Improving Robustness for Joint Optimization of Camera Poses and Decomposed Low-Rank Tensorial Radiance Fields

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Abstract

In this paper, we propose an algorithm that allows joint refinement of camera pose and scene geometry represented by decomposed low-rank tensor, using only 2D images as supervision. First, we conduct a pilot study based on a 1D signal and relate our findings to 3D scenarios, where the naive joint pose optimization on voxel-based NeRFs can easily lead to suboptimal solutions. Moreover, based on the analysis of the frequency spectrum, we propose to apply convolutional Gaussian filters on 2D and 3D radiance fields for a coarse-to-fine training schedule that enables joint camera pose optimization. Leveraging the decomposition property in decomposed low-rank tensor, our method achieves an equivalent effect to brute-force 3D convolution with only incurring little computational overhead. To further improve the robustness and stability of joint optimization, we also propose techniques of smoothed 2D supervision, randomly scaled kernel parameters, and edge-guided loss mask. Extensive quantitative and qualitative evaluations demonstrate that our proposed framework achieves superior performance in novel view synthesis as well as rapid convergence for optimization. The source code is available at https://github.com/Nemo1999/Joint-TensoRF.

1 Introduction

In recent years, neural rendering has become a widely-used method for high-quality novel view synthesis. NeRF as a pioneer work (Mildenhall et al. 2020) represents a 3D radiance field as an implicit continuous function built upon multilayer perceptrons (MLPs) which is trained with differentiable volume rendering. While achieving excellent synthesis quality, NeRF suffers from training/inference inefficiency due to dense evaluation of the computationally expensive MLPs.

To this end, voxel-based methods built upon the explicit scene representation of 3D voxel grid (Sun, Sun, and Chen 2022; Fridovich-Keil et al. 2022; Liu et al. 2020) are proposed to achieve faster training and provide better rendering quality than the original MLP-based NeRF, hence becoming the more preferred choices for downstream applications.

Nevertheless, maintaining a dense 3D voxel grid is in turn memory intensive, thus still restricting wider applications of voxel-based methods. Fortunately, TensoRF (Chen et al. 2022) proposes to tackle such memory-intensive issue of the voxel grid via replacing the dense 3D grid with decomposed low-rank tensor. TensoRF achieves a high data compression ratio and low computational cost at the same time while also achieving state-of-the-art performance. Providing a win-win situation on memory usage and computational efficiency, the decomposed low-rank tensor architecture has been widely adopted in many recent works (Xu et al. 2023; Fridovich-Keil et al. 2023; Goel et al. 2022; Han and Xiang 2023; Shao et al. 2023; Tang et al. 2022; Meuleman et al. 2023).

On the other hand, the effectiveness of NeRF (and most of the aforementioned works) hinges on precise camera poses of input images, which are often calculated using Structure-from-Motion (SfM) algorithms like COLMAP (Schönberger and Frahm 2016). While some works (Wang et al. 2021; Lin et al. 2021; Chng et al. 2022) aim to bypass the slow and occasionally inaccurate COLMAP process by optimizing camera pose and scene representation jointly on the original MLP-based NeRF, their success is often tied to the spectral bias (Yüce et al. 2022) of the MLP architecture which ensures the smoothness of 3D radiance field early in training. Voxel-based methods, however, lack such properties and can overemphasize sharp edges, making naive joint optimization problematic as getting trapped in local optima (Fig. 2 (a)).

In this work, we present simple yet effective methods for refining the camera pose and the 3D scene using decomposed low-rank tensors (cf. Fig. 1). We identify that

Figure 1: Robust joint pose refinement on decomposed tensor. Our method enables joint optimization of camera poses and decomposed voxel representation by applying efficient separable component-wise convolution of Gaussian filters on 3D tensor volume and 2D supervision images.
controlling the frequency spectrum is vital for pose alignment, while directly realizing such control in a dense 3D grid could be nontrivial/challenging as well as computationally demanding. To this end, we introduce an efficient 3D filtering method using component-wise separable convolution for enabling the spectral control, which is more efficient than the traditionally well-known trick of separable convolution kernel as we additionally utilize the separability of the input signal. To further ensure stability in the optimization process, we propose several techniques, including smoothed 2D supervision, randomly scaled kernel parameter, and the edge-guided loss mask. These techniques are experimentally proven crucial for successful pose refinement in our ablation studies. In results, our proposed method requires only 50k training iterations, where all the previous methods typically needs 200k iterations (e.g. the overall training time is reduced to 25%, compared to previous MLP-based methods). The main reason behind this advantage is not only based on property of voxel-based architecture, but also relies on our carefully designed efficient spectral filtering algorithm that requires only single reusable voxel grid (please refer to Sec. 4.3). Moreover, our method performs favorably against state-of-the-art methods on novel view synthesis. Our contributions are three-fold:

• With 1D pilot study, we provide insights into the impact of spectral property of 3D scene on the convergence of joint optimization beyond the coarse-to-fine heuristic discussed in prior research, and propose a learning strategy built upon specially designed efficient component-wise convolution algorithm.

• To enhance the robustness of our joint optimization, we introduce techniques of smoothed 2D supervision, scaled kernel parameters, and the edge-guided loss mask.

• Training time drops by 25% versus existing MLP-based methods, with requiring only 50k iterations against 200k of previous methods. Results show state-of-the-art performance in novel view synthesis with unknown pose.

2 Related Work

Accelerating Neural Rendering. As the seminal work of neural rendering, NeRF adopts MLPs to construct the implicit representation of the 3D scene, providing high-quality view synthesis but having a time-consuming training process due to the computational demands of MLPs. For addressing such issue, different variants of NeRF are proposed to use custom spatial data structures where the scene information is distributed only locally thus aiding faster training and rendering, in which those spatial data structures include point cloud (Xu et al. 2022; Hu et al. 2023), space partitioning tree (Wang et al. 2022; Yu et al. 2021), triangular mesh (Chen et al. 2023b; Kulhanek and Sattler 2023), and voxel grid (Sun, Sun, and Chen 2022; Fridovich-Keil et al. 2022; Liu et al. 2020; Hedman et al. 2021). Among these variants, the voxel grid has become more popular due to its easy implementation and quality reconstruction. However, as scene dimensions grow, the memory usage of the voxel grid becomes inefficient. To address this, (Müller et al. 2022) recommends compressing the grid via hash encoding, while (Chen et al. 2022; Fridovich-Keil et al. 2023) suggest adopting tensor decomposition for 3D feature compression, in which our method is mainly based on (Chen et al. 2022) but can be adaptable to other tensor decomposition-based voxel structures like K-Planes (Fridovich-Keil et al. 2023).

