Fuzzy-Classification Assisted Solution Preselection in Evolutionary Optimization

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Abstract

In evolutionary optimization, the preselection is an efficient operator to improve the search efficiency, which aims to filter unpromising candidate solutions before fitness evaluation. Most existing preselection operators rely on fitness values, surrogate models, or classification models. Basically, the classification based preselection regards the preselection as a classification procedure, i.e., differentiating promising and unpromising candidate solutions. However, the difference between promising and unpromising classes becomes fuzzy as the running process goes on, as all the left solutions are likely to be promising ones. Facing this challenge, this paper proposes a fuzzy classification based preselection (FCPS) scheme, which utilizes the membership function to measure the quality of candidate solutions. The proposed FCPS scheme is applied to two state-of-the-art evolutionary algorithms on a test suite. The experimental results show the potential of FCPS on improving algorithm performance.

Introduction

Sophisticated optimization problems are faced in a variety of real-world applications, and are arisen from scientific to engineering areas (Polak 1997). Generally, an optimization problem can be formulated as:

$$\min_{x \in \Omega} f(x) \quad (1)$$

where $x = (x_1, \cdots, x_n)^T$ is a decision variable vector, $\Omega = \prod_{i=1}^{n} [a_i, b_i]$ defines the feasible region of the search space, and $f : \mathbb{R}^n \to \mathbb{R}$ denotes the objective function.

When optimization problems are friendly, i.e., the objective and/or constraints are linear or convex, the linear programming or convex optimization methods are of great interests (Polak 1997). However real-world applications are usually more complicated where the objective and/or constraints might be nonlinear, non-convex or even without closed forms (Szu 1986; Yuille and Rangarajan 2002). For these problems, traditional optimization methods may become inefficient, or even fail to work. To this end, derivative-free or heuristic optimization methods, which do not make strong assumptions about the problems to optimize, have attracted much attention (Wang et al. 2013; Mallipeddi and Suganthan 2014; Qian, Yu, and Zhou 2015). Among them, the evolutionary algorithms (EAs) (Back, Fogel, and Michalewicz 1997) is a kind of promising one, which includes genetic algorithms (GAs), particle swarm optimization (PSO), differential evolution (DE) (Das and Suganthan 2011), estimation of distribution algorithms (EDAs) (Larraaga and Lozano 2001), to name a few. Evolutionary optimization method is a kind of population based iterative heuristic optimization paradigm that uses a population of solutions to approximate the optimum of (1).

As a kind of fitness value driven method, EAs do not use the (approximated) derivatives to generate candidate solutions. Instead, they sample candidate solutions by using the current solutions, evaluate the candidate solutions, and select promising ones into the next generation. Therefore, the selection operations play an vital role in EAs. Generally, there are three types of selection, i.e. the mating selection, the preselection, and the environmental selection. The mating selection chooses parent solutions for sampling candidate solutions. The environmental selection chooses the promising solutions to the next generation. Preselection may have different meanings (Mahfoud 1992), and it refers to select promising ones from a set of candidate solutions in this paper.

In evolutionary optimization, the preselection operator can help to improve algorithm performance significantly if it is correctly used (Emmerich et al. 2002; Jin 2011), in which case the unpromising candidate solutions can be discarded before the fitness evaluations and thus the computational resources can be saved. A key issue with preselection is on how to measure qualities of candidate solutions, i.e., to judge whether a candidate solution is promising or not. According to the quality measurement, the preselection operators can be roughly classified into three categories: (1) fitness based approaches (Wang, Cai, and Zhang 2011; Li, Zhou, and Zhang 2014), (2) surrogate model based approaches (Jin 2003; 2011; Chen, Xie, and Zou 2013), and (3) classification based approaches (Lu, Tang, and Yao 2011; Lu and Tang 2012; Yu, Qian, and Hu 2016; Hu, Qian, and Yu. 2017; Zhang, Zhou, and Zhang 2018; Wang, Qian, and Yu 2018).

