1)
\]

\[
= (a_{uv} - \nu N_t - \frac{s_{uv}}{t})^2 s_{uv}(t-1)
\]

\[
\le (a_{uv} - \frac{s_{uv}}{t})^2 s_{uv}(t-1)
\]

Finally, we conclude that

\[
P(\hat{X}^2 > \chi_{1 - \epsilon/2}^2(1)) < \epsilon. \tag{10}
\]

**Incorporating Relations**

In this section, we describe our MIDAS-R approach, which considers edges in a relational manner: that is, it aims to group together edges which are nearby, either temporally or spatially.

**Temporal Relations** Rather than just counting edges in the same time tick (as we do in MIDAS), we want to allow for some temporal flexibility: i.e. edges in the recent past should also count toward the current time tick, but modified by a reduced weight. A simple and efficient way to do this using our CMS data structures is as follows: at the end of every time tick, rather than resetting our CMS data structures \( a_{uv} \), we reduce all its counts by a fixed fraction \( \alpha \in (0, 1) \). This allows past edges to count toward the current time tick, with a diminishing weight.
Spatial Relations We would like to catch large groups of spatially nearby edges: e.g. a single source IP address suddenly creating a large number of edges to many destinations, or a small group of nodes suddenly creating an abnormally large number of edges between them. A simple intuition we use is that in either of these two cases, we expect to observe nodes with a sudden appearance of a large number of edges. Hence, we can use CMS data structures to keep track of edge counts like before, except counting all edges adjacent to any node. Specifically, we create CMS counters \( \hat{a}_u \) and \( \hat{s}_u \) to approximate the current and total edge counts adjacent to node \( u \). Given each incoming edge \((u, v, t)\), we can then compute three anomalousness scores: one for edge \((u, v)\), as in our previous algorithm; one for node \( u \), and one for node \( v \). Finally, we combine the three scores by taking their maximum value. Another possibility of aggregating the three scores is to take their sum. Algorithm 2 summarizes the resulting MIDAS-R algorithm.

Algorithm 2: MIDAS-R: Incorporating Relations

```
Input: Stream of graph edges over time
Output: Anomaly scores per edge
1  \( \triangleright \) Initialize CMS data structures:
2      Initialize CMS for total count \( s_{uv} \) and current count \( a_{uv} \)
3      Initialize CMS for total count \( s_u \) and current count \( a_u \)
4  while new edge \((u, v, t)\) is received: do
5      \( \triangleright \) Update Counts:
6          Update CMS data structures for the new edge \((u, v)\)
7          Retrieve updated counts \( s'_{uv} \) and \( a'_{uv} \)
8          Retrieve updated counts \( \hat{s}_u, \hat{s}_v, \hat{a}_u, \hat{a}_v \)
9      \( \triangleright \) Compute Edge Scores:
10         \( \text{score}(u, v, t) = (a_{uv} - \frac{s_{uv}}{t})^2 \frac{t^2}{s_{uv}(t-1)} \)
11      \( \triangleright \) Compute Node Scores:
12         \( \text{score}(u, t) = (\hat{a}_u - \frac{s_u}{t})^2 \frac{t^2}{s_u(t-1)} \)
13         \( \text{score}(v, t) = (\hat{a}_v - \frac{s_v}{t})^2 \frac{t^2}{s_v(t-1)} \)
14      \( \triangleright \) Final Node Scores:
15         output \( \max\{\text{score}(u, v, t), \text{score}(u, t), \text{score}(v, t)\} \)
```

Time and Memory Complexity

In terms of memory, both MIDAS and MIDAS-R only need to maintain the CMS data structures over time, which are proportional to \( O(wb) \), where \( w \) and \( b \) are the number of hash functions and the number of buckets in the CMS data structures; which is bounded with respect to the data size.