Joint Pose Estimation on MLP-based NeRFs. (Wang et al. 2021) is one of the first NeRF-based attempts to tackle the joint problem of estimating camera poses and learning 3D scene representation by directly adjusting camera pose using gradient propagation on neural radiance fields. The robustness of such joint optimization is further enhanced by (Lin et al. 2021; Chng et al. 2022), where they propose various methods to smooth the pose gradient derived from the underlying MLP. (Chen et al. 2023) further increases the noise tolerance by a specially designed local-global joint alignment approach. Our method also tackles joint problems but is specifically designed for the voxel-based NeRF built upon the decomposed low-rank tensor architecture.

Pose Estimation on Decomposed Low-rank Tensors. There do exist works that optimize camera pose on decomposed low-rank tensor (Liu et al. 2023; Meuleman et al. 2023) but require rich additional geometry clues (e.g., depth map and optical flow). To our best knowledge, we are the first attempt to jointly optimize the camera pose and the decomposed low-rank tensor using only 2D image supervision.

Pose Estimation on Multi-Resolution Hash Encoding. Aside from decomposed low-rank tensor, multi-resolution hash encoding is another compressed voxel-based architecture proposed by (Müller et al. 2022). Along with such a choice of architecture, recently (Heo et al. 2023) has proposed to address the joint optimization of camera pose and multi-resolution hash encoding. They suggest a new interpolation scheme that provides smooth gradients hence preventing gradient fluctuation in the hash volume, along with
a curriculum learning scheme that controls the learning rate of the hash table at each resolution level. Although achieving impressive results on joint optimization, the effectiveness of their method is limited to multi-resolution hash encoding and is not applicable to decomposed low-rank tensor, while our proposed separable component-wise 3D convolution (and randomly scaled kernel) is specifically designed for decomposed low-rank tensor and not directly applicable to multi-resolution hash encoding, in which these two representations have their respective pros and cons.

3 Our Proposed Method

3.1 Joint Refinement of 3D Scenes and Poses

Volume Rendering for Radiance Field Reconstruction. Based on the setting of neural volume rendering in NeRF, the radiance fields respective for geometry and appearance for a 3D scene are represented via two functions (implemented by MLPs): \( F_\sigma : \mathbb{R}^4 \rightarrow \mathbb{R}^3 \) and \( F_c : \mathbb{R}^d \rightarrow \mathbb{R}^3 \), where \( F_\sigma \) returns the volume density of an input 3D coordinate, while \( F_c \) outputs the color at an input 3D coordinate given a 3D viewing direction. For rendering a pixel on 2D coordinate \( u \) with its homogeneous form \( \bar{u} = [u; 1]^\top \), we first sample a sequence of \( N \) 3D coordinates \( \{s_n\}_{n=1}^{N} \) along the camera ray defined by the camera center \( \vec{c} \) and the ray direction \( \vec{d} = K^{-1}\bar{u} \).

\[
\{s_n\}_{n=1}^{N} = s(\vec{c}, \vec{d}) = \{\vec{c} + t_n \cdot \vec{d}\}_{n=1}^{N},
\]

where \( K \) is the intrinsic camera matrix and \( \{t_n\}_{n=1}^{N} \) are \( N \) samples equidistantly distributed along the depth axis in between the near and far planes of the view frustum. The resultant color of the pixel is obtained by integrating through the density field \( F_\sigma \) and color field \( F_c \) using the volume rendering equation (Kajiya and Von Herzen 1984; Mildenhall et al. 2020), where we denote the discretized volume rendering integral by a function \( V \):

\[
V(F_\sigma, F_c, s(\vec{c}, \vec{d})) = \sum_{s_n \in s(\vec{c}, \vec{d})} T_n \cdot \alpha_n \cdot C_n,
\]

where \( T_n = \exp(-\sum_{j=1}^{n-1} \delta_j F_\sigma(s_j)) \) represents accumulated transmittance prior to \( s_n \), \( \alpha_n = 1 - \exp(-\alpha_n F_\sigma(s_n)) \) represents the opacity of sample \( s_n \), and \( C_n = F_c(s_n, \vec{d}^n) \) represents the color of sample \( s_n \), and \( \delta_j = ||s_j - s_{j-1}|| \) is the euclidean distance between two adjacent samples.

In the typical setting of NeRF, given a set of \( L \) 2D-images \( \mathbf{I} = \{I_1, \ldots, I_L\} \) with their corresponding camera poses \( \mathbf{P} = \{P_1, \ldots, P_L\} \in \mathfrak{se}(3) \) Lie algebra (parametrizing rigid 3D transformation as \( \mathfrak{se}(3) \) is a very common technique in robotics, here we follow the usage of (Lin et al. 2021)) as input, we aim to reconstruct the 3D scene represented by \( F_\sigma \) and \( F_c \), via minimizing the loss \( \mathcal{L}_{\text{rec}} \) of 2D photometric reconstruction with the gradient-based optimization algorithm, in which

\[
\mathcal{L}_{\text{rec}}(F_\sigma, F_c) = \sum_{i=1}^{L} \sum_{u \in U} \|V(F_\sigma, F_c, \mathcal{W}_d(P_i, s(0, \vec{d}^u))) - I_{iu}\|,
\]

where \( U \) is the set of all possible 2D coordinates in the input images, \( I_{iu} \in \mathbb{R}^3 \) is the RGB color of pixel location \( u \) on training image \( I_u \), warping function \( \mathcal{W}_d(P, \cdot) : \mathbb{R}^3 \rightarrow \mathbb{R}^3 \) performs rigid 3D transformation parameterized by \( P \in \mathfrak{se}(3) \) Lie algebra, and \( \mathcal{W}_d(P, s(\vec{0}, \vec{d}^u)) \) maps each sampled 3D coordinate in canonical ray (\( \vec{c} = \vec{0} \)) into a 3D sample coordinate of camera ray with pose \( P \). Note that this is an ill-posed reconstruction problem that suffers from shape-radiance ambiguity (Zhang et al. 2020).

