Learning Action Translator for Meta Reinforcement Learning on Sparse-Reward Tasks

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Abstract

Meta reinforcement learning (meta-RL) aims to learn a policy solving a set of training tasks simultaneously and quickly adapting to new tasks. It requires massive amounts of data drawn from training tasks to infer the common structure shared among tasks. Without heavy reward engineering, the sparse rewards in long-horizon tasks exacerbate the problem of sample efficiency in meta-RL. Another challenge in meta-RL is the discrepancy of difficulty level among tasks, which might cause one easy task dominating learning of the shared policy and thus preclude policy adaptation to new tasks. This work introduces a novel objective function to learn an action translator among training tasks. We theoretically verify that the value of the transferred policy with the action translator can be close to the value of the source policy and our objective function (approximately) upper bounds the value difference. We propose to combine the action translator with context-based meta-RL algorithms for better data collection and more efficient exploration during meta-training. Our approach empirically improves the sample efficiency and performance of meta-RL algorithms on sparse-reward tasks.

1 Introduction

Deep reinforcement learning (DRL) methods achieved remarkable success in solving complex tasks (Mnih et al. 2015; Silver et al. 2016; Schulman et al. 2017). While conventional DRL methods learn an individual policy for each task, meta reinforcement learning (meta-RL) algorithms (Finn, Abbeel, and Levine 2017; Duan et al. 2016; Mishra et al. 2017) learn the shared structure across a distribution of tasks so that the agent can quickly adapt to unseen related tasks in the test phase. Unlike most of the existing meta-RL approaches working on tasks with dense rewards, we instead focus on the sparse-reward training tasks, which are more common in real-world scenarios without access to carefully designed reward functions in the environment. Recent works in meta-RL propose off-policy algorithms (Rakelly et al. 2019; Fakoor et al. 2019) and model-based algorithms (Nagabandi, Finn, and Levine 2018; Nagabandi et al. 2018) to improve the sample efficiency in meta-training procedures. However, it remains challenging to efficiently solve multiple tasks that require reasoning over long horizons with sparse rewards. In these tasks, the scarcity of positive rewards exacerbates the issue of sample efficiency, which plagues meta-RL algorithms and makes exploration difficult due to a lack of guidance signals.

Intuitively, we hope that solving one task facilitates learning of other related tasks since the training tasks share a common structure. However, it is often not the case in practice (Rusu et al. 2015; Parisotto, Ba, and Salakhutdinov 2015). Previous works (Teh et al. 2017; Yu et al. 2020a) point out that detrimental gradient interference might cause an imbalance in policy learning on multiple tasks. Policy distillation (Teh et al. 2017) and gradient projection (Yu et al. 2020a) are developed in meta-RL algorithms to alleviate this issue. However, this issue might become more severe in the sparse-reward setting because it is hard to explore each task to obtain meaningful gradient signals for policy updates. Good performance in one task does not automatically help exploration on the other tasks since the agent lacks positive rewards on the other tasks to learn from.

In this work, we aim to fully exploit the highly-rewarding transitions occasionally discovered by the agent in the exploration. The good experiences in one task should not only improve the policy on this task but also benefit the policy on other tasks to drive deeper exploration. Specifically, once the agent learns from the successful trajectories in one training task, we transfer the good policy in this task to other tasks to
get more positive rewards on other training tasks. In Fig. 1, if the learned policy $\pi$ performs better on task $T_{(2)}$ than other tasks, then our goal is to transfer the good policy $\pi(\cdot, T_{(2)})$ to other tasks $T_{(1)}$ and $T_{(3)}$. To enable such transfer, we propose to learn an action translator among multiple training tasks. The objective function forces the translated action to behave on the target task similarly to the source action on the source task. We consider the policy transfer for any pair of source and target tasks in the training task distribution (see the colored arrows in Fig. 1). The agent executes actions following the transferred policy if the transferred policy attains higher rewards than the learned policy on the target task in recent episodes. This approach enables the agent to leverage relevant data from multiple training tasks, encourages the learned policy to perform similarly well on multiple training tasks, and thus leads to better performance when applying the well-trained policy to test tasks.

We summarize the contributions: (1) We introduce a novel objective function to transfer any policy from a source Markov Decision Process (MDP) to a target MDP. We prove a theoretical guarantee that the transferred policy can achieve the expected return on the target MDP close to the source policy on the source MDP. The difference in expected returns is (approximately) upper bounded by our loss function with a constant multiplicative factor. (2) We develop an off-policy RL algorithm called Meta-RL with Context-conditioned Action Translator (MCAT), applying a policy transfer mechanism in meta-RL to help exploration across multiple sparse-rewards tasks. (3) We empirically demonstrate the effectiveness of MCAT on a variety of simulated control tasks with the MuJoCo physics engine (Todorov, Erez, and Tassa 2012), showing that policy transfer improves the performance of context-based meta-RL algorithms.