For time complexity, the only relevant steps in Algorithm 1 and 2 are those that either update or query the CMS data structures, which take \( O(w) \) (all other operations run in constant time). Thus, time complexity per update step is \( O(w) \).

Experiments

In this section, we evaluate the performance of MIDAS and MIDAS-R compared to SEDANSPOT on dynamic graphs. We aim to answer the following questions:

Q1. Accuracy: How accurately does MIDAS detect real-world anomalies compared to baselines, as evaluated using the ground truth labels?

Q2. Scalability: How does it scale with input stream length? How does the time needed to process each input compare to baseline approaches?

Q3. Real-World Effectiveness: Does it detect meaningful anomalies in case studies on Twitter graphs?

Datasets: DARPA (Lippmann et al. 1999) has 4.5M IP-IP communications between 9.4K source IP and 2.3K destination IP over 87.7K minutes. Each communication is a directed edge (srcIP, dstIP, timestamp, attack) where the ground truth attack label indicates whether the communication is an attack or not (anomalies are 23.8% of total).

TwitterWorldCup (Rayana and Akoglu 2015; 2016) has 2.6M tweet samples for four months (May-Aug 2014) containing Department of Homeland Security keywords related to terrorism or domestic security. Entity-entity co-mention temporal graphs are built on daily basis (80 time ticks).

TwitterSecurity (Rayana and Akoglu 2015; 2016) has 1.7M tweet samples for the World Cup 2014 season (June 12-July 13). The tweets are filtered by popular/official World Cup hashtags, such as #worldcup, #fifa, #brazil, etc. Similar to TwitterSecurity, entity-entity co-mention temporal graphs are constructed on 5 minute sample rate (8640 time points).

Baseline: As described in our Related Work, only RHSS and SEDANSPOT operate on edge streams and provide a score for each edge. SEDANSPOT uses personalised PageRank to detect anomalies in sublinear space and constant time per edge. However, RHSS was evaluated in (Eswaran and Faloutsos 2018) on the DARPA dataset and found to have AUC of 0.17 (lower than chance). Hence, we only compare with SEDANSPOT.

Evaluation Metrics: All the methods output an anomaly score per edge (higher is more anomalous). We calculate the True Positive Rate (TPR) and False Positive Rate (FPR) and plot the ROC curve (TPR vs FPR). We also report the Area under the ROC curve (AUC) and Average Precision Score.

Experimental Setup

All experiments are carried out on a 2.7GH z Intel Core i5 processor, 16GB RAM, running OS X 10.14.6. We implement MIDAS and MIDAS-R in C++. We use 2 hash functions for the CMS data structures, and we set the number of CMS buckets to 2719 to result in an approximation error of \( \nu = 0.001 \). For MIDAS-R, we set the temporal decay factor \( \alpha = 0.5 \). We used an open-sourced implementation of SEDANSPOT, provided by the authors, following parameter settings as suggested in the original paper (sample size 500).

Q1. Accuracy: Figure 2 plots the ROC curve for MIDAS-R, MIDAS and SEDANSPOT. Figure 3(top) plots accuracy (AUC) vs. running time (log scale, in seconds, excluding I/O). We see that
MIDAS achieves a much higher accuracy (= 0.94) compared to the baseline (= 0.64), while also running significantly faster (0.31s vs. 156s). This is a 46% accuracy improvement at 505× faster speed. MIDAS-R achieves the highest accuracy (= 0.977) which is 52% accuracy improvement compared to the baseline at 163× faster speed.

Figure 3(bottom) plots the average precision score vs. running time. We see that MIDAS is more precise (= 0.969) compared to the baseline (= 0.751). This is a 29% precision improvement. MIDAS-R achieves the highest average precision score (= 0.987) which is 31% more precise than SEDAN SPOT.

We see that MIDAS and MIDAS-R greatly outperform SEDAN SPOT on both accuracy and precision metrics.

