FC-GAGA: Fully Connected Gated Graph Architecture for Spatio-Temporal Traffic Forecasting

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Abstract
Forecasting of multivariate time-series is an important problem that has applications in traffic management, cellular network configuration, and quantitative finance. A special case of the problem arises when there is a graph available that captures the relationships between the time-series. In this paper we propose a novel learning architecture that achieves performance competitive with or better than the best existing algorithms, without requiring knowledge of the graph. The key element of our proposed architecture is the learnable fully connected hard graph gating mechanism that enables the use of the state-of-the-art and highly computationally efficient fully connected time-series forecasting architecture in traffic forecasting applications. Experimental results for two public traffic network datasets illustrate the value of our approach, and ablation studies confirm the importance of each element of the architecture. The code is available here: https://github.com/boreshkinai/fc-gaga.

1 Introduction
Many multivariate time-series (TS) forecasting problems naturally admit a graphical model formulation. This is especially true when the entities whose past is observed and whose future has to be predicted affect each other through simple causal relationships. For example, introducing pepsi products in a store will very likely decrease future sales of coca-cola; car traffic congestion at one point on a highway is likely to slow down the traffic at preceding highway segments. Without graphical modeling, the model is blind to these nuances, making entity interactions a collection of confounding factors, extremely hard for the model to explain and predict. Equipped with a learnable model for entity properties (e.g. entity embeddings), a model for entity interactions (e.g. graph edge weights), and a mechanism to connect them to a TS model (e.g. a gating mechanism), we can learn the otherwise unknown entity interactions to improve forecasting accuracy.

Problems amenable to graphical TS modeling include forecasting demand for related products (Singh et al. 2019), electricity demand (Rolnick et al. 2019), road traffic (Shi et al. 2020) or passenger demand (Bai et al. 2019). Recent studies have shown that models that explicitly account for the underlying relationships across multiple TS outperform models that forecast each TS in isolation. Although the inclusion of graph modeling has proven to improve accuracy, current models have several serious limitations. First, the complexity and therefore runtime of these models is significantly higher. Second, some models rely on the definition of relationships between variables provided by a domain expert (e.g. an adjacency matrix is heuristically defined based on the geographical relationships between observed variables). Finally, existing models tend to rely on Markovian assumptions to make modelling the interactions across variables tractable.

To address these limitations we propose a novel architecture, called FC-GAGA, that is based on a combination of a fully-connected TS model N-BEATS (Oreshkin et al. 2020) and a hard graph gate mechanism proposed in this paper. To produce the forecast for a single TS (node in the graphical model), it weighs the historical observations of all other nodes by learnable graph weights, gates them via a ReLU and then stacks gated observations of all nodes to process them via fully connected residual blocks (see Fig. 1). The advantages of this architecture are threefold. First, the architecture does not rely on the knowledge of the underlying graph focusing on learning all the required non-linear predictive relationships instead. Second, the basic layer of the architecture is stackable and we allow every layer to learn its own graph structure. This endows the model with the ability to learn a very general non-Markovian information diffusion process that can be learned effectively, which we show empirically. Finally, FC-GAGA is a very memory and computation efficient architecture, which we demonstrate via profiling. Ablation studies demonstrate that when using the efficient fully-connected residual time-series prediction module, it is not sufficient to use standard graph attention — the sparsification achieved by our proposed novel graph gate is essential in achieving good predictive performance.

1.1 Problem Statement
Let a graph $G = (V, E)$ be defined as an ordered collection of vertices, $V = 1, \ldots, N$, and edges, $E \subseteq V \times V$. We are interested in the multivariate TS forecasting problem defined on this graph. Each vertex $v$ in the graph is assumed to generate a sequence of observations, $y_v = [y_{v,1}, \ldots , y_{v,T}] \in \mathbb{R}^T$, governed by an unknown stochastic random process. The graph connectivity encoded in $E$ is assumed to capture unknown relations between the vertices. For example, the graph

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The Thirty-Fifth AAAI Conference on Artificial Intelligence (AAAI-21)
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We propose a novel principle of combining a fully connected vector of dimensionality \( y \) and a network \( R \) of all such vectors comprises node embedding matrix \( W \). We expect that the magnitudes of edge weights \( W_{i,j} \) will reflect the strength of mutual influence between the pair of nodes \((i,j)\) at a given FC-GAGA layer.