2 Related Work

Context-based Meta-RL Meta reinforcement learning has been extensively studied in the literature (Finn, Abbeel, and Levine 2017; Stadie et al. 2018; Sung et al. 2017; Xu, van Hasselt, and Silver 2018) with many works developing the context-based approaches (Rakelly et al. 2019; Ren et al. 2020; Liu et al. 2020). Duan et al. (2016); Wang et al. (2016); Fakoor et al. (2019) employ recurrent neural networks to encode context transitions and formulate the policy conditioning on the context variables. The objective function of maximizing expected return trains the context encoder and policy jointly. Rakelly et al. (2019) leverage a permutation-invariant encoder to aggregate experiences as probabilistic context variables and optimizes it with variational inference. The posterior sampling is beneficial for exploration on sparse-reward tasks in the adaptation phase, but there is access to dense rewards during training phase. Li, Pinto, and Abbeel (2020) considers a task-family of reward functions. Lee et al. (2020); Seo et al. (2020) trains the context encoder with forward dynamics prediction. These model-based meta-RL algorithms assume the reward function is accessible for planning. In the sparse-reward setting without ground-truth reward functions, they may struggle to discover non-zero rewards and accurately estimating the reward for model-based planning may be problematic as well.

Policy Transfer in RL Policy transfer studies the knowledge transfer in target tasks given a set of source tasks and their expert policies. Policy distillation (Rusu et al. 2015; Yin and Pan 2017; Parisotto, Ba, and Salakhutdinov 2015) minimize the divergence of action distributions between the source policy and the learned policy on the target task. Along this line of works, Teh et al. (2017) create a centroid policy in multi-task reinforcement learning and distills the knowledge from the task-specific policies to this centroid policy. Alternatively, inter-task mapping between the source and target tasks (Zhu, Lin, and Zhou 2020) can assist the policy transfer. Most of these works (Gupta et al. 2017; Konidaris and Barto 2006; Ammar and Taylor 2011) assume existence of correspondence over the state space and learn the state mapping between tasks. Recent work (Zhang et al. 2020c) learns the state correspondence and action correspondence with dynamic cycle-consistency loss. Our method differs from this approach, in that we enable action translation among multiple tasks with a simpler objective function. Importantly, our approach is novel to utilize the policy transfer for any pair of source and target tasks in meta-RL.

Bisimulation for States in MDPs Recent works on state representation learning (Ferns, Panangaden, and Precup 2004; Zhang et al. 2020a; Agarwal et al. 2021) investigate the bisimilarity metrics for states on multiple MDPs and consider how to learn a representation for states leading to almost identical behaviors under the same action in diverse MDPs. In multi-task reinforcement learning and meta reinforcement learning problems, Zhang et al. (2020a, b) derives transfer and generalization bounds based on the task and state similarity. We also bound the value of policy transfer across tasks but our approach is to establish action equivalence instead of state equivalence.

3 Method

In this section, we first describe our approach to learn a context encoder capturing the task features and learn a forward dynamics model predicting next state distribution given the task context (Sec. 3.2). Then we introduce an objective function to train an action translator so that the translated action on the target task behaves equivalently to the source action on the source task. The action translator can be conditioned on the task contexts and thus it can transfer a good policy from any arbitrary source task to any other target task in the training set (Sec. 3.3). Finally, we propose to combine the action translator with a context-based meta-RL algorithm to transfer the good policy from any one task to the others. During meta-training, this policy transfer approach helps exploit the good experiences encountered on any one task and benefits the data collection and further policy optimization on other sparse-reward tasks (Sec. 3.4). Fig. 2 provides an overview of our approach MCAT.

3.1 Problem Formulation

Following meta-RL formulation in previous work (Duan et al. 2016; Mishra et al. 2017; Rakelly et al. 2019), we assume a distribution of tasks $p(T)$ and each task is a Markov decision process (MDP) defined as a tuple $(S, A, p, r, \gamma, \rho_0)$.
Figure 2: Overview of MCAT. (a) We use forward dynamics prediction loss to train the context encoder $C$ and forward model $F$. (b) We regularize the context encoder $C$ with the contrastive loss, so context vectors of transition segments from the same task cluster together. (c) With fixed $C$ and $F$, we learn the action translator $H$ for any pair of source task $T^{(i)}$ and target task $T^{(j)}$. The action translator aims to generate action $\tilde{a}^{(i)}$ on the target task leading to the same next state $s^{(j)}_{t-1}$ as the source action $a^{(j)}_t$ on the source task. (d) With fixed $C$, we learn the critic $Q$ and actor $\pi$ conditioning on the context feature. (e) If the agent is interacting with the environment on task $T^{(i)}$, we compare learned policy $\pi(s, z^{(j)})$ and transferred policy $H(s, \pi(s, z^{(j)}), z^{(j)}_t)$, which transfers a good policy $\pi(s, z^{(j)})$ on source task $T^{(i)}$ to target task $T^{(j)}$. We select actions according to the policy with higher average episode rewards in the recent episodes. Transition data are pushed into the buffer. We remark that the components $C$, $F$, $H$, $Q$, $\pi$ are trained alternatively not jointly and this fact facilitates the learning process.