Q2. Scalability

Figure 4 shows the scalability of MIDAS and MIDAS-R. We plot the wall-clock time needed to run on the (chronologically) first $2^{12}$, $2^{13}$, $2^{14}$, ..., $2^{22}$ edges of the DARPA dataset. This confirms the linear scalability of MIDAS and MIDAS-R with respect to the number of edges in the input dynamic graph due to its constant processing time per edge. Note that both MIDAS and MIDAS-R process $4M$ edges within 1 second, allowing real-time anomaly detection.

Figure 5 plots the number of edges (in millions) and time to process each edge for DARPA dataset. MIDAS processes 2.38M edges within 1μs each and 1.77M edges within 2μs each. MIDAS-R processes 1.04M edges within 1μs each and 2.24M edges within 2μs each.

Table 2 shows the time it takes SEDAN SPOT, MIDAS and MIDAS-R to run on the TwitterWorldCup, TwitterSecurity and DARPA datasets. For TwitterWorldCup dataset, we see that MIDAS-R is 108× faster than SEDAN SPOT (0.48s vs. 52.17s) and MIDAS is 306× faster than SEDAN SPOT (0.17s vs 52.17s). For TwitterSecurity dataset, we see that MIDAS-R is 112× faster than SEDAN SPOT (0.68s vs. 76.6s) and MIDAS is 283× faster than SEDAN SPOT (0.27s vs 76.6s). For the DARPA dataset, we see that MIDAS-R is 163× faster

SEDAN SPOT requires several subprocesses (hashing, random-walking, reordering, sampling, etc), resulting in the large computation time. MIDAS and MIDAS-R are both both scalable and fast.
Q3. Real-World Effectiveness

We measure anomaly scores using MIDAS, MIDAS-R and SEDAN SPOT on the TwitterSecurity dataset. Figure 6 plots anomaly scores vs. day (during the four months of 2014). To visualise, we aggregate edges occurring in each day by taking the max anomalousness score per day, for a total of 90 days. Anomalies correspond to major world news such as Mpeketoni attack (Event 6) or Soma Mine explosion (Event 1). MIDAS and MIDAS-R show similar trends whereas SEDAN SPOT misses some anomalous events (Events 2, 7), and outputs many high scores unrelated to any true events. This is also reflected in the low accuracy and precision of SEDAN SPOT in Figure 3. The anomalies detected by MIDAS and MIDAS-R coincide with major events in the TwitterSecurity timeline as follows:

1. 13-05-2014. Turkey Mine Accident, Hundreds Dead
   03-06-14. Suicide bombing
4. 09-06-14. Suicide/Truck bombings.
5. 10-06-2014. Iraqi Militants Seized Large Regions.
   11-06-2014. Kidnapping
7. 26-06-14. Suicide Bombing/Shootout/Raid
9. 18-07-14. Airplane with 298 Onboard was Shot Down over Ukraine.

This shows the effectiveness of MIDAS and MIDAS-R for catching real-world anomalies.

**Microcluster anomalies:** Figure 7 corresponds to Event 7 in the TwitterSecurity dataset. All single edges are equivalent to 444 edges and double edges are equivalent to 888 edges between the nodes. This suddenly arriving (within 1 day) group of suspiciously similar edges is an example of a microcluster anomaly which MIDAS-R detects, but SEDAN SPOT misses.

In this paper, we proposed MIDAS and MIDAS-R for microcluster based detection of anomalies in edge streams. Future work could consider more general types of data, including heterogeneous graphs or tensors. Our contributions are as follows:

1. **Streaming Microcluster Detection:** We propose a novel streaming approach for detecting microcluster anomalies, requiring constant time and memory.
2. **Theoretical Guarantees:** In Theorem 1, we show guarantees on the false positive probability of MIDAS.
3. Effectiveness: Our experimental results show that MIDAS outperforms baseline approaches by 46%-52% accuracy (in terms of AUC), and processes the data 108−505 times faster than baseline approaches.

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