3D Joint Optimization. When it comes to jointly estimating camera poses (where the camera poses \( \mathbf{P} \) are also unknown) and learning scene representation (Lin et al. 2021; Chng et al. 2022; Chen et al. 2023a; Heo et al. 2023), the problem is even more ill-defined with the objective now being extended from Eq. 3 and defined as:

\[
\mathcal{L}_{\text{joint}}(F_\sigma, F_c, \mathbf{P}) = \sum_{i=1}^{L} \sum_{u \in U} \|V(F_\sigma, F_c, \mathcal{W}_d(P_i, s(0, \vec{d}^u))) - I_{iu}\|.
\]

Such joint optimization is highly influenced by the structural bias of the underlying representation of \( \{F_\sigma, F_c\} \), which we will conduct a pilot study with a simpler 1D case in Sec. 3.2.

3.2 Gaussian Filter on 1D Signal Alignment

Here we aim to analyze the effect of the signal spectrum (since \( F_\sigma, F_c, \) and \( \mathbf{I} \) in Eq. 4) on the joint optimization process. We begin by reducing 3D joint optimization of camera pose and scene reconstruction into a simpler 1D counterpart of signal alignment.

1D Signal Alignment. Let us consider a target ground truth 1D signal \( f_{GT} \) (assuming the signal to be continuous, bounded, and have finite support), which we aim to reconstruct and align with. We are given randomly translated versions \( f_1, f_2 \) of the ground truth signal \( f_{GT} \), where \( f_1 = \mathcal{W}_{1d}(f_{GT}, p_1) \), \( f_2 = \mathcal{W}_{1d}(f_{GT}, p_2) \) with having \( \mathcal{W}_{1d} \) a signal translation operation defined as \( \mathcal{W}_{1d}(f, p)(x) = f(x - p) \), and \( p_1, p_2 \) are the translation values.

Although the reconstruction is trivial in such a 1D setting, in order to mimic the case of 3D joint optimization, we attempt to estimate a signal \( q \) as well as the translation values \( q_1 \) and \( q_2 \) via adopting the iterative gradient-based optimization on the reconstruction loss:

\[
\mathcal{L}_{1d}(q; q_1, q_2) = \sum_{i \in [1, 2]} \int \| \mathcal{W}_{1d}(g, q_i)(x) - f_i(x) \|^2 dx
\]

\[
= \sum_{i \in [1, 2]} \int \| g(x) - f_{GT}(x - p_i + q_i) \|^2 dx.
\]

Note that Eq. 5 and Eq. 4 are analogous in terms of their structure/formulation, where the difference only lies in the dimensionality. And \( \mathcal{L}_{1d} \) achieves the optimum whenever \( q_1 - q_2 = p_1 - p_2 \) and \( g = \mathcal{W}_{1d}(f_{GT}, p_1 - q_1) \). Please check Figure 3(a) for a simple visual representation of Equation 5, where \( f_1 \) and \( f_2 \) are connected to \( g \) by the reconstruction loss \( \mathcal{L}_{1d} \) (i.e blue arrows), whose gradients are used to update \( g \) and the translation values \( \{q_1, q_1\} \).

Connection between 1D Signal Alignment and 3D Joint Optimization. The formulation of 1D signal alignment effectively simulates the “local phenomenon” of joint camera pose alignment and 3D scene reconstruction on a 2D cross-section: As shown in Figure 3(c), where we consider two
First we transform the problem into 1D Signal Alignment. 

After aligning with each camera plane on a projected straight line, the 3D space passing through both camera planes and intersecting with neighboring camera poses as well as a cross-section in the 3D space passing through both camera planes and intersecting with each camera plane on a projected straight line, the RGB color values on such projected lines correspond to the superposition of all possible combinations of camera poses and cross-sections.

**Spectrum Analysis and Effect of Gaussian Filtering on 1D Signal Alignment.** First we transform the problem into a simpler form with a assumption that is reflected by the fast convergent property of voxel grids (cf. our supplement for detailed derivation of the theorem):

**Theorem 1** If we assume rapid convergence of signal $g$ (which means $g$ achieves local optima $g^*$ w.r.t current $q_1, q_2$, whenever we update $q_1, q_2$), we find that the problem in Eq. 5 is equivalent to pure alignment between two ground-truth signals, that is

$$L_{1d}(g, q_1, q_2) = L_{1d}(g^*, q_1, q_2) = L_{1d}(u) = \int \|f_{GT}(x) - f_{GT}(x + u)\|^2 ds,$$

where $u = (p_1 - p_2) - (q_1 - q_2)$ is the shift between two ground truth signals, which has an initial value of $p_1 - p_2$

We aim for $u$ to reach 0 with gradient-based optimization.

Next, by analyzing the relationship between $f_{GT}$ and the optimization gradient $\frac{d}{du} L_{1d}$ in terms of their spectral properties, we get the following result (cf. our supplement for detailed derivation of the theorem):

**Theorem 2**

$$\frac{d}{du} L_{1d} = \int \|\mathfrak{F}\lbrack f_{GT}\rbrack\|^2 \cdot H(u, k) dk,$$

where $H(u, k) = 4\pi k \sin(2\pi ku)$, $\mathfrak{F}\lbrack f_{GT}\rbrack$ is Fourier transform of $f_{GT}$, and $k$ is the wavenumber in frequency domain.

Particularly, we are interested in the sign of $\frac{d}{du} L_{1d}$ which determines the direction of our iterative optimization. We plot the value of $H(u, k)$ in Fig. 3(b)(Top), where we can observe that the sign of $H$ is well-behaved when the magnitude of $k$ is small (here well-behaving means the direction of the gradient is able to let $u$ descend to 0, i.e., being positive when $u >$ 0 and negative when $u <$ 0). However, when $k$ increases, the sign of $H$ quickly begins to alternate, and the magnitude increases, which causes the gradient to be large and noisy. Hence high-frequency signals with a spreading spectrum can easily lead the optimization process to get stuck in the local optima.

To this end, we demonstrate that applying a Gaussian filter on the signal $f_{GT}$ effectively mitigates the sign-alternating issue of the original $H$ function. Specifically, we show that filtering the input signal is equivalent to modulating $H$ by a Gaussian window (cf. our supplement for derivation):

**Theorem 3** Let $\tilde{L}_{1d}$ denotes $L_{1d}$ calculated with Gaussian convoluted signal $N \ast f_{GT}$, and $\mathfrak{F}\lbrack N\rbrack$ denotes the Fourier transform of the Gaussian kernel $N$, then we have

$$\frac{d}{du} \tilde{L}_{1d} = \int \|\mathfrak{F}\lbrack f_{GT}\rbrack\|^2 \cdot H(u, k) dk,$$

where $\tilde{H}(u, k) = ||\mathfrak{F}\lbrack N\rbrack||^2 \cdot H(u, k)$.