with state space $S$, action space $A$, transition function $p(s'|s, a)$, reward function $r(s, a, s')$, discounting factor $\gamma$, and initial state distribution $\rho_0$. We can alternatively define the reward function as $r(s, a) = \sum_{s'} p(s'|s, a)r(s, a, s')$. In context-based meta-RL algorithms, we learn a policy $\pi(s, z^{(j)}_t)$ shared for any task $T^{(i)} \sim p(T)$, where $t$ denotes the timestep, $i$ denotes the index of a task, the context variable $z^{(j)}_t \in Z$ captures contextual information from history transitions on the task MDP and $Z$ is the space of context vectors. The shared policy is optimized to maximize its value $V^\pi(T^{(i)}) = \mathbb{E}_{p(s, a, r|T^{(i)})} \left[ \sum_{t=0}^{\infty} \gamma^t r_t \right]$ on each training task $T^{(i)}$. Following prior works in meta-RL (Yu et al. 2017; Nagabandi et al. 2018; Nagabandi, Finn, and Levine 2018; Zhou, Pinto, and Gupta 2019; Lee et al. 2020), we study tasks with the same state space, action space, reward function but varying dynamics functions. Importantly, we focus on more challenging setting of sparse rewards. Our goal is to learn a shared policy robust to the dynamic changes and generalizable to unseen tasks.

### 3.2 Learning Context & Forward Model

In order to capture the knowledge about any task $T^{(i)}$, we leverage a context encoder $C : S^K \times A^K \rightarrow Z$, where $K$ is the number of past steps used to infer the context. Related ideas have been explored by (Rakelly et al. 2019; Zhou, Pinto, and Gupta 2019; Lee et al. 2020). In Fig. 2a, given $K$ past transitions $(s^{(i)}_{t-K}, a^{(i)}_{t-K}, \ldots, s^{(i)}_{t-1}, a^{(i)}_{t-1})$, context encoder $C$ produces the latent context $z^{(i)}_t = C(s^{(i)}_{t-K}, a^{(i)}_{t-K}, \ldots, s^{(i)}_{t-2}, a^{(i)}_{t-2}, s^{(i)}_{t-1}, a^{(i)}_{t-1})$. We train the context encoder $C$ and forward dynamics $F$ with an objective function to predict the forward dynamics in future transitions $s^{(i)}_{t+m}$ ($1 \leq m \leq M$) within $M$ future steps. The state prediction in multiple future steps drives latent context embeddings $z^{(i)}_{t}$ to be temporally consistent. The learned context encoder tends to capture dynamics-specific, contextual information (e.g. environment physics parameters). Formally, we minimize the negative log-likelihood of observing the future states under dynamics prediction.

\[
\mathcal{L}_{\text{forward}} = -\sum_{m=1}^{M} \log F(s^{(i)}_{t+m}|s^{(i)}_t, a^{(i)}_t, z^{(i)}_{t-1})
\]  

Additionally, given trajectory segments from the same task, we require their context embeddings to be similar, whereas the contexts of history transitions from different tasks should be distinct (Fig. 2b). We propose a contrastive loss (Hadsell, Chopra, and LeCun 2006) to constrain embeddings within a small distance for positive pairs (i.e. samples from the same task) and push embeddings apart with a distance greater than a margin value $m$ for negative pairs (i.e. samples from different tasks). $z^{(i)}_{t1}$, $z^{(i)}_{t2}$ denote context embeddings of two trajectory samples from $T^{(i)}$, $T^{(j)}$. The contrastive loss function is defined as:

\[
\mathcal{L}_{\text{contrastive}} = \min_{m, z^{(i)}_{t1}, z^{(i)}_{t2}} \{ z^{(i)}_{t1} \in Z, z^{(i)}_{t2} \in Z \} \mathcal{L}(m, z^{(i)}_{t1}, z^{(i)}_{t2})
\]  

where $\mathcal{L}(m, z^{(i)}_{t}, z^{(i)}_{t'})$ is the contrastive loss function. The contrastive loss function is defined as:

\[
\mathcal{L}(m, z^{(i)}_{t}, z^{(i)}_{t'}) = \begin{cases} 
0 & \text{if } |z^{(i)}_{t} - z^{(i)}_{t'}| < m \\
\exp \left( \frac{|z^{(i)}_{t} - z^{(i)}_{t'}|}{\sigma} \right) & \text{otherwise}
\end{cases}
\]  

where $\sigma$ is a temperature parameter. The contrastive loss function is defined as:

