Inferring Patient Zero on Temporal Networks via Graph Neural Networks

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Abstract

The world is currently seeing frequent local outbreaks of epidemics, such as COVID-19 and Monkeypox. Preventing further propagation of the outbreak requires prompt implementation of control measures, and a critical step is to quickly infer patient zero. This backtracking task is challenging for two reasons. First, due to the sudden emergence of local epidemics, information recording the spreading process is limited. Second, the spreading process has strong randomness. To address these challenges, we tailor a gnn-based model to establish the inverse statistical association between the current and initial state implicitly. This model uses contact topology and the current state of the local population to determine the possibility that each individual could be patient zero. We benchmark our model on data from important epidemiological models on five real temporal networks, showing performance significantly superior to previous methods. We also demonstrate that our method is robust to missing information about contact structure or current state. Further, we find the individuals assigned higher inferred possibility by model are closer to patient zero in terms of core number and the activity sequence recording the times at which the individual had contact with other nodes.

Introduction

Artificial intelligence is providing increasingly valuable support to a diverse range of applications in medicine (Buch, Ahmed, and Maruthappu 2018) by assisting humans to sift through massive amounts of medical data and uncover the relevant underlying patterns (Jittprasong 2022). Here, we propose an AI-based solution for source detection in contagion processes, i.e., inferring patient zero, the individual who initially introduces the virus into the local population. At present, countries around the world are plagued by highly contagious diseases, e.g., COVID-19 and Monkeypox. During an incubation period, the initially infected population can be contagious without exhibiting detectable symptoms, which can lead to the unforeseeable outbreak of an epidemic. After an outbreak, source detection is a necessary measure to investigate pathogenesis, cut off the route of transmission and block further propagation. An efficient detection algorithm can use limited data to determine where a virus comes from and guide governments to develop targeted procedures for epidemic prevention.

The backtracking problem’s practical significance means it has received sustained attention across several communities, including epidemiology, network science and computer science. However, many algorithms require detailed information about the spreading process, such as the exact moment when each individual was infected or the person by whom each individual was infected, and the sudden and unexpected onset of epidemics make this data difficult to obtain in practice. Our algorithm is designed for the more common scenario in which the available information is limited to three aspects (see Fig. 1). First, a snapshot of the distribution of the disease throughout the population at the final moment. This final state is usually obtained by carrying out a full screening, in COVID-19, for example, by nucleic acid testing. Second, the contact relation of the local population during the contagion processes, which can be modelled as a temporal network in which nodes represent individuals and links represent physical proximity within a distance which risks transmission. These contact networks can be reconstructed from survey or modern location technologies, such as mobile signaling data. Third, an estimated time interval – not necessarily a precise time – when the outbreak starts.

In many epidemic models, individuals are infected with a certain probability when they come into contact with a patient, with the infection rate depending on the type of disease. Thus, the spreading process is strongly random. Even with the same patient zero, restarting the spreading process many times can result in very different snapshots. For example, when patient zero encounters an individual who is a hub node in the contact network, whether this encounter becomes an effective transmission has a great influence on the final size of infected population. On the other hand, similar final snapshots can emerge from distinct patient zeros, especially when their topological distance on the temporal network is small. Soft Margin Monte Carlo estimator (Antulov-Fantulin et al. 2015) runs extensive simulations of spreading taking each infected individual as a potential patient zero in turn, and quantifies the similarity between the simulated and real snapshots. The individual with maximum similarity is identified as patient zero. However, this method provides limited insights into how the behavior of the spreading dynamics system depends on the initial state (Strogatz 2018),

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and fails when contact networks are dense or the estimated parameters used in simulation deviate slightly from those of the real contagion process.