**Time gate block** The time gate block models the time covariate features (e.g., time-of-day, day-of-week, etc.) that may be available together with the node observations. We propose to model time-related features using a multiplicative gate model that divides/multiplies the input/output of the FC-GAGA layer by time effects derived from the time feature via a fully connected network as depicted in Fig. 1. Additionally, the input feature vector is concatenated with the node embedding to account for the fact that each node may have a different seasonality pattern. This is equivalent to removing a node-specific multiplicative seasonality from the input of the block and applying it again at the output of the block. We allow the input and output time effects to be decoupled via separate linear projection layers, because in general time at the input and at the output is different.

**Graph gate block** The input to the FC-GAGA layer is a matrix \( \mathbf{X} \in \mathbb{R}^{N \times w} \) containing the history of length \( w \) of all nodes in the graph. We denote by \( \mathbf{x} \) the maximum of the input values over the time dimension, \( \mathbf{x}_i = \max_j \mathbf{X}_{i,j} \). The gating operation produces matrix \( \mathbf{G} \in \mathbb{R}^{N \times N_w} \). Row \( i \) of the gated matrix corresponds to node \( i \) and it contains all the information accumulated by the graph during past \( w \) steps:

\[
G_{i,j+k} = \text{ReLU}[(\mathbf{W}_{i,j} \mathbf{X}_{j,k} - \mathbf{x}_i) / \mathbf{x}_i].
\]

Graph gate relates the information collected by nodes \( i, j \) via two mechanisms. First, the measurements in nodes \( i \) and \( j \) are related to each other by subtraction and levelling operations inside ReLU. Furthermore, the ReLU operation has the function of shutting off the irrelevant \( i, j \) pairs while not affecting the scale alignment achieved via \( \mathbf{W}_{i,j} \). The magnitude of \( \mathbf{W}_{i,j} \) affects the probability of opening the hard gate. Our empirical study shows that the magnitude of \( \mathbf{W}_{i,j} \) correlates

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**Figure 1:** FC-GAGA block diagram each layer includes a graph gate, a time gate and a fully connected time-series model.

edges \( E \) may reflect the connectivity of roads in a road network and \( y_v \) may be the sequence of observations of traffic velocity. The task is to predict the vector of future values \( y_v \in \mathbb{R}^H = [y_{v,T+1}, y_{v,T+2}, \ldots, y_{v,T+H}] \) for every vertex \( v \) based on the observations generated by all the vertices in the graph up to time \( T \). The model input of length \( w \leq T \) at vertex \( v \), ending with the last observed value \( y_{v,T} \), is denoted \( \mathbf{x}_v \in \mathbb{R}^w = [y_{v,T-w+1}, \ldots, y_{v,T}] \). We denote \( \mathbf{y}_v \) the point forecast of \( y_v \) at vertex \( v \).

**Metrics:** We measure accuracy via Mean Absolute Error (MAE), Mean Absolute Percentage Error (MAPE), and Root Mean Squared Error (RMSE): MAE, \( \frac{1}{N} \sum_{v=1}^{N} |y_{v,T+H} - \hat{y}_{v,T+H}| \), MAPE, \( \frac{1}{N} \sum_{v=1}^{N} \frac{|y_{v,T+H} - \hat{y}_{v,T+H}|}{|y_{v,T+H}|} \), and RMSE, \( \sqrt{\frac{1}{N} \sum_{v=1}^{N} (y_{v,T+H} - \hat{y}_{v,T+H})^2} \).