Classification based preselection (CPS) (Zhang, Zhou, and Zhang 2018) regards the selection as a classification
procedure, where the chosen candidate solutions belong to the ‘promising’ class, and the discarded ones to the ‘unpromising’ class. In this approach, the visited solutions are used to build a classification model and to predict the qualities, i.e., ‘promising’ or ‘unpromising’, of the candidate solutions, instead of fitness values as done by the fitness and surrogate model based approaches, and the promising ones are then chosen out. Therefore, this approach might be more natural in evolutionary optimization. By using a binary classification model (Zhang, Zhou, and Zhang 2018), CPS, which actually is a binary-class classification based preselection (BCPS), needs to prepare a training data set with two classes. However, in EAs, after several generations, all left solutions in the current population are likely to be promising ones, and the gap between the promising solutions and the unpromising ones will become unclear and fuzzy. In the community of classification, there exits a type of so called fuzzy classification methods (Keller, Gray, and Givens 1985; Derrac, Garcia, and Herrera 2014), which usually judge the data quality according to the membership function (Klir and Yuan 1995) when the features of the data are fuzzy. Thus applying the fuzzy classification models to assist the preselection procedure might be more suitable than the binary classification models.

Following this idea, this paper proposes a fuzzy classification based preselection (FCPS) strategy for evolutionary optimization. For a FCPS assisted EA, a fuzzy classification model is built firstly according to the current solutions. Then for each parent solution, a set of candidate solutions are sampled by the variation operator. Finally for each parent solution, a candidate solution with the maximal fuzzy membership degree to the ‘promising’ class is chosen for fitness evaluation. The major contributions are as follows.

- The fuzzy classification model is introduced to assist the preselection, named as FCPS, in evolutionary optimization.
- The FCPS strategy is applied to two state-of-the-art EAs, and the experimental studies demonstrate its advantages.

The rest of the paper is organized as follows. The next section presents the basic idea of the FCPS strategy, and introduces the FCPS assisted EA framework. After that, CPS assisted EAs are empirically studied on some test instances (Yao, Liu, and Lin 1999). Finally, the paper is concluded with some marks for future work.

Fuzzy Classification based Preselection

This section introduces the three main components, i.e., training set definition, model building, and candidate solution labeling and selection, when implementing FCPS and a general EA framework with FCPS.

Training Set Definition

In current population, each solution \( x \) is with an objective value (fitness) \( f(x) \). In classification, each training sample \( x \), i.e., the solution in our case, is with a label \( l \). Therefore, it needs to assign each solution \( x \) a label \( l \in \{+1, -1\} \). where +1 denotes a ‘promising’ sample and −1 denotes a ‘unpromising’ sample. By this way, the current population will be partitioned into two training classes.

This paper uses the following training set definition strategies (Zhang, Zhou, and Zhang 2018), which are also illustrated in Figure 1.

- **Mean fitness separation (MS):** the solutions with the objective values less than the mean fitness value, are assigned label +1, and the others are assigned label −1.
- **First quartile fitness separation (\( Q_{1/4} \)):** the best 25% solutions are assigned label +1, and the others are assigned label −1.
- **Median fitness separation (\( Q_{1/2} \)):** the best 50% solutions are assigned label +1, and the other ones are assigned label −1.
- **Third quartile fitness separation (\( Q_{3/4} \)):** the best 75% solutions are assigned label +1, and the others are assigned label −1.

Model Building

Fuzzy classification (Derrac, Garcia, and Herrera 2014) is a fuzzy rule-based classification model. In real world applications, a large number of concepts may generally not be described precisely, and in some situations, it does not need to accurately describe the relevant concepts of things. Based on such observations, Zadeh proposed fuzzy mathematics based on fuzzy set theory in 1965 (Zadeh 1965; Zadeh, Klir, and Yuan 1996). As one of the popular methods in fuzzy mathematics field, fuzzy classification is often applied in a fuzzy environment by using precise methods to model and classify imprecise and vague data.

As with many other fuzzy mathematics methods, fuzzy membership function (Klir and Yuan 1995) is used in the fuzzy classification to facilitate classification process in a fuzzy manner. The membership function is defined by the true value of the fuzzy function (Klir and Yuan 1995), indicating the membership degree of the data that is to be classified belonging to a certain category. According to the fuzzy membership degree, the fuzzy classification groups the data with the same characteristics into fuzzy sets. In other words, the determination of the membership function reveals the result of the fuzzy classification. In addition, the membership function is related to each particular practical problem,
which is required to be constructed given the actual problem at hand.

Let

\[ m = Fclass(x) \]

denote a fuzzy classification model for a binary classification problem, where \( x \) is a feature vector, and \( m = (m_1, m_2) \) is the membership degree vector that belongs to the two classes.