To provide implicit understanding and improve concrete inferences, we tailor a graph neural network (GNN) (Santoro et al. 2017; Battaglia et al. 2018; Zhou et al. 2020; Wu et al. 2020) to establish the statistical association between initial sources and final snapshots under the stochastic spreading environment. The source detection problem can be mapped to a multi-classification problem in which each individual in the population is a separate category. The gnn-based model processes the encoded spreading information, and estimates the possibility of each individual to be patient zero (see Fig. 2). Experiments on simulation data generated by classic epidemiological models on five real temporal networks indicate that the performance of our method is significantly superior to established methods. We also design two scenarios with missing information to show the robustness of the proposed algorithm, including partially missing contact structure and partial non-observation of population state. Further, we give some insight into the interior reasoning of gnn-based models based on topological properties of patient zero. Specifically, we find the closeness of the activity sequence (which records the times at which a node had an active edge) and core number (Batagelj and Zaversnik 2003; Carini et al. 2007) to those of the true patient zero tend to increase with inferred possibility to be the infection source, but the same is not true of degree.

**Related Work**

Several methods of source detection (Huang et al. 2018) are based on calculating measures of node centrality on the sampled network, such as distance centrality, Jordan centrality (Zhu and Ying 2014), closeness centrality, modified betweenness centrality (Comin and da Fontoura Costa 2011), dynamical age (Fioriti, Chinnici, and Palomo 2014), and rumor centrality (Shah and Zaman 2010, 2011), which estimates the probability of a node as the source as proportional to the count of all possible sequences of infection starting from that node.

The strategy of Pinto, Thiran, and Vetterli (2012) requires a set of monitoring nodes which record from which neighbor and at which times information is received, and adopt a maximum likelihood estimator for potential sources that averages over two different sources of randomness: the uncertainty in the paths that the information takes to reach the monitors and the uncertainty in the time that the information takes to cross the edges. For every possible source of the epidemic, Lokhov et al. (2014) use a fast dynamic message-passing method (DMP) to estimate the probability that all nodes in the network are the state in the observed snapshot, and a mean-field like approximation to compute the probability of the observed snapshot as a product of the marginal probabilities. Finally, the potential sources are ranked according to that probability. To overcome some drawbacks of DMP, the belief propagation equations are derived (Altarelli et al. 2014) for the posterior distribution of the time evolution of the state of the system conditioned on some observations. GNN has been used to study contagion processes for learning the reverse dynamics and predicting patient zero, yet on static networks (Shah et al. 2020). Time-reversal backward spreading (TRBS) (Shen et al. 2016) requires the arrival time of certain signals at monitoring nodes and network structure weighted to represent time delay of propagation. TRBS starts from a monitor $o_k$ and spreads to all nodes in the network along the reversed direction of links to yield a reversed arrival time $t_{o_k} - t(i, o_k)$ at a node $i$, where $t(i, o_k)$ is the shortest time delay from $o_k$ to $i$. Then, the node $i$ gets a vector $T_i = [t_{o_1} - t(i, o_1), t_{o_2} - t(i, o_2),..., t_{o_m} - t(i, o_m)]^T$ from the set of monitors. The node with the minimum variance of $T_i$ is the inferred source. Backward temporal diffusion process (Huang et al. 2017) extends TRBS to temporal networks.

Most algorithms are either developed for static networks or require a considerable number of monitoring nodes to precisely record information during the spreading process. This is not applicable to our problem due to the time-varying temporal contact network and the unexpected nature of the outbreak making infeasible the timely installation of monitors.

**Method**

**Problem Formulation**

The local population represents a typical complex system. To represent the architecture of the complex system we use a temporal network in which nodes are the system’s components and temporal links capture changing interactions.
between these components (Holme and Saramäki 2012; Li et al. 2017). The temporal network $G = \{G_0, G_1, \ldots, G_T\}$ is an ordered sequence of slice networks $G_t$ on the same node set $V$, as shown in Fig. 1. The evolution of states on slice networks are represented as $S = \{S_0, S_1, \ldots, S_T\}$, where $S_t$ is the state of the node set on slice $G_t$. Since an interval of possible initial times is known rather than an exact initial time, the posited temporal network $\tilde{G}$ may start either earlier or later than reality $G$. Then, our problem is expressed concisely as: inferring $S_0$ given $\{S_T, \tilde{G}\}$. Assuming only one node is infected in $S_0$, the problem is further refined into that of inferring patient zero.