1.2 Summary of Contributions

We propose a novel principle of combining a fully connected state-of-the-art univariate TS forecasting model NBEATS (Oreshkin et al. 2020) with a learnable time gate and a learnable hard graph gate mechanisms. We empirically show that the proposed model learns the graph parameters effectively from the data and achieves impressive predictive performance. We show that the proposed model offers computational advantage and reduces the training time by at least a factor of three relative to models with similar accuracy.
We assume that without the hard gating the graph weighting is not effective. We believe this is due to the fact that for each target node there are only a few nodes that are relevant at a given layer, so the input to the fully connected architecture is supposed to be sparse. Hard gating encourages sparsity. Soft gating provides input that is not sparse, overwhelming a fully connected network with too many low-magnitude inputs originating from many nodes in the graph. Additionally, according to the complexity analysis presented at the end of this section, our graph gate design has $N$ times smaller complexity, $O(N^2)$, compared to the approaches known in the literature that are based on matrix multiplication in the graph diffusion step $O(N^3)$ (e.g. DCRNN and Graph WaveNet).

**Fully connected time-series block** We propose a fully connected residual architecture with $L$ hidden layers, $R$ residual blocks and weights shared across nodes. Its input for node $i$, $Z_i$, is conditioned on the node embedding and its own history: $Z_i = [E_i X / X_i] \theta_i G_i^T$. Using residual block and layer superscripts and denoting the fully connected layer with weights $A^{r, l}$ and biases $b^{r, l}$ as $FC_{r,l}^{(l)}(H^{r,l-1}) \equiv \text{ReLU}(A^{r, l}H^{r,l-1} + b^{r, l})$, the operation of the fully connected residual TS modeling architecture is described as follows:

$$
Z' = \text{ReLU}[Z'^{-1} - Z^{-1}],
$$
$$
H^{l,1} = FC_{r,1}(Z'), \ldots, H^{l,L} = FC_{r,L}(H^{l,L-1}),
$$
$$
\hat{Y}' = B' H^{L,1}.
$$

We assume $\hat{Z}' \equiv 0$, $Z'^{-1} \equiv Z$; projection matrices have dimensions $B' \in \mathbb{R}^{N(w+1)+d \times d_h}$, $F' \in \mathbb{R}^{d_h \times H}$ and the final forecast is the sum of forecasts of all residual blocks, $\hat{Y} = \sum \hat{Y}'$.

**FC-GAGA layer stacking** is based on the following three principles. First, the next layer accepts the sum of forecasts of previous layers as input. Second, each FC-GAGA layer has its own set of node embeddings and thus its own graph gate. Thus each layer is provided a freedom to gate the information flow across nodes in accordance with the processing already accomplished by the previous layer. For example, in the first FC-GAGA layer, for node id 5, it may be optimal to focus on the histories of node ids [10, 200, 500]. However, since the first FC-GAGA layer updates the states of all nodes, node 5 may no longer need the information provided by nodes [10, 200, 500], nor by their neighbours; and instead may wish to focus on node ids [3 and 15], as they now provide more important information. This is clearly a more flexible information diffusion model than the Markov model based on node proximity that is common in the traffic forecasting literature (Li et al. 2018). Finally, the final model output is equal to the average of layer forecasts.

**Complexity analysis** In the following analysis we skip the batch dimension and compute the complexity involved in creating a single forecast of length $H$ for all nodes $N$ in the graph when the input history is of length $w$, the node embedding width is $d$ and the hidden layer width is $d_h$. Analysis details can be found in Appendix B. The graph gate block has complexity $O(N^2(w+d))$, as is evident from eq. (2). The time gate mechanism producing a seasonality factor for each node using its associated time feature scales linearly with the number of nodes, the hidden dimension, the input history length: $O(N(d + w) d_h)$. Finally, the fully-connected TS model with $L$ FC layers and $R$ residual blocks that accepts the flattened input $N \times Nw$ has complexity $O(R(2N^2w d_h + (L-2)Nd_h^2))$. In most practical configurations, the total complexity of the model will be dominated by $O(N^2 Rwd_h)$.