In Fig. 3(b)(Bottom), we plot the modulated $\tilde{H}(u, k)$, with observing that the misbehave region is suppressed (note that we set the variance of $N$ to 4 here). The gradient descent will likely converge to $u = 0$ once the initial magnitude of $u$ is less than 6.0. The region where $\frac{d}{du} \tilde{L}_{1d}$ does well-behave is quasi-convex and is guaranteed to converge to global optima given suitable learning rate that prevents us from getting stuck on saddle points. Our analysis agrees with the motivation behind the coarse-to-fine training schedule of (Lin et al. 2021) and (Heo et al. 2023). Specifically, observing that the well-behaved region in $\tilde{H}(u, k)$ grows wider as $u$ approaches 0 (cf. Fig. 3(b)(Top)), which means that we can loosen the filtering strength of Gaussian kernel as $u$ approaches 0, leading to larger and more accurate gradient.

### 3.3 2D Planar Image Alignment

In addition to the 3D joint optimization problem, previous works (Lin et al. 2021; Chng et al. 2022) also consider a
2D image patches alignment task as a simpler example of joint optimization, in which there are $L_{2d}$ overlapping image patches $I_{2d} = \{I_1, \ldots, I_{L_{2d}}\}$ cropped from a single ground truth image $I_{gt}$ before being transformed by 2D homography. The homography transforms are parameterized by $P_{2d} = \{P_1, \ldots, P_{L_{2d}}\} \subseteq s\ell(3)$ and initialized as $0$ (here we also follow from (Lin et al. 2021) the usage Lie algebra to parameterize 2D homography transform). Analogously to Equation 4, our objective is to jointly optimize the 2D image content $F_{2d} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ and per-patch homography warps $P_{2d}$ by the reconstruction loss. Joint optimization can be formulated as:

$$L_{2d}(F_{2d}, P_{2d}) = \sum_{i=1}^{L} \sum_{u \in U_{2d}} \| F_{2d}(P_{2d}(I_{2d}, u)) - I_{2d} \|_2^2,$$  

(9)

where $U_{2d}$ is the set of all possible 2D coordinates in the image patches, $I_{2d}$ is the color of pixel at location $u$ on input image patch $I_{gt}$, warp function $W_{2d}(P_{2d}) : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ performs 2D homography transformation parameterized by $P_{2d} \in s\ell(3)$ Lie algebra, and $W_{2d}(P_{2d}, u)$ maps 2D coordinate $u$ on $I_{gt}$ into a transformed 2D coordinate on patch $I_{i}$. Notice the strong structural correspondence among Eq. 5 (1D alignment), Eq. 9 (2D alignment), and Eq. 4 (3D alignment), the three problems share similar computational property.

We parameterize $F_{2d}$ by a 2D decomposed low-rank tensor $T_{2d} \in \mathbb{R}^{h \times w}$, where $w, h$ are the dimensions of the image. Motivated by our analysis in Section 3.2, we filter $T_{2d}$ with 2D Gaussian kernel to avoid overfitting.

$$F_{2d}(x) = (N_{2d} *_{2d} T_{2d})(x) = (N_{2d} *_{2d} (\sum_{r=1}^{R} v_r^X \otimes v_r^Y))(x),$$  

(10)

where $x \in \mathbb{R}^2$ is 2D pixel coordinates, $N_{2d}$ is 2D gaussian kernel, $*_{2d}$ is the convolution operator, and $\otimes$ denotes outer product between the $1D$ vector components $v_r^X \in \mathbb{R}^w$, $v_r^Y \in \mathbb{R}^h$. “(x)” at the end of the expressions means bilinearly interpolating the preceding discrete 2D volume with continuous coordinate $x$. Our method outperforms the na"{i}ve tensor method and previous methods (Lin et al. 2021; Chng et al. 2022), experiment results are shown at Sec. 4.1.

The width of Gaussian kernel $N_{2d}$ is controlled by an exponential coarse-to-fine training schedule that changes continuously (cf. our supplement for details of such kernel schedule). In order to support continuous changing width on a discrete Gaussian kernel, the kernel is generated by the following rule:

$$N_{id}^{\sigma}(\sigma) = \begin{cases} L_N / 2 \cdot \min(1, \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{\sigma^2}{2}}) & \text{if } \sigma > 0.0001 \\ \sigma = L_N / 2 & \text{otherwise}, \end{cases}$$

$$N_{2d}^{\sigma}(\sigma) = N_{1d}^{\sigma}(\sigma) \otimes N_{1d}^{\sigma}(\sigma),$$  

(11)

where $L_N$ is the size of the discrete kernel, 1D kernel $N_{1d}^{\sigma}(\sigma) \in \mathbb{R}^{L_N}$ is discretely sampled from continuous Gaussian distribution and clamped to a max value of $1.0$ before being concatenated into a vector by $\oplus$ operator. To avoid numerical instability, when $\sigma < 0.001$, we assign $N_{1d}^{\sigma}(\sigma)$ to be discrete impulse function $\delta$. 2D kernel $N_{2d}^{\sigma}(\sigma) \in \mathbb{R}^{L_N \times L_N}$ is generated by outer product of two 1D kernels.

### 3.4 Decomposed Low-Rank Tensor

This section describes the decomposed low-rank tensor proposed by TensoRF (Chen et al. 2022) which is the scene representation that our proposed method is built upon. While there are two different types of tensor decomposition considered in (Chen et al. 2022): CP-decomposition and VM-decomposition, although our method is also naturally applicable to CP-decomposition.

To represent the 3D color field $F_c$, we store the information in a 3D tensor $T_c \in \mathbb{R}^{I^3 \times J \times K}$, in which now $F_c$ is defined simply as component-wise interpolation of $T_c$.

$$T_c = \sum_{r=1}^{R} v_r^X \otimes M_{\sigma,r}^X \otimes v_r^Y \otimes M_{\sigma,r}^Y + v_r^Z \otimes M_{\sigma,r}^Z + v_r^Z \otimes M_{\sigma,r}^X \otimes v_r^Z,$$  

(12)

where $R$ is the number of components in the decomposition, $(v_r^X, v_r^Y, v_r^Z) \in (\mathbb{R}^I, \mathbb{R}^J, \mathbb{R}^K)$ are 1D vector-components for axes $(X, Y, Z)$ respectively, $(M_{\sigma,r}^X, M_{\sigma,r}^Y, M_{\sigma,r}^Z) \in (\mathbb{R}^{I \times J \times K}, \mathbb{R}^{I \times J}, \mathbb{R}^{I \times J \times K})$ are 2D matrix-components for axes $(X-Y, X-Z, Y-Z)$ respectively, operator $\otimes$ denotes the outer product between vector and matrix.