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0 & \text{if } |z^{(i)}_{t} - z^{(i)}_{t'}| < m \\
\exp \left( \frac{|z^{(i)}_{t} - z^{(i)}_{t'}|}{\sigma} \right) & \text{otherwise}
\end{cases}
\]  

where $\sigma$ is a temperature parameter. The contrastive loss function is defined as:
We aim to learn an action translator \( H : S \times A \times Z \times Z \to A \). \( \hat{a}^{(i)} = H(s^{(i)}_t, a^{(i)}_t, z^{(i)}_t, z^{(i)}_t) \) translates the proper action \( a^{(i)}_t \) from source task \( T^{(i)} \) to target task \( T^{(j)} \). In Fig. 2c, if we start from the same state \( s^{(i)}_t \) on both source and target tasks, the translated action \( \hat{a}^{(i)} \) on target task should behave equivalently to the source action \( a^{(i)}_t \) on the source task. Thus, the next state \( s^{(i)}_{t+1} \sim p^{(j)}(s^{(i)}_{t+1} | s^{(i)}_t, \hat{a}^{(i)}_t) \) produced from the transferred action \( \hat{a}^{(i)}_t \) on the target task should be close to the real next state \( s^{(i)}_{t+1} \) gathered on the source task. The objective function of training the action translator \( H \) is to maximize the probability of getting next state \( s^{(i)}_{t+1} \) under the next state distribution \( s^{(i)}_{t+1} \sim p^{(j)}(s^{(i)}_{t+1} | s^{(i)}_t, \hat{a}^{(i)}_t) \) on the target task. Because the transition function \( p^{(j)}(s^{(i)}_{t+1} | s^{(i)}_t, \hat{a}^{(i)}_t) \) is unavailable and might not be differentiable, we use the forward dynamics model \( F(s^{(i)}_t, \hat{a}^{(i)}_t, z^{(i)}_t) \) to approximate the transition function.

We formulate objective function for action translator \( H \) as:

\[
\mathcal{L}_{\text{trans}} = -\log F(s^{(j)}_{t+1}, \hat{a}^{(i)}_t, z^{(i)}_t)
\]

where \( \hat{a}^{(i)}_t = H(s^{(i)}_t, a^{(i)}_t, z^{(i)}_t, z^{(i)}_t) \). We assume to start from the same initial state, the action translator is to find the action on the target task so as to reach the same next state as the source action on the source task. This intuition to learn the action translator is analogous to learn inverse dynamic model across two tasks.

With a well-trained action translator conditioning on task features \( z^{(j)}_t \) and \( z^{(i)}_t \), we transfer the good deterministic policy \( \pi(s, z^{(j)}_t) \) from any source task \( T^{(j)} \) to any target task \( T^{(i)} \). When encountering a state \( s^{(i)}_t \) on \( T^{(i)} \), we query a good action \( a^{(i)}_t = \pi(s^{(i)}_t, z^{(i)}_t) \) which will lead to a satisfactory next state with high return on the source task. Then \( H \) translates this good action \( a^{(j)}_t \) on the source task to action \( \hat{a}^{(i)}_t = H(s^{(i)}_t, a^{(j)}_t, z^{(i)}_t, z^{(i)}_t) \) on the target task. Executing the translated action \( \hat{a}^{(i)}_t \) moves the agent to a next state on the target task similarly to the good action on the source task. Therefore, transferred policy \( \hat{H}(s^{(i)}_t, \pi(s^{(i)}_t, z^{(i)}_t), z^{(i)}_t, z^{(i)}_t) \) can behave similarly to source policy \( \pi(s, z^{(j)}_t) \). Sec. 5.1 demonstrates the performance of transferred policy in a variety of environments. Our policy transfer mechanism is related to the action correspondence discussed in (Zhang et al. 2020c). We extend their policy transfer approach across two domains to multiple domains(tasks) and theoretically validate learning of action translator in Sec. 4.

### 3.4 Combining with Context-based Meta-RL

MCAT follows standard off-policy meta-RL algorithms to learn a deterministic policy \( \pi(s_t, z^{(i)}_t) \) and a value function \( Q(s_t, a_t, z^{(i)}_t) \), conditioning on the latent task context variable \( z^{(i)}_t \). In the meta-training process, using data sampled from \( B_i \), we train the context model \( C \) and dynamics model \( F \) with \( \mathcal{L}_{\text{forw}} \) and \( \mathcal{L}_{\text{cont}} \) to accurately predict the next state (Fig. 2a 2b). With the fixed context encoder \( C \) and dynamics model \( F \), the action translator \( H \) is optimized to minimize \( \mathcal{L}_{\text{trans}} \) (Fig. 2c). Then, with the fixed \( C \), we train the context-conditioned policy \( \pi \) and value function \( Q \) according to \( \mathcal{L}_{\text{RL}} \) (Fig. 2d). In experiments, we use the objective function \( \mathcal{L}_{\text{RL}} \) from TD3 algorithm (Fujimoto, Hoof, and Meger 2018). See pseudo-code of MCAT in Appendix B.