### 3 Empirical Results

**Datasets** FC-GAGA is evaluated on two traffic datasets, METR-LA and PEMS-BAY (Chen et al. 2001; Li et al. 2018) consisting of the traffic speed readings collected from loop detectors and aggregated over 5 minute intervals. METR-LA contains 34,272 time steps of 207 sensors collected in Los Angeles County over 4 months. PEMS-BAY contains 52,116 time steps of 325 sensors collected in the Bay Area over 6 months. The datasets are split in 70% training, 10% validation, and 20% test, as defined in (Li et al. 2018).

**Baselines** We compare FC-GAGA both with temporal models that do not require a pre-specified graph and spatio-temporal models that may rely on a pre-specified graph or have a learnable graph. The following univariate temporal models provided by (Li et al. 2018) are considered: ARIMA (Makridakis and Hibon 1997), implemented using a Kalman filter; SVR (Wu, Ho, and Lee 2004), a linear Support Vector Regression model; FNN, a Feedforward Neural Network; and FC-LSTM (Sutskever, Vinyals, and Le 2014), a sequence-to-sequence model that uses fully connected LSTMs in encoder and decoder. The spatio-temporal models include DCRNN (Li et al. 2018) (Diffusion Convolutional Recurrent Neural Network, a graph convolutional network inside the sequence-to-sequence architecture); STGCN (Yu, Yin, and Zhu 2018) (Spatio-Temporal Graph Convolutional Network, merges graph convolutions with gated temporal convolutions); Graph WaveNet (Wu et al. 2019), fuses graph convolution and dilated causal convolution; GMAN (Zheng et al. 2020) (Graph Multi-Attention Network, an encoder-decoder model with multiple spatio-temporal attention blocks, and a transform attention layer between the encoder and the decoder); STGRAT (Park et al. 2019) (Spatio-Temporal Graph Attention Network for Traffic Forecasting, an encoder-decoder model using the positional encoding method of the Transformer (Vaswani et al. 2017) to capture features of long sequences and node attention to capture spatial correlation) . Of these methods, only Graph Wavenet can generate predictions without a pre-specified graph. For DCRNN, we report the results after bug fix in the code, which are better than the reported results in the paper. For STGCN, Graph WaveNet, GMAN, and STGRAT we use the settings and report results from the original papers.

**FC-GAGA architecture details and training setup** Scalar $\varepsilon$ in (1) is set to 10. The embedding dimensionality, $d$, is set to 64 and the hidden layer width $d_h$ for all fully connected layers is set to 128. The number of layers $L$ in the fully-connected TS model is equal to 3 and the number of blocks $R$ is equal to 2. We use weight decay of $1e-5$ to regularize fully-connected layers. The model is trained using
Table 1: Error metrics computed using the standard protocol (Wu et al. 2019) (average over last time step of horizon, input window length 12). Lower numbers are better. §Graph WaveNet trained using official code by the authors using only adaptive adjacency matrix without the support of geographical adjacency matrix. ‡FC-GAGA(4 layers) is the proposed model with 4 layers. In the fourth layer, the graph gate weights are set to the identity matrix, implying more reliance on the pure time-series component.

The final FC-GAGA forecast is composed of the average of the forecasts of individual layers. Figure 2 shows the contributions of different layers to the final 15 min ahead forecast (after scaling by the averaging factor 1/3). We can see that the role of the first layer is mostly to provide a baseline forecast, while at the same time accounting for some seasonal effects. The layer 2 contribution to the prediction clearly captures daily seasonality. Layer 2 and especially layer 3 provide iterative correction terms to the original baseline produced by layer 1, based on the most recent data. This is especially evident for layer 3 whose output is inactive most of the time, becoming active when significant correction is required because the observed signals undergo significant stochastic changes in short periods of time.