**Modeling of Contagion Process**

Epidemic modeling describes the dynamical evolution of the contagion process within the local population as a function of time (Pastor-Satorras et al. 2015). Epidemic models generally assume that the population can be divided into different classes depending on the stage of the disease (Diekmann and Heesterbeek 2000), such as susceptible $S$ who are healthy currently and can be exposed to infection, infectious $I$ who are sick and can transmit the disease to contacts, and recovered $R$ who have previously had the disease and are now non-infectious and immune. Here we adopt the classic three-state susceptible-infected-recovered (SIR) model which defines basic individual-level processes governing the two possible transitions of individuals from one class to another as:

$$S(i) + I(j) \xrightarrow{\beta} I(i) + I(j),$$

(1)

$$I(i) \xrightarrow{\gamma} R(i).$$

(2)

The first transition Eq. 1, denoted $S \rightarrow I$, occurs when a susceptible individual $i$ has contact with an infectious individual $j$ and becomes infected with infection rate $\beta$. The second transition Eq. 2, denoted $I \rightarrow R$, occurs when the infectious individual $i$ recovers from the disease with recovery rate $\gamma$ and obtains immunity which lasts longer than the time scale of the epidemic outbreak.

**Encoding Available Information**

The limited information available for source detection includes the final state and structure of temporal networks. These are designed as a representation that can be exploited in machine learning models.

a. Final state. When the SIR model is applied to simulate the spreading process, the state of an individual $C_i$ can transform among three classes; susceptible, infectious and recovered. The final state of the complex system is a macro aggregate comprising the microstates of the node set, $S_T = \{C_0, C_1, \ldots, C_N\}$. The one-hot encoding technique is used to encode the individual state as a node feature (see Fig. 2).

b. Structure of temporal networks. The aggregated network $\tilde{G}_a(V, E)$ is a superposition of all slices in the temporal network $\tilde{G}$, containing any edge which appears in at least one slice. The adjacent matrix $A_a$ of $\tilde{G}_a$ represents the static topology properties of interactions between nodes, but cannot provide temporal properties depending on the times when interactions are active. An additional feature vector $X_a$, of dimension equal to the length of the sequence $\{\tilde{G}_0, \tilde{G}_1, \ldots, \tilde{G}_T\}$, is attached to each edge $e$ to record its activation pattern (see Fig. 2). The set of all edge features is $X_a = \{X_e \mid \forall e \in E\}$.

**Backtracking Network**

We tailor a simple graph neural network focusing on source detection, called backtracking network (BN), as shown in Fig. 2. Compared with the spreading dynamic which drives the system from an initial state forward to its final state, the role of BN is to approximate an inverse function mapping the final state back to its initial state: $S_0 = \text{BN} \left( S_T, \tilde{G} \right)$. Given conditions $S_T$, $A_a$ and $X_a$, the BN computes with
the kernel-based convolutional operator (Gilmer et al. 2017; Simonovsky and Komodakis 2017):

\[ v \rightarrow e : \quad g_{(i,j)}^{l+1} = f^e \left( g_{(i,j), h}^l \right), \]

\[ e \rightarrow v : \quad h_i^{l+1} = f^v \left( h_i^l + \sum_{j \in N(i)} g_{(i,j)}^{l+1} \right). \]