To represent the 3D color field $F_c$, the information $T_c(x) \in \mathbb{R}^{G}$ queried from 3D feature tensor $T_c \in \mathbb{R}^{I^3 \times J \times K}$ is decoded by a small MLP $S$ into RGB color value ($G$ is the input feature dimension of $S$). The implementation can be formulated as

$$F_c(x, \theta) = S(T_c(x), \theta),$$

$$T_c = \sum_{r=1}^{R} v_r^X \otimes M_{\sigma,r}^X \otimes v_r^Y \otimes M_{\sigma,r}^Y + v_r^Z \otimes M_{\sigma,r}^Z + v_r^Z \otimes M_{\sigma,r}^X \otimes v_r^Z,$$  

(13)

$T_c(x)$ denotes the component-wise-linear-interpolation of tensor volume $T_c$ on 3D coordinate $x$. $\theta$ is the viewing direction of the current ray. $v_{c,r}$ and $M_{c,r}$ have the same shape as their $v_{c,r}$ and $M_{c,r}$ counterparts, $b^X_c, b^Y_c, b^Z_c \in \mathbb{R}^G$ are feature components to expand the feature axis of $T_c$.

### 3.5 Separable Component-Wise Convolution

As theoretically analyzed in Sec. 3.2 and empirically shown in Fig. 2(a), na"{i}vely applying low-rank decomposed tensor (which lacks internal bias that limits the spectrum of learned signal, hence corresponds to the top raw of Fig. 3) to joint camera pose optimization results in suboptimal reconstruction quality and inaccurate poses. Therefore, we propose to limit the spectrum of the radiance field $F_c$ and $F_s$ with a coarse-to-fine training schedule.

If we na"{i}vely convolve the 3D Gaussian kernel with our 3D volume $T_c$, (as in the 2D planar case of Eq. 10), we would have to reconstruct the whole 3D tensor before applying convolution, destroying the space compression advantage of decomposed low-rank tensor, see Eq. 14.

$$F_{2d}(x, y, z) = (N_{2d} *_{2d} T_{2d})(x, y, z),$$  

(14)
$O(I \cdot J \cdot K)$ respectively, where $L_N$ is the size of 3D Gaussian kernel in each dimension.

To achieve computationally efficient convolution on the 3D decomposed low-rank tensor volume, we perform our proposed separable component-wise convolution, by taking advantage of the following identity (whose correctness will be proven in the supplementary material).

**Theorem 4**

\[
\tilde{T}_\sigma = \sum_{r=1}^{R} \tilde{\varphi}^X_{c,r} \otimes \tilde{M}^X_{a,r} \otimes b^X + \tilde{\varphi}^Y_{r} \otimes \tilde{M}^Y_{a,r} \otimes b^Y + \tilde{\varphi}^Z_{c,r} \otimes \tilde{M}^Z_{a,r} \otimes b^Z, \tag{15}
\]

where \(\tilde{T}_\sigma = (N_{3d} * 3d \tilde{T}_\sigma)\) denotes the 3D Gaussian convoluted tensor volume, \(\tilde{\varphi}_{\sigma, r} = (\hat{N}_{id} * 1d \tilde{\varphi}_{\sigma, r})\) denotes the 1D Gaussian convoluted vector component, and \(\tilde{M}_{\sigma, r} = (N_{2d} * 2d \tilde{M}_{\sigma, r})\) denotes the 2D Gaussian convoluted matrix component. In other words, the **3D convoluted tensor can be expressed as the composition of individually convoluted components**, which allows us to distribute the 3D Gaussian convolution across the individual components of the decomposed low-rank tensor. Similar to Sec. 3.4, the value of the density field is component-wised linearly sampled from the Gaussian convoluted components, i.e., \(\tilde{F}_\sigma(x) = \tilde{T}_\sigma(x)\). Similarly, the spectral restricted version of the color field \(\tilde{F}_\sigma\) can be obtained as

\[
\tilde{F}_c(x, \tilde{d}) = S(\tilde{T}_c(x), \tilde{d})
\]

\[
\tilde{T}_c = \sum_{r=1}^{R} \tilde{\varphi}^X_{c,r} \otimes \tilde{M}^X_{a,r} \otimes b^X + \tilde{\varphi}^Y_{r} \otimes \tilde{M}^Y_{a,r} \otimes b^Y + \tilde{\varphi}^Z_{c,r} \otimes \tilde{M}^Z_{a,r} \otimes b^Z. \tag{16}
\]

With separable component-wise convolution, the time complexity required is \(O(I \cdot J \cdot L_N + J \cdot K \cdot L_N + K \cdot I \cdot L_N)\) for computing convoluted components (assuming that we separate 2D Gaussian convolution on matrix components into 1D Gaussian convolutions), and \(O(R)\) for each query sample (same as the original decomposed tensor in (Chen et al. 2022)), drastically reducing the computation required for filtering 3D radiance fields \(\tilde{F}_\sigma\) and \(\tilde{F}_c\).

We stress here that our proposed component-wise convolution is different from traditional technique of separated kernel convolution in signal processing literature, in the sense that the common separated kernel technique only separates the 3D kernel without utilizing the separability of the input signal itself, and hence requires sequentially performing three 1D convolution operation on 3D volume, the time complexity of traditional technique would be \(O(I \cdot J \cdot K \cdot L_N)\), and also requires a 3-dimensional memory with space complexity of \((I \cdot J \cdot K)\) to store convolution result.

### 3.6 Techniques for Increasing Pose Robustness

Here we summarize our improvements on naïve decomposed low-rank tensors that improve joint camera pose optimization and radiance field reconstruction.

**Coarse-to-Fine 3D schedule.** Using efficient 3D convolution algorithm in Sec. 3.5. During training, we apply a coarse-to-fine schedule on the 3D radiance field \(\tilde{F}_\sigma, \tilde{F}_c\) by controlling the kernel parameter (\(\sigma\) of Eq. 11) of the Gaussian kernel, which is exponentially reduced to 0 at 10k iterations and remains 0 afterward (for detailed settings of \(\sigma\), please refer to the supplement).