Qualitative results The key empirical results appear in Table 1. FC-GAGA compares favourably even against graph-based models that rely on additional external graph definitions on both METR-LA and PEMS-BAY datasets (DCRNN, STGCN, Graph WaveNet, and GMAN). Most of the time, FC-GAGA outperforms Graph WaveNet model when they are trained and evaluated in the same conditions, i.e. both models only rely on the graph learned from the data (Graph WaveNet is using only the adaptive adjacency matrix that it learns from the data). It significantly outperforms the univariate models (ARIMA, SVR, FNN, and FC-LSTM). Note that STGRAT heavily relies on the main ingredients of Transformer architecture such as positional encoding and attention mechanisms. Therefore, comparing FC-GAGA against it gives a good idea of how our approach stands against Transformer-based methods in terms of accuracy.

Quantitative results Our key empirical results appear in Table 1. FC-GAGA compares favourably even against graph-based models that rely on additional external graph definitions on both METR-LA and PEMS-BAY datasets (DCRNN, STGCN, Graph WaveNet, and GMAN). Most of the time, FC-GAGA outperforms Graph WaveNet model when they are trained and evaluated in the same conditions, i.e. both models only rely on the graph learned from the data (Graph WaveNet is using only the adaptive adjacency matrix that it learns from the data). It significantly outperforms the univariate models (ARIMA, SVR, FNN, and FC-LSTM). Note that STGRAT heavily relies on the main ingredients of Transformer architecture such as positional encoding and attention mechanisms. Therefore, comparing FC-GAGA against it gives a good idea of how our approach stands against Transformer-based methods in terms of accuracy.
nodes; the learned relationships differ significantly across layers, indicating information aggregation from different spatial regions. In Fig. 4 (left) we observe that the gating is less strictly enforced in the first layer (the average $W_{i,j}$ values are higher in the first layer) and the geographic distribution of values is more dispersed (see Fig. 3, left). We interpret this as indicating that in layer 1 FC-GAGA collects information across a wide variety of nodes and geographical locations to construct a stable baseline forecast. As we move from layer 2 to layer 3, we can see that the nodes with highest graph weights more tightly concentrate around the target node for which the forecast is produced (see Fig. 3, middle and right and Fig. 4, right). Fig. 4 (left) indicates that many more $W_{i,j}$ have smaller values progressively in layers 2 and 3, implying stricter gating in eq. (2). Our interpretation of this is that to provide iterative updates to the baseline forecast, FC-GAGA focuses on the nodes that are closer to the target node and restricts the information flow such that the correction terms are defined by the nodes with the most relevant information.

Ablation studies  Our ablation studies validate the effectiveness of the FC-GAGA layer stacking mechanism, the graph gating mechanism and the time gate. Table 2 demonstrates the performance of FC-GAGA as a function of the number of layers. Increasing the number of layers leads to substantial improvement on the METR-LA dataset, while on PEMS-BAY the number of layers does not affect performance significantly. METR-LA is known to be a harder problem than PEMS-BAY because of the more erratic nature of its TS. This implies that increasing the number of FC-GAGA layers to solve harder problems may bring additional accuracy benefits while using only one FC-GAGA layer to solve an easier problem may be beneficial from the computational efficiency standpoint (the runtime scales approximately linearly with the number of layers). The final row in the table (4I) shows the performance when the fourth layer is set to the identity, so that the layer focuses on forming a prediction using only the history of each node. This approach leads to a noticeable improvement; forcing one layer to learn univariate relationships can be beneficial.

The top section of Table 3 shows the results of ablating the graph gate and time gate mechanisms with a 3-layer FC-GAGA network. Both the time gate and graph gate individually lead to improvements over a straightforward multivariate N-BEATS model and then combine to offer further improvement. The bottom section of the table examines different approaches for the graph gate. “graph attention” is a standard graph attention approach that does not perform hard gating. We see that the sparsification provided by our proposed gate is essential; graph attention is even outperformed by the univariate FC-GAGA model (“identity”). The univariate FC-GAGA outperforms all univariate methods in Table 1 by a large margin. When $W$ is set to all ones (“ones”), FC-GAGA can learn relationships between different nodes, but it cannot emphasize influential nodes. We examine three learnable options: “shared learnable” where all layers share a single learnable $W$, “learnable first layer” where $W$ associated with
the first layer is learnable and it is set to the ones matrix for other layers, and the fully learnable FC-GAGA approach. Allowing the architecture to learn a different weight matrix for each layer leads to the best prediction performance, and the additional computational overhead is very minor.

