Abstract

Multi-agent Path Finding (MAPF) deals with finding collision-free paths for a set of agents on a graph, where each agent has its origin and destination. Colored MAPF is a generalization of MAPF, where groups of agents are moving, and the set of destination nodes is specified per group rather than per agent. OzoMorph is software providing an intuitive user interface for specifying Colored MAPF problems, solving them by translation to SAT, and finally visualizing the solution either in a computer simulation or by converting the plans to executable instructions for Ozobot Evo robots.

Introduction

Multi-agent Path Finding is a growing research area dealing with finding collision-free paths for a set of agents – robots (Stern et al. 2019). The problem has numerous applications in automated warehousing, parking, airplane taxing, and computer games. The environment in which the robots move is usually abstracted as an undirected graph, where robots can wait in nodes and move over the edges to reach their destination. Frequently, this graph is a 4-connected grid as it can naturally cover various maps and has the property of equally long edges, which simplifies the synchronization of agents. The task is to find a path for each agent from its start node to its destination node. The paths should be collision-free, which means that robots should not crash into each other. There are various formal descriptions of collisions (Stern et al. 2019), the most widely used are vertex collisions (agents are at the same vertex at the same time) and swapping collisions (agents swap their positions using the same edge). As robots might be late when executing their plans, k-robust plans were introduced that guarantee collision-free execution even if an agent is late for at most k actions (Atzmon et al. 2020). The usual abstract actions used in plans are move (to a neighboring node) and wait (in a given node). These actions are supposed to have identical duration to ensure that robots stay synchronized during execution. However, the same durations may prolong the plan execution as some actions (such as moving forward) are naturally faster than others (such as turning and then moving forward). Therefore models with variable action duration (Barták, Švancara, and Vlk 2018) or with an extended set of actions (for example, by turning actions) (Barták et al. 2019) were proposed.

In this paper, we focus on the generalization of MAPF called Colored MAPF (Solovey and Halperin 2014), where destinations are specified for agent groups rather than for individual agents. Specifically, we present software OzoMorph that demonstrates solving Colored MAPF and executing the plans on robots called Ozobots (Evolve, Inc. 2018). The software allows users to define the problem quickly. We use rectangular 4-connected grids for maps, so users need to specify the grid’s size and agent groups’ initial and goal positions only. The problem is then solved by translation to SAT via the Picat system (Zhou and Kjellerstrand 2016). We use the model with the move, turn, and wait actions with 1-robustness to ensure smooth execution of plans on robots (Barták et al. 2019). The found plans are demonstrated either in simulation on a computer screen or on real robots, where the system generates control instructions for Ozobots. The whole system looks like an artistic tool where one picture – the composition of robots – automatically transforms/morphs into another picture.

Colored MAPF

Let $A = \{1, \ldots, n\}$ be a set of $n$ agents and $G = (V, E)$ be an un-directed graph. Agents are initially staying at some nodes, which is described by initial configuration $S: A \rightarrow V$, where $S(a)$ is the initial position of agent $a$. The final configuration is given by a set of nodes $T \subset V$ such that $|T| = |A|$. Anonymous MAPF problem is given by a quadruple $(G, A, S, T)$ and its solution is a set of collision-free plans. A plan $\pi_a$ for an agent $a$ is a sequence of vertices such that $\pi_a[1] = S(a)$ and for each $t$ either $\pi_a[t] = \pi_a[t+1]$ (agent waits at vertex) or $(\pi_a[t], \pi_a[t+1]) \in E$ (agent moves to a neighboring vertex). Let $m_a$ be the length of plan for agent $a$, then we define $\pi_a[t] = \pi_a[m_a]$ for each $t > m_a$ (agents stay in their final nodes). Let $mks = \max_{a \in A} m_a$ be a makespan of the plans. We require agents to reach the final configuration: $\forall v \in T \exists a \in A : \pi_a[mks] = v$, and the plans to be collision free: $\forall a_1, a_2 \in A, a_1 \neq a_2, \forall t : \pi_{a_1}[t] \neq \pi_{a_2}[t]$ (no vertex collision) and $\forall a_1, a_2 \in A, a_1 \neq a_2, \forall t : \pi_{a_1}[t] \neq \pi_{a_2}[t+1] \lor \pi_{a_1}[t+1] \neq \pi_{a_2}[t]$ (no swapping collision).