On sparse-reward tasks where exploration is challenging, the agent might luckily find transitions with high rewards on one task \( T^{(i)} \). Thus, the policy learning on this task might be easier than other tasks. If the learned policy \( \pi \) performs better on one task \( T^{(j)} \) than another task \( T^{(i)} \), we consider the policy transferred from \( T^{(j)} \) to \( T^{(i)} \). At a state \( s^{(i)}_t \), we employ the action translator to get a potentially good action \( H(s^{(i)}_t, \pi(s^{(i)}_t, z^{(i)}_t), z^{(i)}_t, \pi^{(j)}(s^{(j)}_t)) \) on target task \( T^{(j)} \). As illustrated in Fig. 2e and Fig. 1, in the recent episodes, if the transferred policy earns higher scores than the learned policy \( \pi(s^{(i)}_t, z^{(i)}_t) \) on the target task \( T^{(i)} \), we follow the translated actions on \( T^{(j)} \) to gather transition data in the current episode. These data with better returns are pushed into the replay buffer \( B^{(j)} \) and produce more positive signals for policy learning in the sparse-reward setting. These transition samples help improve \( \pi \) on \( T^{(j)} \) after policy update with off-policy RL algorithms. As described in Sec. 3.3, our action translator \( H \) allows policy transfer across any pair of tasks. Therefore, with the policy transfer mechanism, the learned policy on each task might benefit from good experiences and policies on any other tasks.

### 4 Theoretical Analysis

In this section, we theoretically support our objective function (Equation 3) to learn the action translator. Given \( s \) on two MDPs with the same state and action space, we define that action \( a^{(i)}_t \) on \( T^{(i)} \) is equivalent to action \( a^{(j)}_t \) on \( T^{(j)} \) if the actions yielding exactly the same next state distribution and reward, i.e. \( p^{(i)}(s, a^{(i)}_t) = p^{(j)}(s, a^{(j)}_t) \) and \( r^{(i)}(s, a^{(i)}_t) = r^{(j)}(s, a^{(j)}_t) \). Ideally, the equivalent action always exists on the target MDP \( T^{(j)} \) for any state-action pair on the source MDP \( T^{(i)} \) and there exists an action translator function \( H : S \times A \to A \) to identify the exact equivalent action. Starting from state \( s \), the translated action \( \hat{a} = H(s, a) \) on the task \( T^{(i)} \) generates reward and next state distribution the same as action \( a \) on the task \( T^{(j)} \). Then any deterministic policy \( \pi^{(i)}(s) \) on the source task \( T^{(j)} \) can be perfectly transferred to the target task \( T^{(i)} \) with \( \pi^{(i)}(s) = H(s, \pi^{(j)}(s)) \). The value of the policy \( \pi^{(i)}(s) \) on the source task \( T^{(j)} \) is equal to the value of transferred policy \( \pi^{(i)}(s) \) on the target task \( T^{(i)} \).
Without the assumption of existence of a perfect correspondence for each action, given any two deterministic policies \( \pi^{(j)} \) on \( T^{(j)} \) and \( \pi^{(i)} \) on \( T^{(i)} \), we prove that the difference in the policy value is upper bounded by a scalar \( \frac{1}{\gamma} \) depending on \( L_1 \)-distance between reward functions \( |r^{(j)}(s, \pi^{(j)}(s)) - r^{(j)}(s, \pi^{(j)}(s))| \) and total-variation distance between next state distributions \( D_{TV}(p^{(j)}(\cdot|s, \pi^{(j)}(s)), p^{(j)}(\cdot|s, \pi^{(j)}(s))) \). Detailed theorem (Theorem 1) and proof are in Appendix A.

For a special case where reward function \( r(s, a, s') \) only depends on the current state \( s \) and next state \( s' \), the upper bound of policy value difference is only related to the distance in next state distributions.

Proposition 1 Let \( T^{(i)} = \{S, A, p^{(i)}(r^{(i)}, \gamma, \rho_0) \} \) and \( T^{(j)} = \{S, A, p^{(j)}(r^{(j)}, \gamma, \rho_0) \} \) be two MDPs sampled from the distribution of tasks \( p(T) \). \( \pi^{(i)} \) and \( \pi^{(j)} \) is the deterministic policy on \( T^{(i)} \) and \( T^{(j)} \). Assume the reward function only depends on the state and next state \( r^{(i)}(s, a^{(i)}(s)) = r^{(j)}(s, a^{(j)}(s')) \). Let \( d = \sup_{s \in S} 2MD_{TV}(p^{(i)}(\cdot|s, \pi^{(i)}(s)), p^{(j)}(\cdot|s, \pi^{(j)}(s))) \) and \( M = \sup_{s \in S} p^{(i)}(\cdot|s, \pi^{(i)}(s)) \). We have

\[
\left| V^{\pi^{(i)}}(s, T^{(i)}) - V^{\pi^{(j)}}(s, T^{(j)}) \right| \leq \frac{d}{1 - \gamma} \tag{4}
\]