**Smoothed 2D Supervision.** Inspired by the analysis in Sec. 3.2, we discovered that blurring the 2D training image with a parallel set of scheduled 2D Gaussian kernels also helps the joint optimization. On the one hand, smoothed supervision images produce smoothed image gradients and stabilize the camera alignment. On the other hand, smoothed training image also helps to restrict the spectrum of the learned 3D scene. The Gaussian schedule for smoothing 2D training images is similar to that of the 3D radiance fields.

**Randomly Scaled Kernel Parameter and Edge Guided Loss.** From the previous spectral analysis in Sec. 3.2, one may have the impression that a larger kernel leads to stronger modulation, and hence always results in more robust pose registration. However, this is not always true, because the magnitude of \(H(u, k)\) decreases linearly as \(k\) approaches 0. Notice that in Fig. 3(b) the magnitude of modulated \(H\) is weaker than that of \(H\), which means that \(\frac{\partial}{\partial u} \mathcal{L}_{id}\) is weaker than \(\frac{\partial}{\partial u} \mathcal{L}_{id}\) and therefore is more easily influenced by noise. In the 3D case, this weak and noisy gradient problem caused by overly aggressive filtering corresponds to the excessive blur effect that destroys important edge signals in the training images, causing pose alignment to fail. See Fig. 4(b) for a visualization of the image blurred by an overstrength kernel, in which the thin edge information is eliminated, causing the camera pose to randomly drift.

Based on the effect of weak and noisy gradient problem, when applying only coarse-to-fine 3D schedule and smoothed 2D supervision, we found that it is insufficient to use a single-size kernel on different real-world scene structures (in which the same kernel may be overly aggressive in one scene, but overly gentle in another scene). Therefore, we introduce randomly scaled kernel, which randomly scales the kernel by a factor uniformly sampled from \([0, 1]\). Random scales are sampled independently among 3D Gaussian kernels (for the radiance field) and 2D Gaussian kernels (for training images), allowing combinations of different-sized kernels to guide the joint optimization. See Fig. 4(c) for a visualization of the same input image filtered by a range of randomly sampled kernels. We observe that the training schedule becomes more robust when we alternate between these randomly sampled kernel scales.

Another way to mitigate the weak and noisy gradient problem is the edge guided loss, in which we increase the learning rate by 1.5x (and hence amplify the gradient signal) on the pixels in the edge region, from which the learning signal for pose alignment mainly comes. See visualization in Fig. 4 (d), where we color the edge area that is detected using the Sobel filter (Kanopoulos, Vasanthavada, and Baker 1988) on the filtered 2D images in yellow. Edge-guided rendering loss helps the joint optimization focuses more on the edge area of the training images, resulting in more robust pose optimization. Empirically we apply this edge-guided scale alternately on every other training iteration.
Figure 4: Visualization of 2D Randomly Sampled Kernel and Edge Guided Loss. (a) Input supervision without kernel. Joint optimization using unblurred images easily overfit to high-frequency noises (b) Input supervision blurred by an overly aggressive kernel. Notice that the edge information is largely destroyed by the blurring process, resulting in weak and noisy gradients, causing the poses to drift around easily. (c) Same input supervision blurred by four randomly scaled kernels. We empirically found that mixing different filtering strengths results in a more robust joint optimization. (d) We select edge area of a blurred image by Sobel filter with a threshold set to 1.25x of the average value of the filtered edge-strength map.

Figure 5: Qualitative comparisons of the 2D image patch alignment. 2D TensoRF + 2D Gaussian successfully registers accurate warping parameters, verifying the analysis of Gaussian filtering on joint optimization.

Table 1: Quantitative results of planar image alignment.

<table>
<thead>
<tr>
<th>Methods</th>
<th>sl(3) error ↓</th>
<th>patch PSNR ↑</th>
</tr>
</thead>
<tbody>
<tr>
<td>BARF</td>
<td>0.0105</td>
<td>35.19</td>
</tr>
<tr>
<td>Naive 2D TensoRF</td>
<td>0.5912</td>
<td>20.80</td>
</tr>
<tr>
<td>2D TensoRF + 2D Gaussian</td>
<td><strong>0.0023</strong></td>
<td><strong>40.70</strong></td>
</tr>
</tbody>
</table>

4 Experiments

Although our method is applicable to various decomposed low-rank tensor implementations, in this section, we validate our proposed method using TensoRF (Chen et al. 2022) with inaccurate or unknown camera poses.

We evaluate our proposed method against three previous works BARF (Lin et al. 2021), GARF (Chng et al. 2022), and HASH (Heo et al. 2023). Since the implementation of GARF and HASH are unavailable, we directly use the results reported in their paper for comparison. We compare these methods on the planar image alignment task and novel view synthesis task on NeRF-Synthetic and LLFF dataset. We provide detailed implementation details and experimental setup in the supplementary material.

4.1 Results

Planar Image Alignment (2D). In Fig. 5 we compare our method (i.e., 2D TensoRF + 2D Gaussian) with naive 2D TensoRF implementation (Chen et al. 2022) and BARF (Lin et al. 2021). Quantitative results are reported in Tab. 1, including sl(3) warp error and patch PSNR. These results demonstrate the effectiveness of Gaussian filtering in joint optimization, verifying the analysis in Sec. 3.2.

NeRF (3D): Synthetic Object & Real World Objects. Tab. 2 reports the pose error and novel-view synthesis quality of the NeRF-Synthetic dataset. Our method achieves the smallest pose error in 5 out of 8 scenes and achieves the best reconstruction quality in all eight scenes, and the quantitative results are shown in Fig. 6.

Tab. 3 reports the pose error and novel-view synthesis quality of the LLFF dataset. Our method achieves pose error on par with previous methods and produces the best average view synthesis quality. Our method also scores the best LPIPS in 7 out of 8 scenes, indicating that our method produces perceptually more natural novel-view synthesis.

Note that we achieve state-of-the-art results within only 20% to 25% of training iterations, while all other competing methods train for 200k iterations.

4.2 Ablation

Component Analysis. In Tab. 4, we report the effect of each proposed component on the pose error and PSNR of the optimization results. The results are average across all real-world scenes in the LLFF dataset. In (a) (b), we show the effect of randomly scaled kernel described in Sec. 3.6. In (b)(c), we show the effectiveness of edge guided loss (Sec. 3.6). Finally, in (c)(d)(e), we show the necessity of Gaussian filtering on both 2D supervising images and 3D radiance field represented by a decomposed tensor grid, which validates the analysis in Sec. 3.2.