Colored MAPF (also called Team MAPF or TAPF) with $k$
groups is then given as \( (G, (A_1, S_1, T_1), \ldots, (A_k, S_k, T_k)) \), where each \( (G, A_i, S_i, T_i) \) is anonymous MAPF (Solovey and Halperin 2014). A solution of Colored MAPF is union of solutions of individual anonymous MAPF problems such that the plans across the groups are also collision-free.

Anonymous MAPF can be solved makespan-optimally in polynomial time (Yu and LaValle 2012), but finding a makespan-optimal solution to Colored MAPF is NP-hard (Surynek 2010) (as Colored MAPF is a generalization of classical MAPF, where each agent has own destination). There exists an optimal algorithm for solving Colored MAPF, called Conflict-Based Min-Cost-Flow (Ma and Koenig 2016), but in this work, we decided to adopt an SAT-based approach for two reasons. First, the model for classical MAPF (Barták et al. 2017) can be easily modified to solve Colored MAPF (only the final condition is changed). Second, this approach gives flexibility in exploring different models. In particular, we added constraints for 1-robustness, and we used finer-resolution actions that included turning. This approach gives plans that are more robust during execution on robots (Barták et al. 2019).

OzoMorph Software

OzoMorph is a Java program for formulating Colored MAPF problems, their solving by translation to SAT, and demonstrating the plans either by simulation on a computer screen or by executing on robots Ozobot Evo. The user first enters the size of the 4-connected grid map and then freely allocates “robots” to their initial positions in one map and final positions in the other map (see Figure 1). Colors identify robot groups, so the above formulation corresponds to the Colored MAPF problem. Artistically speaking, the user paints two pixel-based color pictures, where the number of pixels of the same color at both pictures must be identical. The software indicates these numbers, so it is easy to spot if some agents are missing in either picture. Then, by pressing a single button, the software generates the problem instance for the Picat-based solver and solves it. As described above, we use the model with the move, turn, and wait actions and with 1-robustness constraint. Advanced users may write their models in the Picat programming language.

Obtained plans can then be executed in simulation on a computer screen, or the system can generate control codes for Ozobot Evo robots. These codes are then uploaded to individual robots (usually via Bluetooth). The system supports two modes of execution. In one mode, the robots run on a horizontally-placed computer screen (or a tablet) that shows the map (Figure 2) and starts all the robots synchronously by displaying a specific color on the screen. In the second mode, the robots run on a paper map that can be printed from the application. Then robots must be started one by one at specified times (the application provides the timer) to ensure that the plans start synchronously.

When translating the abstract plans obtained from the Picat solver, the system uses predefined templates for actions written in the Ozoblockly language (Evollve, Inc. 2015) – the visual language for programming Ozobots (Figure 3). Advanced users may redefine these templates to use different control sequences for actions.

Figure 1: OzoMorph user interface with the initial (left) and final (right) configurations of robots.

Figure 2: Ozobot Evo robots on a screen displaying the map.

Conclusions

The OzoMorph software supports the whole development cycle for Colored MAPF, starting with the visual definition of the problem instance, solving the problem, and finishing with the translation of plans to robot control sequences or simulating the plans. The software can be used for artistic purposes to generate plans morphing one configuration of robots to another configuration and for research purposes to compare different SAT-based models of the problem and different translations to robot control sequences.

Acknowledgments

This work is supported by the project P103-19-02183S of the Czech Science Foundation.

References


Figure 3: Example of Ozoblockly code for one robot.