**Profiling results** To confirm FC-GAGA’s computational efficiency we conducted a profiling experiment using a P100 GPU in the default Google Colab environment. We profiled the original codes provided by the authors of DCRNN (Li et al. 2018) and Graph Wavenet (Wu et al. 2019). We profiled our tensorflow 2.0 implementation of FC-GAGA, which relies on standard Keras layer definitions, with no attempt to optimize for memory or speed. Table 4 clearly shows that FC-GAGA is more computationally effective as it consumes approximately half the memory and compute time of Graph WaveNet and is about 10 times faster than DCRNN and about 5-10 times more memory efficient. We can also see that it scales well between METR-LA (207 nodes) and PEMS-BAY (325 nodes) datasets, which may be an important property for handling larger scale problems with thousands of nodes.

### 4 Related Work

Multivariate TS prediction or forecasting has been studied intensively for decades. Historically, neural network approaches struggled to compete with state-of-the-art statistical forecasting models. Recently, several neural network architectures that are trained on many time series, but then form predictions for a single variable based on its past history (and covariates) have eclipsed statistical methods (Salinas et al. 2019; Oreshkin et al. 2020; Smyl 2020). In contrast to our work, these architectures do not simultaneously form forecasts for multiple time series using past information from all of them. Other methods use multiple input time-series to predict a single target TS (Bao, Yue, and Rao 2017; Qin et al. 2017; Lai et al. 2018; Guo and Lin 2018; Chang et al. 2018). For these architectures, several innovations have proven effective, including attention mechanisms to determine which input variables and time lags to focus on (Qin et al. 2017; Guo and Lin 2018; Munkhdalai et al. 2019; Liu, Lu, and Cai 2020). In this vein, the transformer architecture is modified in (Li et al. 2019) to address TS forecasting and DeepGLO (Sen, Yu, and Dhillon 2019) is a hybrid model that combines regularized matrix factorization with a temporal convolution network for local prediction.

**Graph-based models** In some settings, we are provided with a graph that is thought to capture the relationships between the variables. The neural network architectures usually combine graph convolutional networks (GCNs), which can focus on spatial relationships, with GRUs, LSTMs, TCNs, or RNNs (Zhao et al. 2019; Li et al. 2018; Huang et al. 2019; Yu, Yin, and Zhu 2018; Chen et al. 2019). A few approaches apply graph-based learning directly to a spatio-temporal graph (Yu et al. 2019; Song et al. 2020). Performance can be improved using attention mechanisms (Guo et al. 2019; Bai et al. 2019; Park et al. 2019; Zheng et al. 2020; Shi et al. 2020). More advanced architectures also offer an avenue for improvement. ST-UNet (Yu, Yin, and Zhu 2019) employs spatio-temporal pooling/unpooling to allow the architecture to learn represen-
### Table 3: Ablation study: the effectiveness of the FC-GAGA graph gate and time gate

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Table 4: Profiling results: total training and evaluation runtime, and GPU memory utilization. Measured using official DCRNN and Graph WaveNet codes and our non-optimized tensorflow implementation of FC-GAGA on NVIDIA P100 GPU in the default Google Colab environment.

6 Conclusions

We proposed and empirically validated a novel neural architecture for spatio-temporal forecasting, which we call FC-GAGA (Fully Connected Gated Graph Architecture). FC-GAGA combines a fully connected TS model with temporal and graph gating mechanisms, that are both generally applicable and computationally efficient. We empirically demonstrate that the proposed model can be learned efficiently from the data to capture non-Markovian relations across multiple variables over layers in the architecture, resulting in excellent generalization performance. We further profile FC-GAGA’s training and inference runtime and demonstrate that it is several times more efficient in the utilization of GPU memory and compute than existing models with comparable accuracy. Our results provide compelling positive evidence to stimulate the development of fully connected architectures for graph based information processing.
References