where \( g_{(i,j)}^l \) and \( h_i^l \) are the hidden features of edge \((i, j)\) and node \(i\) at layer \(l\) respectively. Initially, \( g_{(i,j)}^0 = p^e(X_{(i,j)}) \) and \( h_i^0 = p^v(C_i) \), where \( p^e/p^v \) is the projection layer. The message function \( f^e \) delivers the information on node to the edge originating from it. The update function \( f^v \) integrates the information about disease states of neighbors and activation patterns of their contacts. \( f^e \) and \( f^v \) are represented by two independent fully-connected layers with activation function ReLU. The objective function is formulated as:

\[ \mathcal{L} = - \sum_{i=1}^{N} y_i \log \frac{\exp(h_i)}{\sum_{j=1}^{N} \exp(h_j)}, \]

where \( h_i \in \mathbb{R}^1 \) is the return of another projection layer following the gnns-based layers, and label \( y_i = 1 \) if node \(i\) is the real source else \( y_i = 0 \). The softmax function inside the log function maps \( h_i \) to the detection probability of node \(i\) being the source.

**Expert Knowledge**

Expert knowledge can complement machine, improving performance by injecting human prior knowledge into the machine reasoning process, which is particularly valuable in limited sample scenarios (Raisi, Perdikaris, and Karniadakis 2019; Hao et al. 2022). In SIR model, it is obvious that individuals whose states are susceptible at final moment are certainly not the source. If an individual is the source being infectious at initial moment, his state will not transition to be susceptible (see Eq. 1-2). For humans, this knowledge is easy to obtain because we know the mechanism of the contagion process underlying the data generation whereas the machine does not. What BN learns is that those susceptible individuals have never been the sources in training samples (statistical association – thus gives them low detection probabilities), not that they cannot be the sources (spreading mechanism – these probabilities should be zero). As the sample size increases, the given probabilities get close to zero gradually. However, it may cause the BN to make wrong inferences when sample size is not sufficient enough. Therefore, we add a huge negative value on the susceptible individuals to force their detection probabilities to become zero after applying softmax function according to:

\[ h_s \leftarrow h_s - \infty. \]

Then, \( h_s \) is the final output on susceptible node \(s\) combined with expert knowledge. The overall framework of our method for source detection is summarized as Algorithm 1.

**Experiment**

We evaluate the performance of the proposed method on five real temporal networks, check its robustness in two scenarios (statistical association – thus gives them low detection probabilities), not that they cannot be the sources (spreading mechanism – these probabilities should be zero). As the sample size increases, the given probabilities get close to zero gradually. However, it may cause the BN to make wrong inferences when sample size is not sufficient enough. Therefore, we add a huge negative value on the susceptible individuals to force their detection probabilities to become zero after applying softmax function according to:

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Algorithm 1: Inference of patient zero

**Input:** Final snapshot of spreading in population \( S_T \), epidemic model e.g. SIR, estimated start interval of propagation, backtracking network BN

**Output:** Patient zero

1. Generate training set with size \(M\).
2. \textbf{while} \( M \) has not meet \textbf{do}
3. \textbf{end while}
4. \textbf{end while}
5. Collect the final snapshot and patient zero as a pair of sample and label.
6. \textbf{return} Patient zero in \( S_T \) inferred by BN

**Experiment Steps**

**Temporal networks.** Statistics of the following five networks are provided in Tab. 3: (a) Sexual contact (Rocha, Liljeros, and Holme 2011), is an empirical temporal network of sexual contacts in Brazil; (b) Hospital (Isella et al. 2011), contains contacts among patients and health-care workers in a hospital ward in Lyon, France; (c) European email (Leskovec, Kleinberg, and Faloutsos 2007), is generated using email data from a large European research institution; (d) Bitcoin (Kumar et al. 2016), is a who-trusts-whom network of people who trade using Bitcoin on a platform called Bitcoin OTC; (e) Message (Panzarasa, Opsahl, and Carley 2009), comprises private messages sent on an online social network at the University of California, Irvine. The two face-to-face networks, Sexual contact and Hospital, are undirected, while others are directed and transmission only occurs along the direction of an edge.