According to Proposition 1, if we can optimize the action translator \( H \) to minimize \( d \) for policy \( \pi^{(j)} \) and \( \pi^{(i)}(s) = H(s, \pi^{(j)}(s)) \), the value of the transferred policy \( \pi^{(i)} \) on the target task can be close to the value of source policy \( \pi^{(j)} \). In many real-world scenarios, especially sparse-reward tasks, the reward heavily depends on the state and next state instead of action. For example, robots running forward receive rewards according to their velocity (i.e. the location difference between the current and next state within one step); robot arms manipulating various objects earn positive rewards only when they are in the target positions. Thus, our approach focuses on the cases with reward function approximately as \( r(s, s') \) under the assumption of Proposition 1. For any state \( s \in S \), we minimize the total-variation distance between two next state distributions \( D_{TV}(p^{(j)}(\cdot|s, \pi^{(j)}(s))), p^{(j)}(\cdot|s, \pi^{(j)}(s))) \) on source and target MDPs. Besides, we discuss the policy transfer for tasks with a general reward function in Appendix C.3.

There is no closed-form solution of \( D_{TV} \) and \( D_{TV} \) is related with Kullback–Leibler (KL) divergence \( D_{KL} \) by the inequality \( D_{TV}(p||q)^2 \leq D_{KL}(p||q) \). Thus, we instead consider minimizing \( D_{KL} \) between two next state distributions. \( D_{KL}(p^{(j)}(\cdot|s', \pi^{(j)}(s'))) = -\sum_{s'} p^{(j)}(\cdot|s', \pi^{(j)}(s')) \log p^{(j)}(\cdot|s') + \sum_{s'} p^{(j)}(\cdot|s', \pi^{(j)}(s')) \log p^{(j)}(\cdot|s') \). The second term does not involve \( H \) and thus can be viewed as a constant term when optimizing \( H \). We focus on minimizing the first term \( -\sum_{s'} p^{(j)}(\cdot|s', \pi^{(i)}(s')) \log F(s'|s, \pi^{(i)}(s)) \). We sample transitions \( s, \pi^{(j)}(s), s' \) from the source task. \( s' \) follows the distribution \( p^{(i)}(\cdot|s', \pi^{(j)}(s')) \). Thus, minimizing the negative log-likelihood of observing the next state \( L_{trans} = -\log F(s'|s, \pi^{(j)}(s)) \) is to approximately minimize \( D_{KL} \). Experiments in Sec. 5.1 suggest that this objective function works well for policy transfer across two MDPs. Sec. 3.3 explains the motivation behind \( L_{trans} \) (Equation 3) to learn an action translator among multiple MDPs instead of only two MDPs.

## 5 Experiment

We design and conduct experiments to answer the following questions: (1) Does the transferred policy perform well on the target task (Tab. 1, Fig. 4)? (2) Can we transfer the good policy for any pair of source and target tasks (Fig. 5)? (3) Does policy transfer improve context-based Meta-RL algorithms (Fig. 3, Tab. 2, Tab. 3)? (4) Is the policy transfer more beneficial when the training tasks have sparser rewards (Tab. 4)? Experimental details can be found in Appendix C.

### 5.1 Policy Transfer with Fixed Dataset

We test our proposed action translator with fixed datasets of transitions aggregated from pairs of source and target tasks. On MuJoCo environments HalfCheetah and Ant, we create tasks with varying dynamics as in (Zhou, Pinto, and Gupta 2019; Lee et al. 2020; Zhang et al. 2020c). We keep default physics parameters in source tasks and modify them to yield noticeable changes in the dynamics for target tasks. On HalfCheetah, the tasks differ in the armature. On Ant, we set different legs crippled. A well-performing policy is pretrained on the source task with TD3 algorithm (Fujimoto, Hoof, and Meger 2018) and dense rewards. We then gather training data with mediocre policies on the source and target tasks. We also include object manipulation tasks on Meta-World benchmark (Yu et al. 2020b). Operating objects with varied physics properties requires the agent to handle different dynamics. The knowledge in grasping and pushing a cylinder might be transferrable to tasks of moving a coffee mug or a cube. The agent gets a reward of 1.0 if the object is in the goal location. Otherwise, the reward is 0. We use the manually-designed good policy as the source policy and collect transition data by adding noise to the action drawn from the good policy.

<table>
<thead>
<tr>
<th>Setting</th>
<th>Source policy</th>
<th>Transferred policy</th>
<th>Transferred policy</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(Zhang et al. 2020c)</td>
<td></td>
<td>(Ours)</td>
</tr>
<tr>
<td>HalfCheetah Ant</td>
<td>2355.0 ± 395.6</td>
<td>3017.1 ± 59.4</td>
<td>2937.2 ± 9.5</td>
</tr>
<tr>
<td>Cylinder-Mug</td>
<td>0.0 ± 0.0</td>
<td>308.1 ± 7.8</td>
<td>395.6 ± 19.4</td>
</tr>
<tr>
<td>Cylinder-Cube</td>
<td>0.0 ± 0.0</td>
<td>262.4 ± 48.1</td>
<td>446.1 ± 11.1</td>
</tr>
</tbody>
</table>

Table 1: Mean (± standard error) of episode rewards over 3 runs, comparing source and transferred policy on target task.