Potential Baseline of TensoRF with BARF/GARF. One may suspect that we can solve the joint optimization problem of decomposed low-rank tensor by simply applying the method of (Lin et al. 2021) or (Chng et al. 2022), we clar-
Table 2: Quantitative results on the NeRF-Synthetic dataset. Our method achieves the best average novel-view synthesis quality and the best pose error in 5 out of 8 scenes. Notice that our method converges within 40k iterations, while all previous methods train for 200k iterations.

<table>
<thead>
<tr>
<th>Scene</th>
<th>GARF</th>
<th>BARF</th>
<th>HASH</th>
<th>Ours</th>
<th>GARF</th>
<th>BARF</th>
<th>HASH</th>
<th>Ours</th>
<th>GARF</th>
<th>BARF</th>
<th>HASH</th>
<th>Ours</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chair</td>
<td>0.113</td>
<td>0.096</td>
<td>0.085</td>
<td>0.874</td>
<td>0.549</td>
<td>0.428</td>
<td>0.365</td>
<td>3.501</td>
<td>31.32</td>
<td>31.16</td>
<td>31.95</td>
<td>35.22</td>
</tr>
<tr>
<td>Drum</td>
<td>0.052</td>
<td>0.043</td>
<td>0.041</td>
<td>0.037</td>
<td>0.232</td>
<td>0.225</td>
<td>0.214</td>
<td>0.113</td>
<td>26.29</td>
<td>26.26</td>
<td>28.31</td>
<td>31.37</td>
</tr>
<tr>
<td>Ficus</td>
<td>0.081</td>
<td>0.085</td>
<td>0.079</td>
<td>0.050</td>
<td>0.461</td>
<td>0.474</td>
<td>0.479</td>
<td>0.173</td>
<td>34.69</td>
<td>34.54</td>
<td>35.41</td>
<td>37.18</td>
</tr>
<tr>
<td>Hotdog</td>
<td>0.235</td>
<td>0.248</td>
<td>0.229</td>
<td>0.105</td>
<td>1.123</td>
<td>1.093</td>
<td>1.123</td>
<td>0.499</td>
<td>27.64</td>
<td>27.50</td>
<td>27.92</td>
<td>31.98</td>
</tr>
<tr>
<td>Lego</td>
<td>0.101</td>
<td>0.082</td>
<td>0.071</td>
<td>0.049</td>
<td>0.299</td>
<td>0.291</td>
<td>0.272</td>
<td>0.049</td>
<td>26.29</td>
<td>25.87</td>
<td>26.38</td>
<td>28.03</td>
</tr>
<tr>
<td>Materials</td>
<td>0.842</td>
<td>0.084</td>
<td>0.082</td>
<td>0.058</td>
<td>0.461</td>
<td>0.474</td>
<td>0.479</td>
<td>0.173</td>
<td>34.69</td>
<td>34.54</td>
<td>35.41</td>
<td>37.18</td>
</tr>
<tr>
<td>Mic</td>
<td>0.070</td>
<td>0.071</td>
<td>0.068</td>
<td>0.067</td>
<td>0.232</td>
<td>0.225</td>
<td>0.214</td>
<td>0.113</td>
<td>27.64</td>
<td>27.50</td>
<td>27.92</td>
<td>31.98</td>
</tr>
<tr>
<td>Ship</td>
<td>0.073</td>
<td>0.075</td>
<td>0.079</td>
<td>0.058</td>
<td>0.310</td>
<td>0.280</td>
<td>0.287</td>
<td>0.102</td>
<td>1.123</td>
<td>1.093</td>
<td>1.123</td>
<td>0.499</td>
</tr>
<tr>
<td>Mean</td>
<td>0.195</td>
<td>0.193</td>
<td>0.184</td>
<td>0.400</td>
<td>0.744</td>
<td>0.756</td>
<td>0.722</td>
<td>1.533</td>
<td>28.96</td>
<td>28.84</td>
<td>29.86</td>
<td>32.07</td>
</tr>
</tbody>
</table>

Table 3: Quantitative results on the LLFF dataset. Our method achieves the best average novel-view synthesis quality and best LPIPS in 7 out of 8 scenes. Our method converges within 50k iterations, while all previous methods train for 200k iterations.

<table>
<thead>
<tr>
<th>Scene</th>
<th>GARF</th>
<th>BARF</th>
<th>HASH</th>
<th>Ours</th>
<th>GARF</th>
<th>BARF</th>
<th>HASH</th>
<th>Ours</th>
<th>GARF</th>
<th>BARF</th>
<th>HASH</th>
<th>Ours</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fern</td>
<td>0.470</td>
<td>0.191</td>
<td>0.110</td>
<td>0.472</td>
<td>0.250</td>
<td>0.102</td>
<td>0.102</td>
<td>0.199</td>
<td>24.51</td>
<td>23.79</td>
<td>24.62</td>
<td>26.17</td>
</tr>
<tr>
<td>Flower</td>
<td>0.460</td>
<td>0.251</td>
<td>0.301</td>
<td>1.375</td>
<td>0.220</td>
<td>0.224</td>
<td>0.211</td>
<td>0.102</td>
<td>27.91</td>
<td>27.84</td>
<td>27.14</td>
<td>29.04</td>
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<tr>
<td>Fortress</td>
<td>0.030</td>
<td>0.479</td>
<td>0.211</td>
<td>0.449</td>
<td>0.270</td>
<td>0.364</td>
<td>0.241</td>
<td>0.419</td>
<td>31.39</td>
<td>31.18</td>
<td>32.33</td>
<td>35.22</td>
</tr>
<tr>
<td>Horns</td>
<td>0.030</td>
<td>0.304</td>
<td>0.049</td>
<td>0.386</td>
<td>0.210</td>
<td>0.222</td>
<td>0.209</td>
<td>0.251</td>
<td>27.64</td>
<td>27.50</td>
<td>27.92</td>
<td>31.98</td>
</tr>
<tr>
<td>Leaves</td>
<td>0.130</td>
<td>1.272</td>
<td>0.840</td>
<td>1.990</td>
<td>0.230</td>
<td>0.249</td>
<td>0.228</td>
<td>0.397</td>
<td>26.40</td>
<td>25.37</td>
<td>25.19</td>
<td>25.62</td>
</tr>
<tr>
<td>Orchids</td>
<td>0.430</td>
<td>0.627</td>
<td>0.399</td>
<td>0.279</td>
<td>0.410</td>
<td>0.404</td>
<td>0.386</td>
<td>0.340</td>
<td>29.09</td>
<td>29.08</td>
<td>30.14</td>
<td>29.68</td>
</tr>
<tr>
<td>Room</td>
<td>0.270</td>
<td>0.320</td>
<td>0.271</td>
<td>0.188</td>
<td>0.200</td>
<td>0.270</td>
<td>0.213</td>
<td>0.191</td>
<td>31.39</td>
<td>31.18</td>
<td>32.33</td>
<td>35.22</td>
</tr>
<tr>
<td>T-Rex</td>
<td>0.420</td>
<td>1.138</td>
<td>0.894</td>
<td>0.523</td>
<td>0.360</td>
<td>0.720</td>
<td>0.474</td>
<td>0.416</td>
<td>22.86</td>
<td>22.55</td>
<td>22.97</td>
<td>24.19</td>
</tr>
<tr>
<td>Mean</td>
<td>0.280</td>
<td>0.573</td>
<td>0.384</td>
<td>0.709</td>
<td>0.269</td>
<td>0.331</td>
<td>0.258</td>
<td>0.325</td>
<td>24.55</td>
<td>23.97</td>
<td>24.79</td>
<td>25.27</td>
</tr>
</tbody>
</table>