**Datasets.** We generate 20,000 samples (19,600/200/200 for training/validation/test) for each temporal network by using the SIR model with two parameter combinations of mean infection and recovery rate (\(\tilde{p} = 0.3, \tilde{q} = 0.01\) and

<table>
<thead>
<tr>
<th>Sex</th>
<th>Hospital</th>
<th>Eu email</th>
<th>Bitcoin</th>
<th>Message</th>
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<td>N</td>
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Table 1: Statistics of real temporal networks. \(\langle k\rangle\) and \(\langle k_a\rangle\) is the mean degree in slice and aggregate networks respectively. Times are given in days.
where the vectors $\tilde{r}_s$ and $\tilde{r}_{i,m}$ record the state of the population in the real snapshot and $m$-th simulated one with individual $i$ as source. $\varphi$ is the Jaccard similarity function $\varphi : \mathbb{R}^N \times \mathbb{R}^N \rightarrow [0, 1]$ given by the ratio of the size of the intersection of the sets of infected individuals in $\tilde{r}_s$ and $\tilde{r}_i$ to the size of their union; (f) Soft Margin Monte Carlo estimator with exact start time (SMT). All methods share test sets.

**Evaluation metrics.** Under each evaluation metric, a success is as follows: (a) Top-1. The real patient zero is the individual with maximal inferred probability to be patient zero; (b) Top-5. The real patient zero is among the five individuals with the highest inferred probability to be patient zero; (c) Hop-1. The topological distance between real and inferred patient zero on the aggregate network $G_a$ is less than or equal to one. In other words, the inferred patient zero is within one hop of the true patient zero (either the true patient zero or the true patient zero’s direct neighbor).

**Training details.** We train BN by the ADAM (Kingma and Ba 2015) optimizer with learning rate of $10^{-3}$ (we report the variation of performance with the number of layers in Results). The batch size is 128 and training epoch is 200. We compose our code on PyTorch framework and run all experiments in a local machine with two NVIDIA Tesla V100 32GB GPUs.

**Results.**

On all datasets, the performance of our gnn-based method is significantly superior (see Tab. 2) to SM and SMT, which for Top-5 only achieves accuracy above 0.6 on the small-scale Hospital network, with 75 nodes. The failure of SM and SMT indicates the similarity between the snapshots generated by multiple simulations on the same patient zero is not distinctly higher than the similarity for distinct patient zeros with small topological distance on the temporal network. The superiority of SMT (i.e. SM with exact start time) to SM shows that even if the spreading origins from the same patient zero, starting a few days earlier or later results in different epidemic processes and final snapshots. We find that the accuracy of BN is usually better than that of BNW in metric Top-1. When BNW recognizes as suspicious a set of individuals including both the true patient zero and susceptible individuals, BNW (without expert knowledge) needs more features than BN to exclude the susceptible individuals.

We check the effect of receptive fields of nodes on BN’s performance. As the number of layers (one layer comprises both Eq. 2 and Eq. 3) increases, the node can gather information from its neighbors with farther topological distance, i.e., the receptive field becomes larger. Taking epidemic spreading on sexual contact network as an example, the variation of performance with a number of layers from 1 to 7 is shown in Tab.3. We find the performance approaches its maximum when the number of layers is 5, and further expanding the receptive field provides no obvious improvement to the performance. In other datasets, the performance even declines since the information gathered on adjacent nodes become homogeneous as their receptive field becomes too large.

![Figure 3: Distribution of final number of affected individuals in datasets. The value on abscissa represents the final number of Infectious + Recovered individuals, among whom we infer the single patient zero. There are 20,000 independent samples in each dataset.](image-url)
Table 2: Performance comparison using dataset from SIR model with mean infection and recovery rates (top: $\bar{p} = 0.3$, $\bar{q} = 0.01$; bottom: $\bar{p} = 0.8$, $\bar{q} = 0.05$) on five real temporal networks. Each element contains three values representing the accuracy in metric Top-1/Top-5/Hop-1 respectively.