As presented in Tab. 1, directly applying a good source policy on the target task performs poorly. We learn dynamics model \( F \) on target task with \( L_{for} \) and action translator \( H \) with \( L_{trans} \). From a single source task to a single target task, the transferred policy with our action translator (without conditioning on the task context) yields episode rewards significantly better than the source policy on the target task. Fig. 4 visualizes moving paths of robot arms. The transferred policy on target task resembles the source policy on source
task, while the source policy has trouble grasping the coffee mug on target task. Videos of agents’ behavior are in supplementary materials. Tab. 1 reports experimental results of baseline (Zhang et al. 2020c) transferring the source policy based on action correspondence. It proposes to learn an action translator with three loss terms: adversarial loss, domain cycle-consistency loss, and dynamic cycle-consistency loss. Our loss $L_{\text{trans}}$ (Equation 3) draws upon an idea analogous to dynamic cycle-consistency though we have a more expressive forward model $F$ with context variables. When $F$ is strong and reasonably generalizable, domain cycle-consistency loss training the inverse action translator and adversarial loss constraining the distribution of translated action may not be necessary. Ours with a simpler objective function is competitive with Zhang et al. (2020c).

We extend the action translator to multiple tasks by conditioning $H$ on context variables of source and target tasks. We measure the improvement of our transferred policy over the source policy on the target tasks. On HalfCheetah tasks $\mathcal{T}^{(1)} \ldots \mathcal{T}^{(5)}$, the armature becomes larger. As the physics parameter in the target task deviates more from source task, the advantage of transferred policy tends to be more significant (Fig. 5a), because the performance of transferred policy does not drop as much as source policy. We remark that the unified action translator is for any pair of source and target tasks. So action translation for the diagonal elements might be less than 0%. For each task on Ant, we set one of its four legs crippled, so any action applied to the crippled leg joints is set as 0. Ideal equivalent action does not always exist across tasks with different crippled legs in this setting. Therefore, it is impossible to minimize $\delta$ in Proposition 1 as 0. Nevertheless, the inequality proved in Proposition 1 still holds and policy transfer empirically shows positive improvement on most source-target pairs (Fig. 5b).

5.2 Comparison with Context-based Meta-RL
We evaluate MCAT combining policy transfer with context-based TD3 in meta-RL problems. The action translator is trained dynamically with data maintained in replay buffer and the source policy keeps being updated. On MuJoCo, we modify environment physics parameters (e.g. size, mass, damping) that affect the transition dynamics to design tasks. We predefine a fixed set of physics parameters for training tasks and unseen test tasks. In order to test algorithms’ ability in tackling difficult tasks, environment rewards are delayed to create sparse-reward RL problems (Oh et al. 2018; Tang 2020). In particular, we accumulate dense rewards over $n$ consecutive steps, and the agent receives the delayed feedback every $n$ step or when the episode terminates. To fully exploit the good data collected from our transferred policy, we empirically incorporate self-imitation learning (SIL) (Oh et al. 2018), which imitates the agent’s own successful past experiences to further improve the policy.

We compare with several context-based meta-RL methods: MQL (Fakoor et al. 2019), PEARL (Rakelly et al. 2019), Distral (Teh et al. 2017), and HiP-BMDP (Zhang et al. 2020b). Although the baselines perform well on MuJoCo environments with dense rewards, the delayed environment rewards degrade policy learning (Tab. 2, Fig. 3) because the rare transitions with positive rewards are not fully exploited. In contrast, MCAT shows a substantial advantage in performance and sample complexity on both the training tasks and the test tasks. Notably, the performance gap is more significant in more complex environ-
ments (e.g. HalfCheetah and Ant with higher-dimensional state and sparser rewards). We additionally analyze effect of SIL in Appendix D.4. SIL brings improvements to baselines but MCAT still shows obvious advantages.

<table>
<thead>
<tr>
<th>Setting</th>
<th>Hopper Armature</th>
<th>Half Cheetah Armature</th>
<th>Half Cheetah Mass</th>
<th>Ant Damp</th>
<th>Ant Cripple</th>
</tr>
</thead>
<tbody>
<tr>
<td>MQL</td>
<td>1607.5</td>
<td>-77.9</td>
<td>-413.9</td>
<td>103.1</td>
<td>38.2</td>
</tr>
<tr>
<td>PEARL</td>
<td>1755.8</td>
<td>-18.8</td>
<td>25.9</td>
<td>73.2</td>
<td>3.5</td>
</tr>
<tr>
<td>Distral</td>
<td>1319.8</td>
<td>566.9</td>
<td>-29.5</td>
<td>90.5</td>
<td>-0.1</td>
</tr>
<tr>
<td>HiP-BMDP</td>
<td>1368.3</td>
<td>-102.4</td>
<td>-74.8</td>
<td>33.1</td>
<td>7.3</td>
</tr>
<tr>
<td>MCAT (Ours)</td>
<td><strong>1914.8</strong></td>
<td><strong>2071.5</strong></td>
<td><strong>1771.1</strong></td>
<td><strong>624.6</strong></td>
<td><strong>281.6</strong></td>
</tr>
</tbody>
</table>

Table 2: Test rewards at 2M timesteps, averaged over 3 runs.