Figure 6: Visual comparisons of novel view synthesis.
Table 6: Ablation On Low-Pass Filters.

<table>
<thead>
<tr>
<th>Filter</th>
<th>Rot. ↓</th>
<th>Trans. ↓</th>
<th>PSNR ↑</th>
<th>SSIM ↑</th>
<th>LPIPS ↓</th>
</tr>
</thead>
<tbody>
<tr>
<td>Box filter</td>
<td>9.98</td>
<td>0.06</td>
<td>20.18</td>
<td>0.387</td>
<td>0.165</td>
</tr>
<tr>
<td>Gaussian filter</td>
<td>0.46</td>
<td>0.004</td>
<td>29.49</td>
<td>0.874</td>
<td>0.063</td>
</tr>
</tbody>
</table>

Table 7: Ablation on Applying Randomly Scaled Kernel Parameter and Edge Guided Loss in Synthetic Scenes

<table>
<thead>
<tr>
<th>Setting</th>
<th>Rot. ↓</th>
<th>Trans. ↓</th>
<th>PSNR ↑</th>
</tr>
</thead>
<tbody>
<tr>
<td>w/ random kernels &amp; edge guided loss</td>
<td>0.06</td>
<td>0.002</td>
<td>34.34</td>
</tr>
<tr>
<td>w/o random kernels &amp; edge guided loss</td>
<td>0.28</td>
<td>0.010</td>
<td>34.43</td>
</tr>
</tbody>
</table>

Table 8: Ablation: Sensitivity Analysis On Gaussian Noise in Blender Chair.

<table>
<thead>
<tr>
<th>σ</th>
<th>0.125</th>
<th>0.15</th>
<th>0.175</th>
<th>0.2</th>
</tr>
</thead>
<tbody>
<tr>
<td>BARF Rotation ↓</td>
<td>0.094</td>
<td>0.068</td>
<td>0.100</td>
<td>0.108</td>
</tr>
<tr>
<td>Translation ↓</td>
<td>0.004</td>
<td>0.004</td>
<td>0.005</td>
<td>0.005</td>
</tr>
<tr>
<td>Ours Rotation ↓</td>
<td>0.07</td>
<td>0.062</td>
<td>0.072</td>
<td>0.066</td>
</tr>
<tr>
<td>Translation ↓</td>
<td>0.003</td>
<td>0.003</td>
<td>0.003</td>
<td>0.002</td>
</tr>
</tbody>
</table>

Using Other Low-Pass Filters. As we would like to have identical filtering strength along all spatial directions, we adopt the Gaussian filter in our method as it is the only kernel that is both circularly symmetric and separable (a well-known property in signal processing). Nevertheless, we experiment with other low-pass filters. We report in Tab. 6 the performance of using the box filter (i.e., a representative low-pass filter) on the LLFF Fortress scene, in which we clearly observe the benefits of using the Gaussian filter.

Applying Randomly Scaled Kernel Parameter and Edge Guided Loss on Synthetic Scenes. Although the two techniques are originally proposed to improve the robustness of complex real-world scenes, they do not harm the performance of synthetic ones and even slightly boost the pose estimation, as shown in Tab. 7.

Sensitivity w.r.t. Pose Initialization. We adopt the Chair scenes in the Blender dataset to conduct sensitivity analysis upon pose initialization via varying variance σ of Gaussian noise. The result is shown in Tab. 8, which demonstrates that both BARF and our proposed method show certain robustness against the noisy initialization of camera poses.

4.3 Time Complexity

In Fig. 7, we compare with previous methods on average PSNR and training iterations in the Synthetic NeRF dataset.

Figure 7: PSNR and training iterations comparison.

The figure shows two advantages of our method: (1) rapid convergence and (2) high-quality novel view synthesis.

The early-stage blurry supervision can hinder detailed structure reconstruction later in the optimization, impacting the final result quality. Our method resolves this problem by applying 3D filters with directly controllable kernel parameters, which enables smooth and rapid transition (by continuous exponential kernel schedule) of the 3D content across the spectrum domains, as opposed to previous methods that use indirect methods (e.g., learning rate in (Heo et al. 2023), encoding magnitude in (Lin et al. 2021)) to influence learned 3D scene spectral property. Furthermore, our method is carefully designed to use a single voxel grid, which is trained only once in the coarse-to-fine schedule controlled by our proposed efficient component-wise convolution algorithm, thus leading to faster convergence; in comparison, (Heo et al. 2023), which also uses voxel-based representation, requires sequential curriculum learning upon multiple voxel grids of different resolutions, resulting in four times more training iterations than ours.

5 Conclusion

Our contributions is three fold: 1) Theoretically, we provide insights into the impact of 3D scene properties on the convergence of joint optimization beyond the coarse-to-fine heuristic discussed in prior research (e.g., BARF, Heo et al. 2023), thus offering a filtering strategy for improving the joint optimization of camera pose and 3D radiance field. 2) Algorithmically, we introduce (and prove the equivalence of) an effective method for applying the pilot study’s filtering strategy on the decomposed low-rank tensor, notice that the proposed separable component-wise convolution is more efficient than the traditionally well-known trick of separable convolution kernel as we additionally utilize the separability of the input signal. Furthermore, we also propose other techniques such as randomly-scaled kernel parameter, blurred 2D supervision, and edge-guided loss mask to help our proposed method better perform in complex real-world scenes. 3) Comprehensive evaluations demonstrate our proposed framework’s state-of-the-art performance and rapid convergence without known poses.
Acknowledgments
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References