Table 3: Performance versus receptive field of node on dataset of sexual contact. In column $L_n$, BN uses $n$ layers.

Robustness

We design two more practical scenarios in which spreading information is missing, as shown in Fig. 4. (a) Links missing. The incomplete network structure generates fictitious temporal patterns of contacts and activity rhythms of individuals in $\hat{G}$. The original propagation paths are obscured and clues to infer by whom patients are infected became blurred. To investigate this, we adjust the proportion of missing links from mild to severe, and remove the links randomly from each slice of the temporal network. (b) Partial observation. Only a fraction of node states in final state $S_T$ is observed. This leads to four classes of individual states in $S_T$: susceptible, infectious, recovered and unknown. Confused by the unobserved individuals, we even fail to judge the final number of affected individuals. In this case, the problem is expressed as: inferring $S_0$ given $\{S_T, \hat{G}\}$. Concretely, we adjust the proportion of observed nodes from dense to sparse, and select observed nodes randomly from the population. Taking epidemic spreading on sexual contact network as an example, the robustness of our algorithm is shown in Fig. 5. The faster decline in the first scenario supports the assertion that the underlying structure of the temporal network has a drastic impact on spreading dynamics (Holme and Saramäki 2012; Bansal et al. 2010). When the information about network structure is insufficient, BN is challenged to establish correctly the association between the final state and initial state which represents the inversion of spreading dynamics. In contrast, partial observation has a substantially weaker influence on inference via BN. Even if eighty percent of final states are unknown, BN still achieves around 0.7 accuracy according to the metric Top-5.

Topological Insight into the Interior of BN

To give some insight into the implicit inverse association $S_0 = \text{BN} \big( S_T, \hat{G} \big)$, we analyze from this perspective: what are the common characteristics among the individuals which BN assigns top probability of being the source? We visualize two cases of the final snapshot of the epidemic on temporal network of sex contacts, and observe that the individ-
Figure 5: Robustness to missing information. The values on the abscissa represent the proportion of either missing links (ml) or unobserved individuals (ui). The filled areas indicate the gap of robustness between two scenarios.

Figure 6: The role of patient zero plays in spreading process (a) Passerby and (b) Participant. The five nodes given top probabilities are enlarged in size and filled with different shades of red. The two local aggregated networks shown here only contains the second-order inner neighbors of patient zero whose states are infectious or recovered in the final snapshot.

Figure 7: Quantification of match between patient zero and nodes given top inferred probability (a) Mean similarity of activity sequence and (b) MAD of k-shell and degree on aggregated network $G_a$.

Our research involves backtracking the spreading of epidemics on temporal networks and inferring patient zero with the help of artificial intelligence. The gnn-based method we propose opens a novel path to deal with this kind of inverse problem in random environments. We show that this problem is solved efficiently by a gnn-based method even in the case of missing information about network structure and node states.

Source detection is not only restricted to epidemiology, but extends to other fields such as rumor in sociology and pollution in ecology. The emergency of any of these phenomena will lead to confusion in the local area, and locating the source is crucial for subsequent interventions to eradicate negative events. The proposed method can be easily transferred to solve these problems. Moreover, the inference of patient zero is just a special case of initial state inference for complex systems the entities of which can have a diverse mixture of states described by a mixture of discrete and continuous values, and many important scientific questions can be formulated in this way. Hence, extending our research to inference of more general types of initial states is a interesting direction.

Conclusion

Our research involves backtracking the spreading of epidemics on temporal networks and inferring patient zero with the help of artificial intelligence. The gnn-based method we propose opens a novel path to deal with this kind of inverse problem in random environments. We show that this problem is solved efficiently by a gnn-based method even in the case of missing information about network structure and node states.

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Ethics Statement

Our problem entails privacy and ethical concerns: the identity of spreading sources, and the data which would allow identification of these sources, should be kept safe.

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