Some commonly used fuzzy classification models are based on neural networks, K nearest neighbors (KNN), etc. (Keller, Gray, and Givens 1985; Derrac, Garcia, and Herrera 2014). This paper uses the fuzzy KNN (FKNN) to do classification, which uses the fuzzy similarity rather than the distance in original KNN to do classification (Derrac, Garcia, and Herrera 2014).

**Candidate Solution Labeling and Selection**

In FCPS, for each parent solution \( X = \{x_1, x_2, \cdots, x_N\} \), \( M \) candidate solutions, \( Y = \{y_1, y_2, \cdots, y_M\} \), are sampled. The candidate solution with the maximal membership degree belongs to ‘promising’ class is chosen.

**Experimental Study**

The proposed FCPS strategy is integrated into two state-of-the-art evolutionary optimization algorithms, i.e., the composite differential evolution (CoDE) (Wang, Cai, and Zhang 2011) and the hybrid estimation of distribution algorithm with cheap and expensive local search (EDA/LS) (Zhou, Sun, and Zhang 2015) to study its performance.

**CoDE** CoDE (Wang, Cai, and Zhang 2011) is a multioperator based DE. It utilizes three mutation schemes, i.e., “DE/rand/1/bin”, “DE/rand/2/bin”, and “current-to-rand/1”, along with three groups of control parameters in candidate solution generation. In each generation, three combinations of mutation and parameter are used to generate three candidate solutions for each parent, and the one with best fitness value is chosen as the real offspring solution. The details of the algorithm are referred to (Wang, Cai, and Zhang 2011).

**EDA/LS** EDA/LS (Zhou, Sun, and Zhang 2015) is a hybrid EDA that employs both cheap and expensive local search methods. Its basic idea is to use both global statistical information and individual location information for solution generation. The details of the algorithm are referred to (Zhou, Sun, and Zhang 2015).
Table 1: Statistical results for the median, mean and standard deviation values of the results obtained by CoDE, EDA/LS, and their variants on $f_1$-$f_{13}$ after 300,000 FES over 30 independent runs.

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</tbody>
</table>

Figure 2: The mean function value of the best individuals obtained by CoDE and its variants versus FES on 4 instances over 30 independent runs.

Figure 3: Bar plots of the median FES obtained by EDA/LS and its variants when achieve the same values on 4 instances over 30 independent runs.

2406
Experimental Settings
The first 13 benchmark functions from the YLL test suite (Yao, Liu, and Lin 1999) are employed for empirical study. Among the test problems, $f_1\sim f_3$ are unimodal, $f_5$ is unimodal when $n = 2$ and $n = 3$, and is multimodal when $n > 3$, $f_6$ is a step function, $f_7$ is with white noise, and $f_8\sim f_{13}$ are multimodal. All the test instances have an optimal objective value 0. The definitions of these functions are referred to (Yao, Liu, and Lin 1999).

The variable dimensions are $n = 30$ for all instances. The population size is $N = 150$ for EDA/LS and its variants, and $N = 30$ for CoDE and its variants. The stop condition is fitness evaluations (FES) = 300,000 for all of the algorithms. Each algorithm is executed on each test instance for 30 independent runs. For FCPS based approaches, the number of candidate solutions is $M = 4$. The other control parameters are the same as in the original algorithms (Zhou, Sun, and Zhang 2015; Wang, Cai, and Zhang 2011).

In the experiments, FCPS is also compared with BCPS. As suggested in (Zhang, Zhou, and Zhang 2018), the classification and regression trees (CART) based BCPS approach performs better than other binary classification models, besides K nearest neighbor (KNN). Thus, in this paper in order to evidence the efficiency of FCPS model, the CART model is employed. The MS strategy is used for training set definition.

In the following subsections, CoDE and EDA/LS, their variants with FCPS, i.e., FCPS-CoDE and FCPS-EDA/LS, and their variants with BCPS (Zhang, Zhou, and Zhang 2018), i.e., BCPS-CoDE and BCPS-EDA/LS, are empirically studied.

The Wilcoxon rank sum test is used to compare the experimental results, where “+”, “−”, or “∼” in the tables indicate the value obtained by an algorithm is smaller than, greater than, or similar to that obtained by its FCPS based version at 95% significance level. The value in the brackets denote the corresponding rank value in the tables.