5.3 Ablative Study

Effect of Policy Transfer Our MCAT is implemented by combining context-based TD3, self-imitation learning, and policy transfer (PT). We investigate the effect of policy transfer. In Tab. 3, MCAT significantly outperforms MCAT w/o PT, because PT facilitates more balanced performance across training tasks and hence better generalization to test tasks. This empirically confirms that policy transfer is beneficial in meta-RL on sparse-reward tasks.

<table>
<thead>
<tr>
<th>Setting</th>
<th>Hopper Armature</th>
<th>Half Cheetah Armature</th>
<th>Half Cheetah Mass</th>
<th>Ant Damp</th>
<th>Ant Cripple</th>
</tr>
</thead>
<tbody>
<tr>
<td>MCAT w/o PT</td>
<td>1497.5</td>
<td>579.1</td>
<td>-364.3</td>
<td>187.7</td>
<td>92.4</td>
</tr>
<tr>
<td>MCAT</td>
<td>1982.1</td>
<td>1776.8</td>
<td>67.1</td>
<td>211.8</td>
<td>155.7</td>
</tr>
<tr>
<td>Improve(%)</td>
<td>32.3</td>
<td>206.8</td>
<td>118.4</td>
<td>12.8</td>
<td>68.5</td>
</tr>
</tbody>
</table>

Table 3: Test rewards at 1M timesteps. We report improvements brought by policy transfer (PT).

Sparser Rewards We analyze MCAT when rewards are delayed for different numbers of steps (Tab. 4). When rewards are relatively dense (i.e. delay step is 200), during training, the learned policy can reach a high score on each task without the issue of imbalanced performance among multiple tasks. MCAT w/o PT and MCAT perform comparably well within the standard error. However, as the rewards become sparser, it requires longer sequences of correct actions to obtain potentially high rewards. Policy learning struggles on some tasks and policy transfer plays an important role to exploit the precious good experiences on source tasks. Policy transfer brings more improvement on sparser-reward tasks.

In Appendix, we further provide ablative study about More Diverse Tasks (D.3), Effect of SIL (D.4) and Effect of Contrastive Loss (D.5). Appendix D.6 shows that trivially combining the complex action translator (Zhang et al. 2020c) with context-based meta-RL underperforms MCAT.

6 Discussion

The scope of MCAT is for tasks with varying dynamics, same as many prior works (Yu et al. 2017; Nagabandi et al. 2018; Nagabandi, Finn, and Levine 2018; Zhou, Pinto, and Gupta 2019). Our theory and method of policy transfer can be extended to more general cases (1) tasks with varying reward functions (2) tasks with varying state & action spaces.

Following the idea in Sec. 4, on two general MDPs, we are interested in equivalent state-action pairs achieving the same reward and transiting to equivalent next states. Similar to Proposition 1, we can prove that, on two general MDPs, for two correspondent states $s^{(i)}$ and $s^{(j)}$, the value difference $|V^{\pi^{(i)}}(s^{(i)}, T^{(i)}) - V^{\pi^{(j)}}(s^{(j)}, T^{(j)})|$ is upper bounded by $\frac{d}{1-\gamma}$, where $d$ depends on $D_{TV}$ between the next state distribution on source task and the probability distribution of correspondent next state on target task. As an extension, we learn a state translator jointly with our action translator to capture state and action correspondence. Compared with Zhang et al. (2020c) learning both state and action translator, we simplify the objective function training action translator and afford the theoretical foundation. For (1) tasks with varying reward functions, we conduct experiments on Meta-World moving the robot arm to a goal location. The reward at each step is inversely proportional to its distance from the goal location. We fix a goal location on source task and set target tasks with distinct goal locations. Furthermore, we evaluate our approach on 2-leg and 3-leg HalfCheetah. We can test our idea on (2) tasks with varying state and action spaces of different dimensions because the agents have different numbers of joints on the source and target task. Experiments demonstrate that ours with a simpler objective function than the baseline (Zhang et al. 2020c) can transfer the source policy to perform well on the target task. Details of theorems, proofs, and experiments are in Appendix E.

7 Conclusion

Meta-RL with long-horizon, sparse-reward tasks is challenging because an agent can rarely obtain positive rewards, and handling multiple tasks simultaneously requires massive samples from distinctive tasks. We propose a simple yet effective objective function to learn an action translator for multiple tasks and provide the theoretical ground. We develop a novel algorithm MCAT using the action translator for policy transfer to improve the performance of off-policy, context-based meta-RL algorithms. We empirically show its efficacy in various environments and verify that our policy transfer can offer substantial gains in sample complexity.
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References