Experimental Results
Table 1 summarizes the median, mean and standard deviation of the results obtained by CoDE, EDA/LS and their variants on the 13 YLL test instances after 300,000 FES over 30 runs respectively. Table 2 records the rank values obtained by the algorithms. The experimental results are summarized as follows.

CoDE and its variants: The results in Table 1 suggest that on $f_1\sim f_4$, $f_7$, FCPS-CoDE performs better than CoDE; on $f_6$, and $f_8\sim f_{13}$, the two algorithms obtain similar results; and on $f_5$, $f_9$, FCPS-CoDE performs worse than CoDE. On $f_1\sim f_4$, $f_7$, FCPS-CoDE performs better than BCPS-CoDE; on $f_5$ and $f_9$, BCPS-CoDE outperforms FCPS-CoDE; and on other 6 instances, the two algorithms obtain similar results.

EDA/LS and its variants: The results in Table 1 suggest that on $f_3$, $f_5$, $f_6$, and $f_8\sim f_{13}$, FCPS-EDA/LS, BCPS-EDA/LS, and EDA/LS obtain similar results; and on $f_1$, $f_2$, $f_4$, $f_7$, FCPS-EDA/LS gets the best results. The Wilcoxon rank sum test also shows that on most of the instances, the FCPS variant works no worse than the original algorithms and the corresponding BCPS variants. The rank values in Table 2 also suggest that according to both the median value and the mean value, the FCPS variants of CoDE and EDA/LS always achieve the best mean rank values.

Figure 2 plots the run time performance of FCPS-CoDE, BCPS-CoDE and CoDE on four test instances. It shows that on $f_1, f_7, f_{10}$ FCPS-CoDE in red curve converges faster than BCPS-CoDE and CoDE. On $f_5$, BCPS-CoDE is the fastest one.

Figure 3 plots the median FES obtained by FCPS-EDA/LS, BCPS-EDA/LS and EDA/LS when achieve the same values on four representative test instances $f_1, f_5, f_7, f_{10}$. The figure suggests on all of the test instances FCPS-EDA/LS always uses the smallest numbers of FES to achieve the fitness values.

The above results indicate that the FCPS assisted approaches work no worse than the original algorithms and the BCPS based approaches on most of the 13 test instances. This also suggests that FCPS could be regarded as a general strategy to improve the performances of existing EAs.

Influence of Training Set Definition Strategies
This section studies the 4 training data set definition strategies. In this study, CoDE is chosen as the basic optimizer in the experiments.

The statistical results for FCPS-CoDE with the 4 training set definition strategies on 4 test instances over 30 independent runs are shown in Figure 4.

Figure 4 shows FCPS-CoDE with Q1S, Q2S, and Q2S perform similarly and are worse than FCPS-CoDE with MS. This suggests that the population can be stably partitioned into two classes by the mean objective value of the current population. The reason might be that MS is statistically more stable than the other three strategies. To this end, the MS strategy might be a promising choice.

Comparison between FCPS and BCPS Strategies
This section investigates why the fuzzy classification model works better than the binary classification model. The following experiment is conducted. For a given population, both FKNN and CART models are built, then the models are used to predict the quality of the newly generated candidate solutions, and finally an offspring solution is chosen according to each of the model. The two offspring solutions are compared according to the real function values, and the number of win solutions achieved by the FKNN model
Figure 4: The run time performance of FCPS-CoDE with 4 training set definition strategies on 4 instances over 30 independent runs.

Table 3: The median, mean, max, min of win numbers obtained by FKNN-CoDE comparing to those of CART-CoDE in each generation.

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Figure 5: The mean runtime performance of FCPS, SVM, GP, RBF, Btree assisted CoDE on 4 instances.

Table 4: The statistical results obtained by FCPS, SVM, GP, RBF, and Btree assisted CoDE on f_1 – f_{13}.

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The figure presents that on SVM, GP, Btree, RBF assisted CoDE on 4 test instances. The rank values in Table 4 suggest that FCPS and Btree assisted CoDE achieve the best mean rank value.

<table>
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From Table 3, it can be seen that 16.67%-100.00% offspring solutions chosen by the FKNN model are better than those chosen by the CART model, and on the contrary, only 0.00%-83.33% offspring solutions chosen by the CART model are better than those chosen by the FKNN model. The median and mean values are quite consistent. According to the mean values, 50%-96.67% offspring solutions chosen by the FKNN model are better than those chosen by the CART model. It is clear that except f7, in over 97% generations, more than 50.00% offspring solutions chosen by the FKNN model are better than those chosen by the CART model on all the other test instances. This suggests that the FKNN performs better than CART on choosing offspring solutions.

**Comparison between Fuzzy Classification and Surrogate Models**

This section compares FCPS and surrogate model based preselection (SPS) assisted CoDE. The surrogate model employed in this section are SVM, GP, Btree, RBF. For simplicity, the name of the model is directly used to represent CoDE with the corresponding strategy.

Table 4 summarizes the median results obtained by FCPS, SVM, GP, Btree, RBF assisted CoDE on the 13 YLL test instances after 300,000 FES over 30 independent runs respectively.

The rank values in Table 4 suggest that FCPS and Btree assisted CoDE achieve the best mean rank value.

Figure 5 plots the mean run time performance of FCPS, SVM, GP, Btree, RBF assisted CoDE on 4 test instances. The figure presents that on f1, f10, FCPS assisted CoDE in red curve converges faster than the others, and the Btree assisted CoDE performs the second best. On f5, Btree assisted CoDE performs the best, and on f7, GP assisted CoDE is faster than the others, and FCPS and Btree assisted CoDE perform similarly. Thus it can be concluded that FCPS assisted CoDE outperforms the surrogate model assisted CoDE. And for the surrogate models, the Btree model is the best one.

In order to investigate why the fuzzy classification model works better than the surrogate model, the following experiment is conducted. For a given population, both FKNN and Btree models are built, then the models are used to predict the quality of the newly generated candidate solutions, and finally an offspring solution is chosen according to each of the models. The two offspring solutions are compared according to the real function values, and the number of win solutions achieved by the FKNN model is recorded. This comparison is applied to each generation. The test instances f1 – f13 are chosen to do the experiment. The population size is 30. The experimental results are shown in Table 5.

From Table 5, it can be seen that 16.67%-100.00% offspring solutions chosen by the FKNN model are better than those chosen by the Btree model, and on the contrary, only 0.00%-83.33% offspring solutions chosen by the Btree model are better than those chosen by the FKNN model. The median and mean values are quite consistent. According to the mean values, 53.33%-96.67% offspring solutions chosen by the FKNN model are better than those chosen by the Btree model. It is also clear that except f7, in over 91.00% generations, more than 50.00% offspring solutions chosen by the FKNN model are better than those chosen by the Btree model on all the other test instances. This suggests the FKNN performs better than Btree on choosing offspring solutions. It can also be concluded that FCPS can significantly improve the performance of EAs than surrogate models.

**Conclusions**

This paper proposed a fuzzy classification based preselection (FCPS) strategy for evolutionary optimization. FCPS applies a fuzzy classification model instead of a binary classification model to assist preselection. To apply FCPS in EAs, firstly a fuzzy classification model is built according to the current solutions that belong to the 'promising' and 'unpromising' training data sets. Then, for each parent solution, a set of candidate solutions are sampled by the variation operator. Finally, a solution belongs to the 'promising' class with maximal membership degree according to the fuzzy classification model is chosen as the offspring solution.

FCPS is applied to two state-of-the-art algorithms, i.e., CoDE (Wang, Cai, and Zhang 2011), EDA/LS (Zhou, Sun, and Zhang 2015), and studied on 13 YLL test instances (Yao, Liu, and Lin 1999). The CART based BCPS scheme is also employed for comparison study. The experimental results suggest that on most cases, the FCPS based approach works better than the BCPS based approach and the original algorithm. Some more discussions have also

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1The number of win solutions achieved by CART-CoDE equals to the population size minus that achieved by FKNN-CoDE.

2The number of win solutions achieved by Btree-CoDE equals to the population size minus that achieved by FKNN-CoDE.
proved that the fuzzy classification model is more efficient than the CART model and surrogate model on prediction in evolutionary optimization.

Some future work to improve the performance of FCPS-EA could be in following ways: (a) find a more proper way to combine fuzzy classification with EAs, and (b) reduce the computational cost in fuzzy classification building.

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References


